Tenure and Experience Effects on Wages: A Theory

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Abstract

This paper investigates equilibria in a labor market where firms post wage/tenure contracts and risk-averse workers, both employed and unemployed, search for better paid job opportunities. Different firms typically offer different contracts. Workers accumulate general human capital through learning-by-doing. With on-the-job search, a worker's wage evolves endogenously over time through experience effects, tenure effects and quits to better paid employment. This equilibrium approach suggests how to identify econometrically between experience and tenure effects on worker wages.

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1 Introduction

Here we investigate individual wage dynamics in the context of an equilibrium labour market framework where workers accumulate human capital while working, firms post contracts, and workers search while employed. The analysis leads to new insights into two important areas in labour economics - the nature of equilibrium in search markets, and the empirical decomposition of wages into experience and tenure effects.

There is a significant empirical literature which has attempted to decompose wages into experience and tenure effects (see, for example, Altonji and Shakotko (1987), Topel (1991), Altonji and Williams (2005), and Dustmann and Meghir (2005)). The results obtained are still hotly debated. There are two major difficulties faced by researchers in this area. First, tenure and experience are perfectly correlated within any employment spell. Second, it is unreasonable to assume a quit (which resets tenure to zero) is an exogenous outcome which is orthogonal to the wages paid by the previous employer and the new one. Without an equilibrium framework it seems an heroic task identifying between tenure and experience wage effects. A major objective of this study is to provide a coherent framework which identifies between these two factors.

The typical theoretical justification presented to explain why wages change both with experience and with tenure is based on two big ideas associated with Rosen (1972) and Mincer (1974). First, although there is no free lunch, it is accepted by many that individuals accumulate human capital by working. Typists become better typists while working as typists, economists become more productive by doing economics, etc. This seems both an important and intuitive idea. A related idea now common among labour economists, is that human capital can be dichotomized into general human capital and firm specific human capital. A worker who enjoys an increase in general human capital becomes more productive at all jobs, whereas accumulating firm specific human capital implies a worker is only more productive at that firm. Workers who change job, or those who are laid off, lose their firm specific human capital but keep their general human capital. Putting these two ideas together, plus assuming a worker's wage is an increasing function of both his/her general and

specific human capital, leads to at least the rudiments of a theory of how a worker's wage can depend on both experience and tenure.

The central difficulty with using this simple theory in applied work is that when the market is competitive, firm specific capital has no impact on wages and so, in the absence of any frictions, there should be no tenure effect on wages. Conversely when markets are frictional, job search yields non-trivial wage dynamics. Indeed even when there is no human capital accumulation, Burdett (1978) demonstrated some time ago that through on-the-job search, quit turnover alone could explain why the average wage of workers is a concave, increasing function of worker experience.

In the present study we describe a labour market with frictions where workers accumulate general human capital through learning-by-doing and there are also (endogenous) tenure effects. It yields a description of cross section wage dispersion which is consistent with the distribution of wage/age profiles across individual workers. The framework is particularly rich as:

- (i) workers are ex-ante heterogeneous - workers have different productivities when first entering the labour market;
- (ii) randomness in the job search process implies even workers of the same age may have very different work experience and thus have accumulated different levels of human capital;
- (iii) there is dispersion in wage contracts offered by firms so that starting wages and tenure effects vary systematically across firms;
- (iv) there is sorting with age, where on-the-job search implies older workers have, on average, better paid employment.

Even allowing for such richness, the model yields a relatively straightforward econometric structure. We discuss this structure in detail in Section 6 below. An important observation, however, is that the wage tenure effect at any given firm depends on its starting wage offer: the greater a firm's initial wage offer, the smaller the wage-tenure effect. Indeed a firm whose payrates are close to the highest in the market will have very small tenure effects. This structure also predicts that younger workers (who on average tend to be less well paid) enjoy greater wage increases with

tenure than do older workers.

