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CENTER FOR ECONOMIC STUDIES

TRUTH OR CONSEQUENCES?
ENFORCING POLLUTION
STANDARDS

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ENFORCING POLLUTION STANDARDS

Abstract

Evidence suggests that a surprisingly large fraction of firms comply with pollution emission standards even though expected penalties for noncompliance are low. We offer an explanation of this puzzle by extending the standard model of enforcement to include a self-reporting requirement and enforcement power. These extensions are enough to overturn the conventional result that higher fines lead to higher compliance rates. Specifically, under plausible conditions, higher compliance rates are achieved with lower fines for noncompliance. In addition, the cost of enforcing a given level of aggregate pollution is then minimized by setting the fine for noncompliance equal to zero.

Keywords: pollution control, environmental regulation, compliance, self-reporting

JEL: D62, D82, L51

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1. Introduction

Theory suggests that firms comply with pollution laws when the cost of compliance is less than the expected penalty for noncompliance and not otherwise. The empirical implication is that we should observe, *ceteris paribus*, low compliance rates when expected penalties are low and high compliance rates when expected penalties are high. It is puzzling therefore, that we commonly observe high compliance rates even when expected penalties are very low. For example, Russell, Harrington and Vaughan (1988) observe that expected penalties for noncompliance with pollution standards are low in the U.S. and yet, compliance rates are surprisingly high. Cropper and Oates (1992) concur that substantial compliance seems to exist even though few polluters have actually been fined for their violations. Moreover, they note, where such fines have been levied, they have been quite small.¹ Evidence from Canada shows a similar pattern. Data on industrial compliance rates over the period 1986-89 show that six of the nine industrial sectors were in compliance with all monthly pollution standards more than 70 percent of the time.² Yet plants that violate monthly pollution limits are rarely fined.³

If the expectation of being fined is low, why do firms comply with pollution standards? The purpose of this paper is to address this question. We construct a model that extends the standard enforcement model in two directions. The first is a requirement that firms monitor their own pollution emissions and report their compliance status to the enforcement agency; the agency can then choose whether or not to use this information. Self-reporting is becoming an increasingly common feature of enforcement, particularly enforcement of pollution standards. The second is to allow the enforcement agency the power to exploit the information revealed through self-reported violations. This, too, is a common feature of law enforcement. When a firm

¹Cropper and Oates (1992) pages 696-7.

²Of the remaining three sectors, only one shows compliance rates below 50 percent. These data apply to the Province of Ontario and are taken from the Ontario Ministry of the Environment, Annual Direct Discharge Reports.

³No comprehensive data set exists on enforcement activity. However, available evidence taken from Statistics Canada, "Human Activity and the Environment", Catalogue 11-509E Occasional, indicates that convictions and fines are rare. For example, from April to September 1991, of the 1872 inspections conducted by Environment Canada, 49 warnings were issued to firms and yet only 6 were prosecuted. Over the 30 month period from April 1988 to September 1990, a total of 33 fines were levied in all of Canada by Environment Canada.

has been identified as a violator of a pollution law, it is common and, indeed, rational for the enforcement agency to take enforcement actions.

Our paper is closest in purpose to Harrington (1988) who attempts to explain the puzzling phenomenon of high compliance rates and low expected fines by modelling enforcement as a repeated game between the agency and the firm. Just as insurance companies use experience-rating to better judge the risk class of their customers, Harrington allows the agency to use firms' past compliance behaviour to divide them into low- and high-risk (of violation) groups. Harrington shows that the compliance rate of firms in the second group is maximized by setting fines for noncompliance as high as possible for the second group but equal to zero (the lowest possible) for firms in the first group. As a result, his model predicts we should never observe first-time offenders being fined.

Our paper is closest in structure to Kaplow and Shavell (1994) and Malik (1993) who add a self-reporting requirement to the standard model of enforcement. In this setting, firms would confess to (self-report) violating a pollution standard only if they expected that not confessing would lead to a more severe punishment. If we let F_2 be the fine imposed on violators apprehended through random inspections that occur with probability π and F_1 be the fine imposed with certainty on firms that confess to a violation, we clearly need $F_1 \leq \pi F_2$ to induce firms to confess truthfully. Malik and Kaplow and Shavell show that the addition of a self-reporting requirement to the standard probabilistic model of enforcement unambiguously raises social welfare. One way to see this is that it lowers the cost of enforcement because it reduces the number of firms that need to be inspected.⁴

We offer a different explanation than Harrington (1988) of the puzzling observation of high compliance rates and low expected fines in this paper. While not denying the important leverage that memory gives the enforcement agency by allowing it to use experience rating, we abstract from it in this paper in order to focus on the different but, we believe, equally important enforcement tools of the self-reporting requirement and enforcement power.

Our model differs in structure from Malik (1993) and Kaplow and Shavell (1994) because we allow for repeated interaction between regulator and firms

⁴In the context of pollution control, Swierzbinski (1994) and Harford (1987) include self-reporting as a feature of their analysis; however, neither of these papers relate directly to our paper.

and because we assume the regulator exploits the information revealed when firms self-report. In particular, we assume the regulator has the power to force any firm revealed to be in violation of a pollution law to return to compliance. This has the important implication that truth-telling is not incentive compatible for all firms.

We find that the addition of self-reporting and enforcement power to the standard enforcement model is enough to overturn the conventional result that higher fines lead to higher compliance rates. Specifically, we show that under plausible conditions, compliance rates are a decreasing function of the fine for noncompliance and, that under these conditions, it is optimal to set the fine for noncompliance equal to zero, where the objective is to minimize the social cost of achieving a given pollution target. The implication is that observing low, even zero, fines for noncompliance in some polluting sectors, even though compliance is imperfect, is consistent with rational behaviour by firms and the enforcement agency.

In the next section, we introduce a model of pollution that allows for both deliberate violations of the pollution standard and violations which occur through random equipment failure. The third section introduces the self-reporting requirement and investigates the relationship between the aggregate compliance rate and the fine for noncompliance. In Section 4, we consider the consequences of allowing the enforcement agency to set the non-compliance fine so as to minimize the cost of enforcement. Extensions to the model are considered in Section 5 and conclusions are drawn in Section 6.

2. The pollution model

Firms are assumed to emit a single type of pollution and are required by law to respect an exogenous upper limit on allowable emissions, called the pollution standard. The responsibility of the enforcement agency (which we shall also call the regulator) is to enforce the pollution standard for individual firms; however, pollution emissions are unobservable to the regulator except during costly inspection visits when they can be accurately measured. Firms found in violation of the standard can be charged a fine. We assume there are no costs associated with levying fines.

We distinguish between initial and continuing compliance. A firm is said to be in initial compliance if it has installed a production process that makes compliance technically feasible. For concreteness, we assume the firm is in initial compliance if it has installed a pollution abatement device (PAD) and

not otherwise. Without a PAD, compliance is feasible only by not operating the plant.

It is a relatively simple matter for the regulator to verify a firm's initial compliance status. Inspectors need only determine whether or not a firm's production process is technically capable of meeting the pollution standard, just as an automobile can be inspected to verify the presence of a functioning catalytic converter. A firm that has installed a PAD is said to be in initial compliance.

A firm is said to be in continuing compliance if it actually operates the PAD and repairs it when it fails. It is more difficult for the regulator to verify a firm's continuing compliance status: while a single inspection visit can verify a firm's initial compliance status, repeated, nearly continuous, inspection visits would be required to determine with high probability a firm's continuing compliance status. We focus on the more challenging and interesting problem of continuing compliance in this paper.

The cost of operating the PAD is c per period. A firm's manager can bypass the PAD in production and thereby wilfully violate the pollution standard at a saving of c per period. However, violations of pollution standards probably arise more frequently from a lack of adequate maintenance and repairs to the PAD than from a deliberate act of violation. To capture this, we assume the PAD breaks down with probability β per period. To remain in compliance, the firm must immediately undertake repairs at a cost k which, we assume, leads to instantaneous resumption of its compliance status. If the PAD is not repaired, the firm's pollution emissions increase causing it to be in violation of the pollution standard. It continues to be in violation until the equipment is repaired.

Firms differ according to their compliance cost, c , but we assume that the repair cost, k , is the same for all firms. The distribution function of c , $g(c)$ defined over the interval $[0, \bar{c}]$, is continuous, and is common information to firms and the regulator but the regulator does not know the compliance cost of any individual firm. We define the cumulative distribution function as $G(c)$.

At the beginning of each period, the firm discovers the state of the world that prevails. With probability $(1 - \beta)$, its PAD is functioning and remains functioning for the duration of the period; with probability β , it is broken. If it is broken, it can be repaired immediately at cost k if the firm wishes to remain in compliance. It then returns to the working state for the duration

of the period. If it is not repaired, it remains broken and the firm enters and remains in a state of non-compliance until it is repaired.

Our model contains, as a special case, the standard model of probabilistic enforcement if we rule out the possibility of equipment failure (set $\beta = 0$). Then, firms comply with the pollution standard if they operate the PAD at a cost c . Assuming risk neutrality, a firm complies if

$$c \leq \pi F \quad (1)$$

and does not comply otherwise, where π is the probability of inspection and F is the fine imposed on violators.⁵ On average, the industry compliance rate is $G(\pi F)$.

In the context of pollution control, the enforcement models of Harford (1978) and Storey and McCabe (1980) have this basic flavour although the probability of detection and the size of the fine are allowed to depend on the size of the violation in Harford's model. The industry compliance rate is increased by increasing either the fine, F , or the inspection probability, π . Optimal enforcement, as Becker (1968) first concluded, requires setting the fine at its maximum level, \bar{F} .⁶ As noted earlier, this model is inconsistent with the observation of high compliance rates and low expected fines.

3. Self-Reporting

We assume that firms are required to monitor their own pollution emissions and submit compliance reports to the enforcement agency.⁷ To verify the truthfulness of reports, the agency randomly inspects firms reporting compliance (there is no need to inspect firms reporting non-compliance). The penalty for submitting a false report is a fine, F_2 and an order to return to compliance. The penalty for truthfully reported noncompliance is a fine F_1 and an order to return to compliance.

⁵This model of probabilistic enforcement is best thought of as a one-shot game. If the game were repeated over time, it would be necessary to assume the regulator can commit to not use the information it acquires when a firm is identified as a violator. For example, it must commit to not force the firm to return to compliance through higher sanctions or more intensive monitoring.

⁶The maximum level for the fine is assumed to be beyond the control of the enforcement agency.

⁷Private monitoring costs are assumed to be zero as in Kaplow and Shavell (1994) and Malik (1993).

The order to return to compliance is the only action we assume the regulator takes in response to the information acquired about a firm when it is identified as a type that does not comply.⁸ Firms that have been ordered to return to compliance are allowed one period to comply with that order. We assume all firms delay their return to compliance to the full extent possible but that all do so by the end of the period. This assumption gives considerable enforcement power to the agency; however, we believe it captures an important element of enforcement not currently present in the literature.⁹

We define an *enforcement policy* as a triple $\{F_1, F_2, \pi\}$, $0 \leq F_i \leq \bar{F}$, $i = 1, 2$ and $\pi \in (0, 1)$. We initially study options for firms given an arbitrary enforcement policy and then look at the choice of policy facing the enforcement agency.

Strategy choices

For now, we assume the firm cannot choose to violate the pollution standard by simply not operating the PAD. Instead, violations can occur only after equipment failure. We relax this assumption in Section 5.

A firm can follow one of three strategies, S_{ij} , where $i = C$ or N for compliance or noncompliance and $j = T$ or F for truthful or false reporting of the state of compliance.

1. S_{CT} : full compliance and truth-telling means that the firm operates the PAD at a cost of $c > 0$ per period and repairs the machine (instantaneously) if it breaks, at a cost of $k > 0$. It is clear that there is no

⁸In particular, we assume the regulator does not alter its policy of random inspections in response to information acquired about firms' types. The regulator has no incentive to alter its monitoring of firms that have violated the standard as a result of equipment failure and confess; but it does have an incentive to monitor more intensively firms that have been identified via inspections as violators, just as it does in the standard model of probabilistic enforcement. However, if we allowed for this, our model would mix features of Harrington's (1988) experience-rating model with our self-reporting model. As Harrington has already shown, this would bias our model in favour of providing an explanation for low fines. To avoid this bias, and to focus on the power of self-reporting alone as a possible explanation of low fines, we assume the regulator cannot use experience-rating to adjust inspection rates.

⁹The notable exception is the model of "voluntary compliance" by Russell, Harrington and Vaughan (1986). In practice, the order itself has to be enforced and this is done perhaps with the threat of higher and certain penalties. We take a simplified view of this control process which, we believe, nevertheless captures the essence of enforcement power.

incentive for the fully-complying firm to be other than truthful, so that S_{CF} is ruled out.

2. S_{NT} : non-compliance and truth-telling means that the firm operates the PAD but does not repair it if it breaks down. Under S_{NT} , the firm truthfully reports that it is in a state of non-compliance and can expect certain punitive action.
3. S_{NF} : non-compliance and false reporting means that the firm operates the PAD, does not repair it if it breaks down, but always reports that it is in compliance. In this case, imperfect monitoring by the regulator means that the firm faces some chance of punitive action.

A firm will choose the strategy with the highest expected payoff, which clearly depends on the structure of penalties, costs of operation and repair of the PAD, the probabilities of failure and detection, and the magnitude of any fines imposed by the regulator. A firm that reports a violation is assessed a fine of F_1 and is allowed to operate out of compliance for one period. At the end of the period, it repairs the PAD as required, at cost k . It then starts the next period, once again facing a probability β that the PAD is broken and probability $(1 - \beta)$ that it is not broken.¹⁰

We assume the regulator inspects firms randomly with the probability of a firm being inspected being $\pi \in (0, 1)$. The regulator is able to determine without error the compliance status of the firm at the time of inspection. Effectively then, an inspection determines whether a firm is telling the truth or not.¹¹ Clearly, the regulator does not inspect firms that report a violation, but only those firms claiming to be in compliance.