The paper builds on the seminal work of Burdett (1978) and Burdett and Mortensen (1998) which show how equilibrium search can generate wage dispersion and individual wage profiles that are (on average) increasing and concave in experience. Stevens (2004) subsequently demonstrated why, in that framework, firms increase profit by offering contracts which increase the wage paid with tenure (or seniority). Essentially paying higher wages at longer tenures rewards worker loyalty. This is profitable to the firm as rewarding loyalty reduces a worker's quit incentive and the firm can then pay lower wages at short tenures to better extract the search rents of new hires. With risk neutral workers, Stevens (2004) showed the optimal tenure contract is a step contract, say the firm pays some base wage until the worker reaches some promotion tenure T , after which the worker is paid marginal product. Burdett and Coles (2003) showed with strictly risk averse workers, the optimal contract smooths wage payments by tenure. It then described a search equilibrium where different firms post different optimal contracts and workers used optimal search strategies.¹

Several papers have considered general human capital accumulation within the Burdett/Mortensen framework (see for example Bunzel et. al. (2000), Barlevy (2005), Burdett et al (2010)). The addition of learning-by-doing generates interesting sorting effects: higher wage firms not only attract and retain more workers, but also, in steady state, enjoy a more experienced and thus more productive workforce. The introduction of learning-by-doing also significantly increases equilibrium wage inequality: young workers not only have little work experience, the reservation wage (or piece rate) of the unemployed is low as experience is valuable and an employee will accept a low paid job as an investment in increased (future) productivity.

A complementary approach to the one taken here assumes instead firms compete on wages when an employee receives an outside offer (see for example Postel Vinay and Robin (2002a,b)). This approach yields an important econometric structure for applied work on wages and turnover. With competitive bidding by firms, turnover becomes very simple: a worker quits whenever he/she contacts a higher productivity

¹More recently Shi (2009) has applied this contracting approach to the directed search framework.

firm. Observed wages are then a convolution of each firm's bid function and the distribution of firm productivities: the wage paid to any given employee simply matches the value of that employee's best previous offer. Yamaguchi (2006), and Bagger et al. (2010) also extend that framework to human capital accumulation while employed.

Of course it is an empirical question whether firms match offers or not (though see Postel-Vinay and Robin (2004) and Holzner (2010) who ask when this policy may, or may not be, privately optimal for firms). Clearly, in some labor markets firms do respond to outside offers (as in the academic labor market), whereas in others (as in the labor market for bricklayers) firms do not respond. The empirical implications of these two approaches are different. For example Burdett and Coles (2010) show that turnover is not efficient when firms post tenure contracts: well paid senior workers may reject job offers at more productive firms whose starting salaries are too low. Also the quit behaviour of workers is different. Here within any employment spell, a worker's quit rate decreases with tenure; i.e. at any given firm, there is negative duration dependence in its employees' job-to-job hazard rate. Conversely in a matching offers framework, a worker quits as soon as he/she contacts a higher productivity firm. In that case at any given firm, there is no duration dependence in its employees' job-to-job hazard rate. Finally the matching offers framework implies income is subject to large shocks within an employment spell: a worker may enjoy a substantial payrise by generating an outside offer. Conversely the framework here implies wages within an employment spell increase incrementally (through an internal promotion scheme).

The next Section specifies the basic framework. Section 3 characterises the set of optimal contracts offered by firms and section 4 defines a market equilibrium and describes its steady state properties. Section 5 proves the existence of a Market Equilibrium. Section 6 describes the empirical implications of this framework and concludes.

2 THE BASIC FRAMEWORK

The object is to construct an equilibrium framework where the income received by an employed worker may vary with total work experience as well as with tenure. A worker's wage changes with experience as the worker becomes more productive through learning-by-doing. Further a worker's wage can vary with tenure as a result of the wage contract offered by a firm.

Time is continuous with an infinite horizon and only steady-states are considered. There is a continuum of both firms and workers, each of measure one. All firms are equally productive and have a constant returns to scale technology. A worker's life in this market is described by an exponential distribution with parameter $\phi > 0$. Hence over any small time period $dt > 0$, any worker leaves the market for good with probability ϕdt . The parameter ϕ also describes the inflow of new labour market entrants. Each new entrant is initially unemployed and, for the moment, we assume each has the same initial productivity y_0 . Later we show that the results generalize straightforwardly to the case that workers are ex-ante heterogeneous.

Learning-by-doing implies a worker's productivity increases while employed. Let $\rho > 0$ denote this learning rate. Thus after x years of work experience, a worker's productivity is $y = y_0 e^{\rho x}$. We restrict our attention to $\rho < \phi$ so that lifetime payoffs are bounded. While unemployed there is no learning-by-doing but nor is there human capital decay - an unemployed worker's productivity y simply remains constant. A worker with productivity y generates revenue flow y while employed and income by while unemployed, where $0 < b < 1$.