The optimal policies

Let V_{ij} be the expected discounted profit of a firm following a strategy S_{ij} . Although we set up the model as being dynamic, the horizon is infinite and all the stochastic processes are stationary so that a firm following a particular

¹⁰Note that the PAD only occupies two states: functioning and broken so we are not concerned with issues of 'partial' compliance.

¹¹In reality, the inspection determines whether or not the firm was falsifying records of monitoring and reporting. This might involve tips from disgruntled employees or direct evidence of falsification. However, we take a stylized view of this process by assuming the truth-telling is verified on inspection

strategy at date t will find it optimal to follow the same strategy at date $t+1$. The date subscript is therefore omitted from the calculations below.

The expected value from adopting strategy S_{CT} , (full compliance), is given by

$$V_{CT} = (1 - \beta)(y - c) + \beta(y - c - k) + \delta V_{CT}$$

With probability $1 - \beta$, the PAD does not break and the firm receives net revenue of y less the cost of operating the PAD. With probability β the PAD breaks down and is repaired immediately at cost k . Next period, the firm expects to receive V_{CT} again discounted one period by the discount factor δ . Note that though this firm reports compliance and may therefore be inspected, there are no payoff-relevant implications of such an inspection, as long as the inspection does not interfere with the firm's operation and is totally accurate. Solving this gives

$$V_{CT} = \frac{y - \beta k - c}{1 - \delta} \quad (2)$$

The expected value from adopting strategy S_{NT} , (non-compliance and truth-telling) is

$$V_{NT} = (1 - \beta)(y - c) + \beta(y - F_1 - \delta k) + \delta V_{NT}$$

If the PAD does not fail, (probability $1 - \beta$), net revenues are $y - c$ as before. If the PAD breaks down, (probability β), a non-compliance report is filed, the firm is fined F_1 and is ordered to repair the PAD at the end of the period (hence the discounting factor on k). Note that the cost of operating the PAD, c , is avoided for one period. Next period, the process begins again yielding a present value of δV_{NT} . Solving gives

$$V_{NT} = \frac{y - (1 - \beta)c - \beta(F_1 + \delta k)}{1 - \delta}$$

The expected value from adopting strategy S_{NF} , (non-compliance and non-truth-telling), is more complex because inspection is both possible and will have payoff-relevant consequences. We have

$$V_{NF} = (1 - \beta)[y - c + \delta V_{NF}] + \beta(\pi[y - (F_2 + \delta k) + \delta V_{NF}] + (1 - \pi)[y + \delta V_0]) \quad (3)$$

where

$$V_0 = \pi[y - (F_2 + \delta k) + \delta V_{NF}] + (1 - \pi)[y + \delta V_0] \quad (4)$$

If the machine does not break (with probability $1 - \beta$), the firm complies and continues next period with the same expected payoff discounted by one period. Note again that in this case, the firm will report compliance and, if inspected, will incur no additional costs. If the machine breaks down (with probability β), the firm does not report the violation and does not repair the machine. With probability π , the firm is inspected, fined F_2 , forced to repair the machine next period and continues next period with the expected payoff V_{NF} discounted one period. If the firm is not inspected (with probability $1 - \pi$), it receives net revenue of y this period and incurs no cost of operating the broken PAD. Next period, the firm receives V_0 , which is a recursive formula repeating the same potential sequence of events of being inspected or not. It is the value of starting the period with a broken PAD.

Solving for V_{NF} gives

$$V_{NF} = \frac{y}{1 - \delta} - \left[\frac{(1 - \beta)[1 - \delta(1 - \pi)]c + \beta\pi(F_2 + \delta k)}{(1 - \alpha)(1 - \delta)} \right] \quad (5)$$

where $\alpha \equiv \delta(1 - \pi)(1 - \beta) \in (0, 1)$.

Firms differ in their costs of operating the PAD and are distributed according to the continuous distribution function G , and density g , defined on $c \in [0, \bar{c}]$. A firm with a given c chooses

$$\max_S \{V_{NT}, V_{CT}, V_{NF}\}$$

All payoff functions V are linear and decreasing in c . We have

$$\begin{aligned} \frac{\partial V_{NT}}{\partial c} &= -\frac{1 - \beta}{1 - \delta} < 0 \\ \frac{\partial V_{CT}}{\partial c} &= -\frac{1}{1 - \delta} < 0 \\ \frac{\partial V_{NF}}{\partial c} &= -\frac{(1 - \beta)[1 - \delta(1 - \pi)]}{(1 - \alpha)(1 - \delta)} < 0 \end{aligned}$$

from which we see that

$$\left| \frac{\partial V_{CT}}{\partial c} \right| > \left| \frac{\partial V_{NT}}{\partial c} \right| > \left| \frac{\partial V_{NF}}{\partial c} \right|$$

Given these properties, a number of possibilities arise for the shape of the upper envelope of the value functions. However, the main features of the model are best illustrated by analyzing the case illustrated in Figure 1. Here, we assume that each payoff line intersects the other two in the interior of $[0, \bar{c}]$.

[Figure 1 here]

Figure 1 is drawn so that no strategy is dominated by another over all possible values of compliance cost, c . In this case, firms are sorted into three groups according to which of the three strategies is optimal over some range. For firms with low compliance costs, $0 < c < \hat{c}$, the optimal strategy is S_{CT} , full compliance. Firms with intermediate compliance costs, $\hat{c} < c < \bar{c}$, choose to violate but truthfully report violations to the regulatory agency. Firms with high compliance costs, $\bar{c} < c < c_2$, choose to violate but report instead that they are in compliance. Firms with costs higher than c_2 do not participate.

Truth-telling

When is truth-telling incentive compatible? Firms that comply always tell the truth. However, firms that do not comply adopt the truth-telling strategy, S_{NT} , rather than the false-reporting strategy, S_{NF} , if and only if

$$V_{NT} > V_{NF}$$

which reduces to

$$F_1 + \delta k < \frac{\pi}{1 - \alpha}(F_2 + \delta k) - \frac{\alpha}{1 - \alpha}c \quad (6)$$

The truth-telling constraint in (6) is not satisfied for all firms. Even if F_1 is at its minimum level ($F_1 = 0$) and F_2 is at its maximum level ($F_2 = \bar{F}$), there may exist some $c \in [0, \bar{c}]$ which violates the constraint. To state this more formally, we first make the following assumptions:

A1: $0 \leq F_1 < F_2 \leq \bar{F}$, $i = 1, 2$ and, for any feasible enforcement policy $\{F_1, F_2, \pi\}$, $\max\{c_0, c_1\} < c_2 \leq \bar{c}$ (or, equivalently $\max\{c_0, c_1\} < \min\{c_2, \bar{c}\}$) where c_0 is defined by $V_{CT} = 0$, c_1 is defined by $V_{NT} = 0$ and c_2 is defined by $V_{NF} = 0$.¹²

¹²So

$$c_0 = y - \beta k$$

This leads to

Proposition 1: Given A1, truth-telling is not an incentive-compatible strategy for all firms.