Following Stevens (2004), firms offer optimal wage contracts where, inter alia, the wage paid depends on the employee's tenure (or seniority) τ .² In general firm j 's employment contract is a function which pays each employee a wage $w = w_j(y, x, \tau)$. Clearly there is no loss in generality by focussing on piece-rate contracts $\theta = \theta_j(y, x, \tau)$ with wage paid $w = y\theta_j(y, x, \tau)$. Further as $y = y_0 e^{\rho x}$, and experience $x = x_0 +$

²See Stevens (2004) for a complete discussion on the structure of optimal contracts when workers are risk neutral. Note that such a contract rules out matching-offer behaviour as considered in Postel-Vinay and Robin (2002a,b).

τ where x_0 is the employee's prior work experience, there is no loss in generality by further restricting attention to piece-rate tenure contracts of the form $\theta_j(\tau, x_0)$. In the absence of tenure effects and learning-by-doing, Carillo (2008) explores how conditioning wages on prior experience x_0 affects market outcomes in a frictional labour market. Here we rule out such discrimination by supposing each firm must offer the same contract to potential hires with the same productivity. Specifically firm j offers the same piece rate tenure contract $\theta = \theta_j(\tau)$ to each new hire. Thus more experienced workers are hired at a higher starting wage $w = y\theta_j(0)$ but the contract is not otherwise allowed to discriminate by experience. We discuss further the role of this assumption in the conclusion.

Workers are either unemployed or employed and all obtain new job offers at Poisson rate λ , independent of their employment status. Given an employee receives an outside contract offer, say $\tilde{\theta}(\cdot)$, the worker compares the value of remaining at his/her current firm with contract $\theta(\cdot)$ with current tenure τ , or switching to the new firm offering contract $\tilde{\theta}(\cdot)$ with zero tenure. Any job offer received is assumed to be the realization of a random draw from the distribution of all offers made by firms. We describe this in more detail below. There are job destruction shocks in that each employed worker is displaced into unemployment according to a exponential random variable with parameter $\delta > 0$. As is standard, there is no recall of previously rejected employment offers.

In the absence of job destruction shocks, workers would find their earnings always increase over time. An optimal consumption strategy with liquidity constraints would then imply workers consume current earnings $\theta(\tau)y$. Job destruction shocks, however, generate a precautionary savings motive. For tractability, however, we simplify by assuming workers can neither borrow nor save; i.e. consumption equals earnings at all points in time. We further assume a flow utility function with constant relative risk aversion; i.e. $u(w) = w^{1-\sigma}/(1-\sigma)$ with $\sigma \geq 0$.³

Firms and workers have a zero rate of time preference. Firms are also risk neutral

³as typically done, we assume the worker's continuation payoff is zero in the event of death. But note that $\sigma > 1$ implies flow utility is negative and in that case we must also rule out suicide.

and so the objective of each is to maximize steady state flow profit. Each worker chooses a search and quit strategy to maximize expected total lifetime utility where the exit process implies each discounts the future at rate ϕ . Unless otherwise stated, proofs of all claims made below are presented in the technical Appendix.

Workers

Let $V = V(y, \tau|\theta)$ denote the maximum expected lifetime utility of an employed worker with current productivity y , tenure τ with piece rate contract $\theta(\cdot)$. As a contract which induces an employee to quit into unemployment is never optimal,⁴ an optimal contract and standard arguments imply $V(\cdot)$ satisfies:

$$\begin{aligned} \phi V(y, \tau|\theta) = & \frac{\theta(\tau)^{1-\sigma} y^{1-\sigma}}{1-\sigma} + \rho y \frac{\partial V}{\partial y} + \frac{\partial V}{\partial \tau} + \delta[V^U(y) - V(y, \tau|\theta)] \\ & + \lambda[E \max\{V(y, \tau|\theta), V(y, 0|\tilde{\theta})\} - V(y, \tau|\theta)], \end{aligned}$$

where $V^U(y)$ denotes the maximum expected lifetime utility to an unemployed worker with productivity y . Note, the employee's payoff varies through time as the worker's productivity increases through learning-by-doing (picked up by the $\partial V/\partial y$ term) and as the piece rate earned varies with tenure (picked up by the $\partial V/\partial \tau$ term). Also at rate λ the worker receives a (random) outside contract offer $\tilde{\theta}$ and quits if $V(y, 0|\tilde{\theta}) > V(y, \tau|\theta)$. The value of being unemployed $V^U(y)$ satisfies

$$\phi V^U(y) = \frac{(by)^{1-\sigma}}{1-\sigma} + \lambda[E \max\{V^U(y), V(y, 0|\tilde{\theta})\} - V^U(y)].$$

As firms pay piece rates then wages earned are always proportional to productivity y . Further a CRRA utility function and the assumption that productivity grows at a constant rate now imply these value functions are separable in productivity y ; i.e. V

⁴Suppose an optimal contract implies the worker quits into unemployment at tenure $T \geq 0$. Thus at tenure T , the firm's continuation profit is zero and the worker obtains V^U . The same contract but which instead offers piece rate $\theta(t) = b$ for all tenures $t \geq T$ is strictly profit increasing - on-the-job learning implies the worker obtains an improved payoff no lower than V^U at T and, by not quitting, the firm's continuation payoff is strictly positive (as $b < 1$). This latter contract then makes greater expected profit which contradicts optimality of the original contract.

and V^U take the form

$$\begin{aligned} V(y, \tau|\theta) &= y^{1-\sigma} U(\tau|\theta) \\ V^U(y) &= y^{1-\sigma} U^U, \end{aligned}$$

where $U(\tau|\theta)$ is termed the piece rate value of contract θ (at tenure τ) and U^U is called the piece rate value of unemployment.⁵

Let $U_0 = U(0|\tilde{\theta})$ denote the starting piece rate value of a representative contract offer $\tilde{\theta}$. As search is random, let $F(\tilde{U}_0)$ denote the fraction of firms making a contract offer whose starting piece rate value is no greater than $\tilde{U}_0$. Substituting out $V(y, \tau|\theta) = y^{1-\sigma} U(\tau|\theta)$ and $V^U(y) = y^{1-\sigma} U^U$ in the Bellman equations above now yields the following equations for $U(\cdot|\theta)$ and U^U :

$$[\delta + \phi - \rho(1 - \sigma)]U - \frac{dU}{d\tau} = \frac{[\theta(\tau)]^{1-\sigma}}{1 - \sigma} + \delta U^U + \lambda \int_U^{\bar{U}} [1 - F(U_0)] dU_0. \quad (1)$$

$$\phi U^U = \frac{b^{1-\sigma}}{1 - \sigma} + \lambda \int_U^{\bar{U}} [U_0 - U^U] dF(U_0) \quad (2)$$

This has an obvious but important implication. Independent of the worker's current productivity y , an unemployed worker will accept offer U_0 if and only if $U_0 \geq U^U$. This implies the expected duration of unemployment is the same for all workers. Further a worker's quit rate is also independent of productivity y : an employed worker with current piece rate value $U(\tau|\theta)$ will accept a job offer $\tilde{\theta}$ if and only if the latter's starting piece rate value $U(0|\tilde{\theta}) > U(\tau|\theta)$.

The above yields a complete description of optimal quit behaviour by workers: any employee with tenure τ at a firm offering contract $\theta(\cdot)$ leaves at rate $\phi + \delta + \lambda[1 - F(U(\tau|\theta))]$. Thus at the time of hiring, the probability the new hire will still be employed at the firm after any given tenure τ is

$$\psi(\tau|\theta) = e^{-\int_0^\tau \{\phi + \delta + \lambda[1 - F(U(s|\theta))]\} ds}. \quad (3)$$

⁵Note, equilibrium will find $U(\tau|\theta) > 0 (< 0)$ when $\sigma < 1 (> 1)$ so that payoffs are always increasing in productivity y .

Firms

Let $\bar{u}\bar{e}$ denote the steady state unemployment rate and let $N(x)$ denote the fraction of unemployed workers who have experience no greater than x . Measure $1 - \bar{u}\bar{e}$ of workers are thus employed. Let $H(x, U)$ denote the proportion of employed workers who have experience no greater than x and piece rate value no greater than U . Below we determine each of these objects (in a steady state equilibrium) but for now take them as given.