Proof: For truth-telling to be incentive compatible for all firms, the V_{NF} strategy must be dominated by at least one of the truth-telling strategies for all $c \in [0, \bar{c}]$. Referring to Figure 1, and recalling that $|\partial V_{CT}/\partial c| > |\partial V_{NT}/\partial c| > |\partial V_{NF}/\partial c|$, this cannot occur if c_2 exceeds c_0 or c_1 , whichever turns out to be larger.

qed

How plausible are the restrictions in A1 that ensure that truth-telling is not incentive-compatible for all firms? The condition $c_2 > c_0$ implies

$$\pi(F_2 + \delta k) < y + k(1 - \beta)[1 - \delta(1 - \pi)]$$

The condition $c_2 > c_1$ implies

$$\pi(F_2 + \delta k) < F_1 + \delta k + \delta(1 - \pi)[y - (F_1 + \delta k)]$$

It is possible for these conditions to be violated by making the fines sufficiently high (which requires making \bar{F} sufficiently high). In that sense, truth-telling can always be made incentive compatible for all firms if the punishment for lying is sufficiently severe. However, making the fines high enough to ensure truth telling almost certainly guarantees that all firms also comply all of the time which is not only unrealistic, it means there is no enforcement problem. In this sense, the restrictions in A1 seem plausible.

Proposition 1 differs from the results of Kaplow and Shavell (1994) where truth-telling is an optimal strategy for all firms provided that $F_1 \leq \pi F_2$. The reason that our results differ is that we allow the regulator the power to

$$c_1 = \frac{y - \beta(F_1 + \delta k)}{1 - \beta}$$

and

$$c_2 = \frac{(1 - \alpha)y - \beta\pi(F_2 + \delta k)}{(1 - \beta)[1 - \delta(1 - \pi)]}$$

exploit the information revealed by a firm that tells the truth. As a result, truth-telling is not incentive compatible for some firms.¹³

It is helpful to see that if we set $\beta = 1$, our model reduces to the model of enforcement studied by Kaplow and Shavell (1994) and Malik (1993). Setting $\beta = 1$ reduces the truth-telling constraint in (6) reduces to

$$F_1 + \delta k < \pi(F_2 + \delta k)$$

Interpreting $F_1 + \delta k$ as the full penalty violators must pay makes this truth-telling constraint equivalent to that in Kaplow and Shavell (1994).

Why is the role of β so important? With $\beta = 1$, the firm begins each period with a broken PAD even following an order by the regulator to return to compliance. It is impossible, therefore, to force a firm to return to compliance and impossible, therefore, for information revealed in a confession of guilt to be used against the firm. As a result, truth-telling is incentive compatible for all firms. In contrast, when $0 < \beta < 1$, a guilty firm is forced back to compliance (with probability $1 - \beta$).

Assumptions A1 are consistent with four general configurations for the payoffs.

Case I:

When both types of noncompliance strategies exist (truth telling and lie telling), there exists a \bar{c} , shown in Figure 1, such that all firms with $c < \bar{c}$ will choose truth-telling, and those with $c > \bar{c}$ will falsely report. In other words \bar{c} is given by $V_{NT} = V_{NF}$, or

$$\bar{c} = \frac{\pi F_2 - (1 - \alpha)F_1 - \delta k(1 - \alpha - \pi)}{\alpha} \quad (7)$$

Such a \bar{c} exists as long as $V_{NT}|_{c=0} > V_{NF}|_{c=0}$ and $c_1 < c_2$.

Some simple comparative statics on \bar{c} , with respect to policy parameters,¹⁴ are

$$\frac{\partial \bar{c}}{\partial F_1} = -\frac{(1 - \alpha)}{\alpha} < 0$$

¹³An attractive feature of this result is that our model avoids the somewhat unsatisfactory implication of a truth-telling model that all firms tell the truth in the equilibrium and, yet, the regulator continues to inspect firms even though the outcome of the inspection is known in advance.

¹⁴It is easily shown, additionally, that \bar{c} falls with increases in k and β .

$$\begin{aligned} \frac{\partial \bar{c}}{\partial F_2} &= \frac{\pi}{\alpha} > 0 \\ \frac{\partial \bar{c}}{\partial \pi} &= \frac{\delta(1 - \beta)(F_2 - F_1)}{\alpha^2} > 0 \quad \text{since } F_2 > F_1 \end{aligned}$$

Note that the proportion of firms that truthfully reveal their compliance status is

$$T = \frac{G(\bar{c})}{G(c_2)}$$

so that a reduction in F_1 necessarily increases truth-telling.

Case II:

Assumptions A1 are also consistent with there being only one noncompliance strategy (lie-telling), in which case V_{NT} lies everywhere below $\max\{V_{CT}, V_{NF}\}$ as in Figure 2. Here, firms following strategy S_{CT} are distinguished from those firms following strategy S_{NF} by a c' satisfying

$$c' = k(1 - \alpha) + \pi(F_2 + \delta k)$$

with the properties:

$$\begin{aligned} \frac{\partial c'}{\partial F_1} &= 0 \\ \frac{\partial c'}{\partial F_2} &= \pi > 0 \\ \frac{\partial c'}{\partial \pi} &= k\delta(1 - \beta) + F_2 + \delta k \end{aligned}$$

[Figure 2 here]

The proportion of firms that truthfully report their compliance status in this case is

$$T = \frac{G(c')}{G(c_2)}$$

Case III:

In this case V_{CT} lies everywhere below $\max\{V_{NF}, V_{NT}\}$ and so once again \bar{c} distinguishes the truth-tellers from those reporting falsely, but there are no fully complying firms.

Case IV:

If $\max\{V_{NT}, V_{CT}\}$ is everywhere dominated by V_{NF} then there is no truth-telling.

Compliance

Differences in PAD operating costs also allow us to identify those firms that comply. Of those firms that choose truth-telling, some will comply with the standards and some will not. The condition for compliance among truth-telling firms is that $V_{CT} \geq V_{NT}$. The equality defines a critical cost, shown as \hat{c} in Figure 1, such that firms with $c < \hat{c}$ comply and those with $c > \hat{c}$ violate. Such a \hat{c} exists if $V_{CT}|_{c=0} > V_{NT}|_{c=0}$,¹⁵ and if c_1 is greater than c_0 .¹⁶ It is straightforward to see that

$$\hat{c} = F_1 - k(1 - \delta) \quad (8)$$

with the comparative-statics

$$\frac{\partial \hat{c}}{\partial F_1} = 1 > 0 \quad (9)$$

$$\frac{\partial \hat{c}}{\partial k} = -(1 - \delta) < 0 \quad (10)$$

$$\frac{\partial \hat{c}}{\partial \delta} = k > 0 \quad (11)$$

The overall industry compliance rate depends on how many firms choose each of the three strategies. To illustrate, continue to assume that all three strategies exist (Case I). Then, the proportion of firms choosing to always

¹⁵This amounts to

$$F_1 > k(1 - \delta)$$

¹⁶Since $c_0 = y - \beta k$, this amounts to

$$F_1 < y + (1 - \beta - \delta)k$$

or, since $F_1 > k(1 - \delta)$ from the previous footnote,

$$k(1 - \delta) < y + (1 - \delta)k - \beta k$$

or $0 < y - \beta k$.