Consider a firm which posts contract $\theta(\cdot)$ with starting piece rate value $U_0 = U(0|\theta)$. If $U_0 < U^U$ all potential employees prefer unemployment to accepting this job offer and so such an offer yields zero profit. Suppose instead $U_0 \geq U^U$ - such offers are accepted at least by unemployed workers. As there is no discounting, the firm's steady state flow profit can be written as

$$\begin{aligned}\Omega(\theta) = & \lambda\bar{u}\bar{e} \int_{x=0}^{\infty} \left[\int_0^{\infty} \psi(\tau|\theta)[1 - \theta(\tau)]e^{\rho\tau}[y_0 e^{\rho x}]d\tau \right] dN(x) \\ & + \lambda(1 - \bar{u}\bar{e}) \int_{U'=\underline{U}}^{U_0} \int_{x=0}^{\infty} \left[\int_0^{\infty} \psi(\tau|\theta)[1 - \theta(\tau)]e^{\rho\tau}[y_0 e^{\rho x}]d\tau \right] dH(x, U').\end{aligned}$$

The firm's steady state flow profit is composed of two terms. The first term describes the hiring inflow of unemployed workers by experience x (with corresponding initial productivity $y = y_0 \exp(\rho x)$) times the expected profit obtained by employing such a worker. The second term describes the hiring inflow of currently employed workers by experience x and (outside) value U' (where a worker on piece rate value U' will only accept the job offer if $U' < U_0$) times the expected profit per each type of hire. Simple manipulation establishes

$$\Omega(\theta) = \lambda[\bar{u}\bar{e} \int_{x=0}^{\infty} y_0 e^{\rho x} dN(x) + (1 - \bar{u}\bar{e}) \int_{U'=\underline{U}}^{U_0} \int_{x=0}^{\infty} y_0 e^{\rho x} dH(x, U')] \left[\int_0^{\infty} \psi(t|\theta)[1 - \theta(t)]e^{\rho t} dt \right].$$

Note the first bracketed term depends only on U_0 (given $\bar{u}\bar{e}$, N , H).

To determine the contract that maximizes Ω we use the following two step procedure. First we identify a firm's piece rate contract which maximizes

$$\int_0^{\infty} \psi(t|\theta(\cdot))[1 - \theta(t)]e^{\rho t} dt$$

conditional on the contract yielding piece rate value U_0 . Such a contract is termed an optimal contract and is denoted $\theta^*(\cdot|U_0)$. We can then define maximized profit per hire

$$\Pi^*(0|U_0) = \int_0^\infty \psi(t|\theta^*)[1 - \theta^*(t|U_0)]e^{\rho t} dt.$$

An optimal contract thus yields steady-state flow profits

$$\Omega^*(U_0) = \lambda y_0 \left[\bar{ue} \int_{x=0}^\infty e^{\rho x} dN(x) + (1 - \bar{ue}) \int_{U'=\underline{U}}^{U_0} \int_{x=0}^\infty e^{\rho x} dH(x, U') \right] \Pi^*(0|U_0).$$

The firm's optimization problem then reduces to choosing a starting payoff U_0 to maximize $\Omega^*(U_0)$. Before formally defining an equilibrium, it is convenient first to characterise the set of optimal contracts θ^* for any given distribution functions F , N and H .

3 Optimal Piece Rate Tenure Contracts.

In this Section we extend the arguments used in Burdett and Coles (2003) to a more general setting. A useful preliminary insight is that as the arrival rate of offers is independent of a worker's employment status, an unemployed worker will always accept a contract which offers $\theta(\tau) = b$ for all t . Further, as $b < 1$ by assumption, a firm can always obtain strictly positive profit by offering this contract. Thus, without loss of generality, we make the following restrictions: all firms make strictly positive profit; i.e., $\Omega^* > 0$, and $\underline{U} \geq U^U$, i.e., all firms make acceptable offers. To simplify the exposition further, however, we also assume F has a connected support.

For any starting value $U_0 \geq U^U$, an optimal contract $\theta^*(\cdot|U_0)$ solves the program

$$\max_{\theta(\cdot)} \int_0^\infty \psi(t|\theta(\cdot))e^{\rho t}[1 - \theta(t)]dt \quad (4)$$

subject to (a) $\theta(\cdot) \geq 0$, (b) $U(0|\theta(\cdot)) = U_0$ and (c) the optimal quit strategies of workers which determine the survival probability $\psi(\cdot|\theta)$. As $\sigma > 0$ implies the marginal utility of consumption is infinite at $\theta = 0$, we will show an optimal contract always implies $\theta > 0$ for all $t > 0$.