comply is $G(\hat{c})$ - these firms have a 100% compliance rate. Next, the proportion of firms choosing to not comply but to report truthfully is $G(\bar{c}) - G(\hat{c})$ - these firms have a compliance rate of $1 - \beta$, the proportion of the time their PAD is operating. Finally, the proportion of firms choosing not to comply and to report falsely is $G(c_2) - G(\bar{c})$ - these firms comply only when their machines are working but do not report the truth when their machines are not working. As a result, their noncompliance status is discovered only by inspections with probability π each period, after which they return to compliance. The steady-state proportion of these firms that have working PAD machines, and therefore the compliance rate of these firms, can be shown to be $\pi(1 - \beta)/[\beta + \pi(1 - \beta)]$.¹⁷

The total compliance rate of participating firms (i.e., relative to c_2) is therefore

$$C = \beta \frac{G(\hat{c})}{G(c_2)} + (1 - \beta) \frac{G(\bar{c}) - G(\hat{c})}{G(c_2)} + \frac{\pi(1 - \beta)}{\beta + \pi(1 - \beta)} \frac{G(c_2) - G(\bar{c})}{G(c_2)}$$

Simplifying gives

$$C = \beta \frac{G(\hat{c})}{G(c_2)} + \frac{\beta(1 - \beta)(1 - \pi)}{\beta + \pi(1 - \beta)} \frac{G(\bar{c})}{G(c_2)} + \frac{\pi(1 - \beta)}{\beta + \pi(1 - \beta)} \quad (12)$$

It is easily shown that an increase in π and an increase in F_2 both increase the compliance rate. As usual, more frequent inspections and/or higher penalties

¹⁷To see this, denote by K_t the number of such firms that are in compliance at date t , and by N_t the number of firms out of compliance, and let $1 = K_t + N_t$. The evolution of K_t is described by

$$K_t = (1 - \beta)K_{t-1} + \pi(1 - \beta)N_{t-1}$$

Since these firms never report when they are out of compliance and do not voluntarily fix broken PADs, firms that were in compliance in $t - 1$ remain so only if the machine does not break down - with probability $1 - \beta$. Those firms that were not in compliance in $t - 1$ are inspected and forced into compliance with probability π and there is a probability $1 - \beta$ that the PAD does not break down again.

Using $N_{t-1} = 1 - K_{t-1}$ and setting $K_t = K_{t-1}$ for the steady state gives

$$K = \frac{\pi(1 - \beta)}{\beta + \pi(1 - \beta)}$$

for false compliance reports increases the compliance rate.¹⁸

However, the impact of F_1 on the compliance rate is unusual in this model and, indeed, stands as the contribution of this model towards a better understanding of the puzzling empirical phenomenon of high compliance rates and low expected fines. The role played by F_1 can be seen graphically by considering Figure 1. As F_1 increases, the V_{NT} curve shifts down, while the other curves remain unchanged. Thus, \hat{c} increases, increasing the number of firms that comply always, and \bar{c} falls, reducing truth-telling. So, while the number of firms that comply voluntarily increases as F_1 increases, the number of violating firms that can be detected and forced back into compliance decreases. The first effect tends to increase the overall compliance rate, while the second effect tends to reduce it. In addition to these two offsetting forces, the overall effect of a change in F_1 depends on the density of firms in the neighbourhoods of \hat{c} and \bar{c} . Before we consider this complication, we present our results initially using the assumption that the density of firms' costs is independent of the cost level. We relax this later.

A2: The cost structure of firms has a uniform density over $[0, \bar{c}]$. Denote this density simply by g , so that $G'(\cdot) = g > 0$ for all $c \in (0, \bar{c})$.

Proposition 2: Given assumptions A1 and A2, the compliance rate is a non-increasing function of the fine, F_1 and is a strictly decreasing function of the fine, F_1 , if also $\bar{c} > \hat{c}$.

Proof: The impact of F_1 on the compliance rate is found by differentiating equation (12). Given A1, the proportion of firms choosing the lying strategy

¹⁸By a similar logic, it follows that the compliance rate in Case II is

$$C = \beta \frac{G(c')}{G(c_2)} + \frac{\pi(1-\beta)}{\beta + \pi(1-\beta)}$$

which is increasing in F_2 and π . That in Case III is

$$C = \frac{\beta(1-\beta)(1-\pi)}{\beta + \pi(1-\beta)} \frac{G(\bar{c})}{G(c_2)} + \frac{\pi(1-\beta)}{\beta + \pi(1-\beta)}$$

which is decreasing in F_1 , and increasing in F_2 and π . Finally, in Case IV we have

$$C = \frac{\pi(1-\beta)}{\beta + \pi(1-\beta)}$$

which is independent of the fine structure, but increasing in π .

is greater than zero, and there are three cases to be considered.

Case I: When each of the strategies is optimal over some range of compliance costs, as shown in Figure 1, we get

$$\frac{\partial C}{\partial F_1} = \frac{\beta}{G(c_2)} \left(-\frac{g(1-\delta)}{\delta[\pi(1-\beta) + \beta]} \right) < 0 \quad (13)$$

Case II: If strategy S_{NT} (violate but report truthfully) is dominated by either or both of the other two strategies, so that, as in Figure 2, V_{NT} lies everywhere below the envelope $\max\{V_{CT}, V_{NF}\}$, then

$$\frac{\partial C}{\partial F_1} = 0$$

F_1 has no impact on the compliance rate because no firms choose the strategy which involves paying the fine.

Case III: If strategy S_{CT} (full compliance) is dominated everywhere but both S_{NT} (noncompliance with truthful reporting) and S_{NF} (noncompliance and false reporting) exist, (which occurs when $F_1 < k(1-\delta)$) then

$$\frac{\partial C}{\partial F_1} = -\frac{\beta[1-\delta(1-\beta)(1-\pi)]}{\delta[\pi(1-\beta) + \beta]} g < 0$$

In this case, a reduction in F_1 unambiguously raises the compliance rate.

Case IV: If V_{NF} everywhere exceeds $\max\{V_{CT}, V_{NT}\}$, then

$$\frac{\partial C}{\partial F_1} = 0$$

qed

Proposition 2 challenges the conventional result in the theory of enforcement that compliance can be increased by increasing the fine for non-compliance. Instead, we obtain the result that the compliance rate *may* be increased by decreasing the fine for non-compliance. Why is this so? In Case (I), in which all three strategies are present, lowering F_1 does lower the proportion of firms that choose to comply (\hat{c} in Figure 1 falls). However, at the same time, the proportion of truth-telling firms increases. As a result,

the proportion of firms that choose to violate but not report it decreases, (\bar{c} increases in Figure 1). Graphically, a fall in F_1 shifts V_{NT} out uniformly to the right, leaving V_{CT} and V_{NF} unaffected. Lowering F_1 converts some violating firms from liars to truth-tellers. This has a positive effect on the industry compliance rate because those firms that now report their violations instead of filing false compliance reports can be returned to compliance sooner, since they are identified immediately instead of with probability π each period. Because of the relative slopes of V_{CT} and V_{NF} and with a uniform density, more violating firms become truth-tellers than do complying firms become violators. For a given reduction in F_1 , \bar{c} is increased by more than \hat{c} is reduced.

In Case (III), in which the strategy of full compliance does not exist, lowering F_1 cannot reduce the proportion of firms that comply because it is already zero. As a result we only have the second effect in which untruthful firms switch to being truthful as \bar{c} increases.

4. Cost-Minimizing Enforcement

We suppose now that the agency's objective is to minimize its cost of enforcement subject to a constraint on industry pollution emissions.¹⁹ The agency achieves this by choosing an enforcement policy $\{F_1, F_2, \pi\}$, with $0 \leq F_1 < F_2 \leq \bar{F}$ and $\pi \in (0, 1)$.

To establish the relationship between compliance and emission levels, we assume that when in compliance, a firm's pollution emissions are exactly equal to its emissions standard, x ; when out of compliance, its emissions are $x_N > x$. The total industry emissions are then

$$X = G(c_2)[x_N(1 - C) + xC]$$

There are $G(c_2)$ firms participating: a proportion $1 - C$ are out of compliance and emit x_N ; a proportion C are in compliance and emit x . The exogenous industry emissions target is denoted \bar{X} and this is assumed to be feasible for at least some $\{F_1, F_2, \pi\}$.

Let N be the number of firms reporting compliance. In general, this is the number always choosing to comply plus the number choosing not to comply

¹⁹Alternatively, we could assume the agency has a given budget and chooses the parameters to minimize industry pollution emissions. Our results are the same in either case.

and to submit false reports. The number of firms that must be inspected each period is πN . Note that the exact equations for C and N depends on how many strategies are in effect.

If w is the cost per inspection, the enforcement agency's problem is

$$(P) \quad \min_{\{F_1, F_2, \pi\}} w\pi N(F_1, F_2, \pi)$$

subject to

$$\bar{X} \geq G(c_2(F_2, \pi))[x_N - (x_N - x)C(F_1, F_2, \pi)]$$

and $0 \leq F_1 < F_2 \leq \bar{F}$, $\pi \in (0, 1)$.

This cost-minimization leads to the following result:

Proposition 3: Given assumptions A1 and A2, the solution to the cost minimization problem (P) requires setting $F_1 = 0$ and $F_2 = \bar{F}$ for any $\pi \in (0, 1)$.

The formal proof is straightforward once we note that, under A1 and A2, both X and N are increasing functions of F_1 in Cases I and III and are independent of F_1 in Cases II and IV, and that X and N are decreasing functions of F_2 in all four cases. Thus, both cost and emissions can be reduced continuously by raising F_2 to its maximum. Further, both cost and emissions can be reduced continuously by lowering F_1 to its minimum in Cases I and III. In Cases II and IV, both cost and emissions are unaffected by the value of F_1 because no firms are ever fined for noncompliance in these cases. We therefore arbitrarily set $F_1 = 0$ in these cases.

For completeness, we are able to state the conditions for the optimal choice of π . In view of Proposition 3, the problem is:

$$\min_{\pi} w\pi N(0, \bar{F}, \pi)$$

subject to $\bar{X} \geq X(0, \bar{F}, \pi)$. First, we note that X is a decreasing function of π . Thus, define by $\bar{\pi}$, the smallest value of π which satisfies the constraint. This is defined implicitly by

$$\bar{X} = X(0, \bar{F}, \bar{\pi})$$

Also, let $\hat{\pi}$ be the solution to the unconstrained minimization problem

$$\hat{\pi} = \operatorname{argmin}_{\pi} w\pi N(0, \bar{F}, \pi)$$

then, the optimal choice of inspection level is

$$\pi^* = \begin{cases} \bar{\pi} & \text{if } \hat{\pi} \leq \bar{\pi} \\ \hat{\pi} & \text{if } \hat{\pi} > \bar{\pi} \end{cases}$$

5. Extensions

The main part of this paper has worked through a model of environmental regulation which has been restricted in two principal ways. First, we ruled out the possibility that firms might voluntarily disable the PAD so as to save on running costs. This is relaxed in the following subsection. Secondly, we assumed that running costs were uniformly distributed across firms. We re-examine this assumption and discuss alternative sufficient conditions for the main results of the paper to hold.

Initiating noncompliance

Our concern so far has been with the consequences of noncompliance being forced on firms through the (random) breakdown of the abatement technology. In this section we consider briefly an additional option for a firm – that of deliberately disconnecting the PAD. In this case the firm is voluntarily initiating the state of noncompliance and is not simply a victim of the exogenous breakdown of the equipment.

The possibility of deliberate noncompliance substantially weakens the enforcement power we have given to the regulator in our model. Although a firm that adopts this noncompliance strategy can be ordered to return to compliance, such an order is ineffective because the firm immediately returns to a state of noncompliance. The regulator therefore has no power to prevent a firm from always being out of compliance. This severely constrains the extent to which compliance gains can be achieved through lower fines for noncompliance as was the case in the previous section.²⁰

This extension introduces two new potential courses of action for the firm in addition to those discussed earlier. The firm may choose to disconnect the PAD and then to report that it has done so, or it may report falsely. Denote by S_{DT} the strategy of disconnecting the PAD and truthfully reporting it and V_{DT} the associated expected value of this strategy. Similarly, let S_{DF} denote

²⁰A more sophisticated enforcement power (such as an increasing fine structure for repeat offenders) is clearly required to deal with deliberate noncompliance. It is beyond the scope of this paper to consider different forms of enforcement power.

the strategy of disconnecting the PAD and filing a false report on compliance status, and let V_{DF} be the resulting expected value to the firm. We assume that technological failure does not befall a deliberately disconnected PAD and that any disconnection brought to the attention of the regulator, either by a truthful report or by random inspection, requires the firm to restart the device at a cost $s > 0$. The fine structure is the same as before. It is straightforward to see that V_{DT} is given recursively by

$$V_{DT} = y - F_1 - \delta s + \delta V_{DT}$$

where the discount term on s indicates that the firm is given one period to complete the start-up. Without loss of generality, we assume that the firm can immediately disconnect the device next period.

Similarly, a firm may choose to disconnect and file a false report. It is easy to see that V_{DF} in this case is given by

$$V_{DF} = \pi(y - F_2 - \delta s + \delta V_{DF}) + (1 - \pi)(y + \delta V_{DF})$$

If the firm is inspected, with probability π , it is fined and forced back into compliance, thus incurring the start-up cost. However, the firm immediately disables the PAD and returns to noncompliance.

Notice that the firm avoids the running cost under both strategies, so that only one can be optimal for all firms. We consider first the case in which $V_{DF} > V_{DT}$; that is, false-reporting dominates truthful reporting of the disconnection of the PAD. This case occurs if the expected penalty from false reporting, $\pi(F_2 + \delta s)$, is less than the certain penalty from truthful reporting, $F_1 + \delta s$. This condition is satisfied even with $F_1 = 0$ and $F_2 = \bar{F}$ as long as

$$\frac{\pi}{1 - \pi} \bar{F} < \delta s$$

which requires that the start-up cost, s , be sufficiently large. Intuitively, it is unprofitable to truthfully report disconnecting the PAD in this case because of the high cost of re-starting the PAD each period.

In this case, the results concerning the aggregate compliance rate and the cost-minimizing enforcement policy are qualitatively unchanged:

Proposition 4: If, in addition to the noncompliance strategies already examined, noncompliance can be initiated by deliberate disconnection of the PAD,

but false reporting dominates truthful reporting of this strategy then, (a) the aggregate compliance rate is a non-increasing function of F_1 and (b) the cost-minimization problem (P) is solved by setting $F_1 = 0$, $F_2 = \bar{F}$, and $\pi \in (0, 1)$.

Proof: To prove part (a), we show that the results in the proof of Proposition 2 are not changed by the addition of the new strategy. This, together with the demonstration that the number of firms to inspect, wN , is non-decreasing in F_1 proves part (b).

When the new strategy is present, the number of cases that can arise increases. However, many of these cases exclude the truth-telling strategy, S_{NT} . In these cases, the aggregate compliance rate and the number of firms to inspect are both independent of F_1 because no firms choose the strategy that results in this fine being imposed. As before, the value of F_1 is irrelevant in these cases so we arbitrarily set it equal to zero.

Four cases can arise that include the truth-telling strategy, S_{NT} , and therefore involve the fine F_1 being imposed. We consider each in turn.

First, all four strategies may co-exist: $(S_{CT}, S_{NT}, S_{VF}, S_{DF})$. The compliance rate is

$$C = G(\hat{c}) + (1 - \beta)[G(\bar{c}) - G(\hat{c})] + \gamma[G(c_3) - G(\bar{c})]$$

where $\gamma = \pi(1 - \beta)/(\beta + \pi(1 - \beta))$ and c_3 is the solution to $V_{DF} = V_{VF}$. In this case, $\partial c_3/\partial F_1 = 0$. Hence, $\partial C/\partial F_1 < 0$ as in (13) under A1 and A2. Next, the number of firms to be inspected is

$$\pi N = \pi[G(\hat{c}) + 1 - G(\bar{c})]$$

which is increasing in F_1 .

Second, the S_{NF} strategy is dominated everywhere but the other three remain: (S_{CT}, S_{NT}, S_{DF}) . The compliance rate is

$$C = G(\hat{c}) + (1 - \beta)[G(c_3) - G(\hat{c})]$$

where c_3 is the solution to $V_{NT} = V_{DF}$. In this case, $\partial c_3/\partial F_1 < 0$ but $\partial C/\partial F_1 = 0$ under A1 and A2. Next, the number of firms to inspect is

$$\pi N = \pi[G(\hat{c}) + 1 - G(c_3)]$$

which is increasing in F_1 .

Third, the S_{CT} strategy is dominated but the other three exist: (S_{NT}, S_{NF}, S_{DF}) . The compliance rate is

$$C = (1 - \beta)G(\bar{c}) + \gamma[G(c_3) - G(\bar{c})]$$

where c_3 is the solution to $V_{NF} = V_{DF}$. In this case, $\partial c_3/\partial F_1 = 0$ and $\partial C/\partial F_1 < 0$ under A1 and A2. In addition,

$$\pi N = \pi[1 - G(\bar{c})]$$

which is increasing in F_1 .

Fourth, only two strategies exist: (S_{NT}, S_{DF}) . The compliance rate is

$$C = (1 - \beta)G(c_3)$$

where c_3 is the solution to $V_{NT} = V_{DF}$. In this case, $\partial c_3/\partial F_1 < 0$ which makes $\partial C/\partial F_1 < 0$ under A1 and A2. In addition

$$\pi N = \pi[1 - G(c_3)]$$

which is increasing in F_1 .

Next, we consider the case in which $V_{DF} < V_{DT}$; that is, truthful reporting dominates false reporting of the disconnection of the PAD. This case is more likely to occur when start-up costs, s , are small and necessarily occurs if $s = 0$. A firm following this strategy deliberately and openly violates the pollution standard repeatedly, and willingly pays the fine F_1 and the discounted start-up costs, δs .

In this case, we get

Proposition 5: If, in addition to the noncompliance strategies already examined, noncompliance can be initiated by deliberate disconnection of the PAD, and truthful reporting dominates false reporting of this strategy then, (a) the aggregate compliance rate is an ambiguous function of F_1 and (b) the cost-minimization problem (P) is, in general, solved with $F_1 > 0$ and $F_2 = \bar{F}$, $\pi \in (0, 1)$.

Proof: The proof is straightforward when $s = 0$ for in this case, setting $F_1 = 0$ would induce all firms to adopt the strategy of disconnection combined with truthful reporting; in that case, the aggregate compliance rate would be zero.

For larger values of s , the proof follows the same steps as in Proposition 4 with four cases to examine. The expressions for C and πN are identical to those in the proof of Proposition 4. The difference is that c_3 is determined by the conditions $V_{NF} = V_{DT}$, $V_{NT} = V_{DT}$, $V_{NF} = V_{DT}$, and $V_{NT} = V_{DT}$ respectively. In each case, $\partial c_3 / \partial F_1 > 0$ which is enough to make the aggregate compliance rate sometimes increasing and sometimes decreasing in F_1 under A1 and A2, depending on parameter values. In the other cases, C is independent of F_1 . This proves part (a) of the proposition. Part (b) follows directly.

Propositions 4 and 5 show that when enforcement power is weakened by the ability of polluters to openly defy enforcement orders, the ability of the regulator to obtain high compliance rates with low fines hinges on the technical ability of firms to switch back and forth between states of compliance and noncompliance. If it is sufficiently costly to move between these states, firms that choose to deliberately disconnect the PAD will continue to (falsely) report compliance to the agency. In this case, Proposition 4 shows that the cost-minimizing enforcement policy involves setting the noncompliance fine equal to zero under assumptions A1 and A2. On the other hand, if the cost of moving between the states of compliance and noncompliance is sufficiently low that some firms choose to deliberately disconnect the PAD and truthfully report that they have done so, it is impossible to obtain higher compliance rates by lowering the noncompliance fine.

Sufficient conditions

The focus of the paper has been on a leading special case in which the distribution of costs is assumed to be uniform. This has permitted us to ignore the influence of the cost structure on firm behaviour in response to changes in the fine structure. To consider the general case, we can look at the derivative of (12) with respect to F_1 for an arbitrary, but differentiable distribution function. A simple calculation shows this to be

$$\frac{\partial C}{\partial F_1} = \frac{\beta}{G(c_2)} \left([g(\hat{c}) - g(\bar{c})] - \frac{(1-\beta)(1-\pi)(1-\delta)}{\alpha[\beta + \pi(1-\beta)]} g(\bar{c}) \right)$$

A large number of alternative sufficient conditions for C to be decreasing in F_1 are now apparent; for example, that g always has more mass around \bar{c} than around \hat{c} . In general, the intuitive interpretation of any alternative to the uniform density as a sufficient condition, is that C will fall with F_1

as long as not "too many" additional firms switch from being compliers to being noncompliers relative to the number switching from being truth-tellers to being false-reporters for each dollar reduction in F_1 .

6. Conclusion

The point of departure for this paper is the observation that the predictions of the standard theory of enforcement are at odds with a stylized fact of pollution-standards enforcement: compliance rates are high even though penalties for violations are low. The purpose of this paper is to argue that this observation is in fact consistent with theoretical predictions when the theory is extended to include a self-reporting requirement and enforcement. Both of these elements are present in practice. Our main findings are that in this extended enforcement model it is possible, under some conditions, to achieve higher compliance rates with lower fines (the reverse of the conventional prediction) and that, when this is true, the cost of enforcing a given level of aggregate pollution is minimized by setting the fine for noncompliance equal to zero.

Lowering the fine for noncompliance has two effects in our model. First is the conventional effect that lowering the fine reduces the proportion of firms that choose to comply always. This reduces the compliance rate. Second is the new effect that lowering the fine raises the proportion of noncomplying firms that file truthful reports about their compliance status. This increases the overall compliance rate because it leads to earlier detection of noncompliers. That is, rather than having to rely on identification through random inspections, the regulator, by lowering the fine for noncompliance, can rely on noncompliers to identify themselves. This permits the regulator to take actions to order these firms to return to compliance sooner than would otherwise be the case.

We found the conditions under which the second effect dominates the first to be plausible. A necessary condition is that it not be too easy for to alternate between states of compliance and noncompliance. If the cost of moving between states is sufficiently low and the fine is also low, the optimal strategy for most firms is to never comply but to report truthfully. The only way to prevent this in our model is to raise the fine for noncompliance. The model predicts then, that in situations where the cost of alternating between compliance and noncompliance is low (as may be the case for illegal waste disposal and, to suggest a non-pollution example, speeding infractions),

enforcement policies would include substantial fines for noncompliance.

If the cost of alternating between states of compliance and noncompliance is sufficiently high, as it would be if the control method is an integral part of the production technology or the process of disabling and re-enabling the pollution control equipment is costly (as it might be for catalytic converters and flue gas scrubbers, for example), our results depend on the density of firms at low versus high cost of abatement. In the case of the uniform density, we find that the aggregate compliance rate is non-increasing in the fine for noncompliance and that setting the fine equal to zero minimizes the cost of enforcing a given level of aggregate pollution emissions. These results hold for other distributions as long as not too many firms adopt noncompliance strategies and a sufficiently large number adopt truth-telling behaviour.

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References

- Becker, G.S. (1968) "Crime and Punishment: An Economic Approach", *Journal of Political Economy* 76, 169-217.
- Cropper, Maureen L. and Wallace Oates (1992) "Environmental Economics: A Survey", *Journal of Economic Literature* 30 (2), 675-740.
- Harford, Jon D. (1978) "Firm behavior under imperfectly enforceable pollution standards and taxes", *Journal of Environmental Economics and Management* 5, 26-43.
- Harford, Jon D. (1987) "Self-reporting of pollution and the firm's behavior under imperfectly enforceable regulations", *Journal of Environmental Economics and Management* 14, 293 - 303.
- Harrington, Winston (1988) "Enforcement leverage when penalties are restricted", *Journal of Public Economics* 37, 29-53.
- Kaplow, Louis and Steven Shavell (1994) "Optimal law enforcement with self-reporting of behavior", *Journal of Political Economy* 102, 583-606.
- Malik, Arun S. (1993) "Self-reporting and the design of policies for regulating stochastic pollution", *Journal of Environmental Economics and Management* 24, 241-257.
- Ontario Ministry of the Environment, 1986-89, Annual direct discharge reports.

Russell, Clifford S., W. Harrington, and W.J. Vaughan, 1986, *Enforcing pollution control laws* (Resources for the Future, Washington, DC.)

Storey, D.J. and P.J. McCabe (1980) "The criminal waste disaster", *The Scottish Journal of Political Economy* 27, 30 - 40.

Swierzbinski, Joseph E. (1994), "Guilty until proven innocent - regulation with costly and limited enforcement", *Journal of Environmental Economics and Management* 27, 163-184.

FIGURE 1

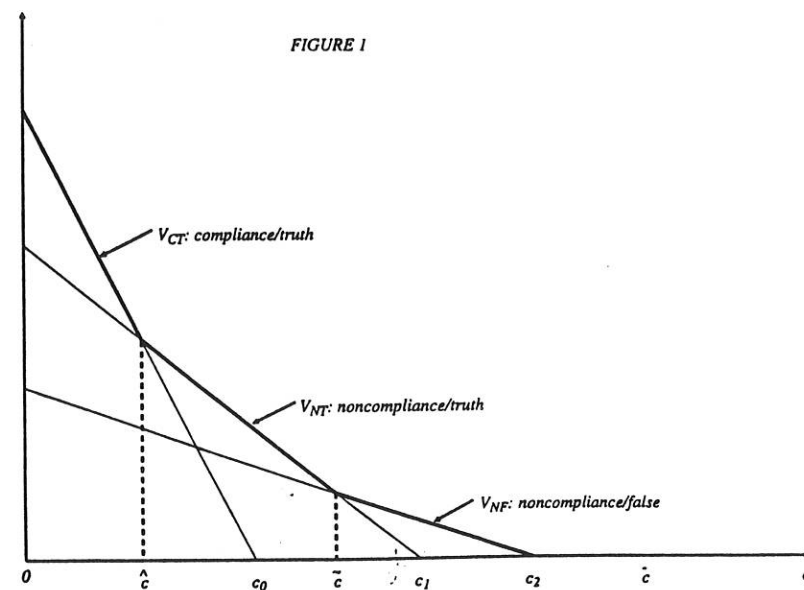
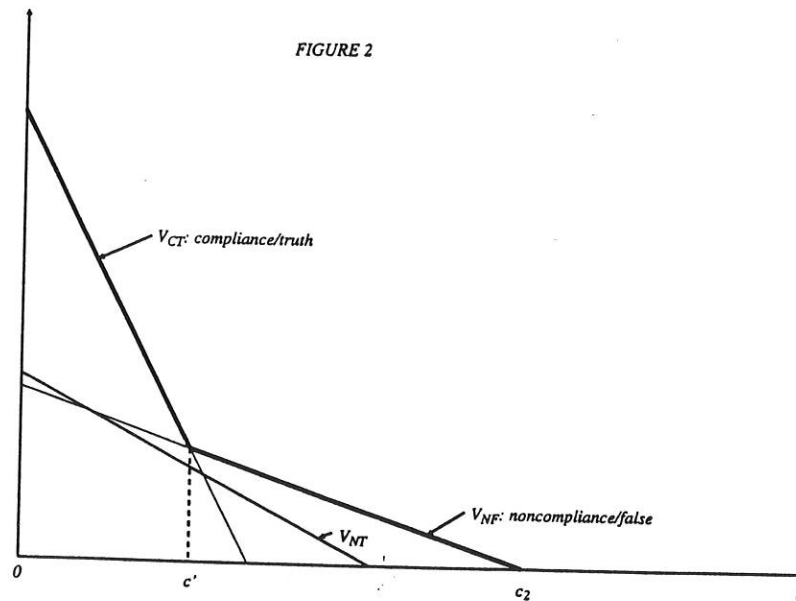


FIGURE 2



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