Given an optimal contract θ^* which yields starting value U_0 , let $U^* \equiv U(\tau|\theta^*)$ denote the worker's piece rate value of employment at tenure τ and note we can describe U^* as $U^*(\tau|U_0)$. Similarly given an optimal contract θ^* which yields starting value U_0 , let $\Pi^*(\tau|U_0)$ denote the firm's continuation value at tenure τ ; i.e.

$$\Pi^*(\tau|U_0) = \int_{\tau}^{\infty} e^{-\int_{\tau}^t [\delta + \phi - \rho + \lambda(1 - F(U^*(s|U_0)))] ds} [1 - \theta^*(t|U_0)] dt.$$

Theorem 1. For any $U_0 \geq \underline{U}$, an optimal contract $\theta^*(\cdot|U_0)$ and corresponding worker and firm payoffs U^* and Π^* are solutions to the dynamical system $\{\theta, U, \Pi\}$ where

(a) θ is determined by

$$\begin{aligned} & \frac{\theta^{1-\sigma}}{1-\sigma} + \theta^{-\sigma} [1 - \theta + [\rho - \phi - \delta - \lambda(1 - F(U))]\Pi] \\ &= [\delta + \phi - \rho(1 - \sigma)]U - \delta U^U - \lambda \int_U^{\bar{U}} [1 - F(U_0)] dU_0. \end{aligned} \quad (5)$$

(b) Π is given by

$$\Pi(t) = \int_t^{\infty} e^{-\int_t^s [\delta + \phi - \rho + \lambda(1 - F(U(\tau)))] d\tau} (1 - \theta(s)) ds, \text{ and} \quad (6)$$

(c) U evolves according to the differential equation

$$\frac{dU}{dt} = -\theta^{-\sigma} \frac{d\Pi}{dt} \quad (7)$$

with initial value $U(0) = U_0$.

The above characterization of an optimal contract is very general - it allows for mass points in F and the density of F need not exist. In the equilibrium described in Theorem 3 below, however, the density of offers F' exists. In that case, a more intuitive structure arises if we totally differentiate (5) and (6) with respect to t and so obtain the following differential equation system for (θ, Π, U) :

$$\dot{\theta} = \frac{\lambda [\theta^{1-\sigma}]}{\sigma} F'(U) \Pi - \rho \theta \quad (8)$$

$$\dot{\Pi} = [\delta + \phi - \rho + \lambda(1 - F(U))]\Pi - (1 - \theta) \quad (9)$$

$$\dot{U} = -\theta^{-\sigma} \dot{\Pi} \quad (10)$$

(8) describes how piece rates change along the optimal piece rate contract. If workers are risk neutral ($\sigma = 0$), as in Stevens (2004), the optimal contract is to pay $\theta = 0$ for a finite spell $\tau < T$, after which the worker is paid marginal product, $\theta = 1$. The reason is that an employee who is paid less than marginal product is likely to be poached by a better paying competitor. When the worker is risk neutral, the firm extracts the search rents of new hires as quickly as possible by paying the floor wage $w = 0$. When instead workers are strictly risk averse ($\sigma > 0$), workers prefer a smoother consumption profile. The optimal contract then involves a trade-off between lower wage variation (smoother consumption) and reducing worker quit incentives.

The wage received within the employment spell is $\theta(\tau)e^{\rho\tau} [y_0 e^{\rho x_0}]$, where x_0 describes the worker's prior experience when hired by the firm. Thus (8) implies the wage received evolves according to

$$\frac{\frac{d}{dt}[y_0 e^{\rho x_0} e^{\rho t} \theta(t)]}{y_0 e^{\rho x_0} e^{\rho t} \theta(t)} = \frac{\lambda F'(U) \Pi}{\sigma \theta^\sigma}. \quad (11)$$

Wages are thus always increasing within an employment spell, and strictly increasing when the density of competing outside offers is positive (i.e., $F'(U) > 0$). The optimal contract reveals the underlying trade-off between lower wage variation (smoother consumption) and reducing the marginal quit incentives of employees: $F'(U)$ describes the marginal number of competing firms who might attract employee on value U , and Π describes the firm's corresponding loss in profit should this employee quit. Note further that a constant wage (perfect consumption smoothing) requires a piece rate $\theta(\tau)$ which declines at rate ρ . Thus even though an optimal contract implies wages must always increase within an employment spell, tenure effects may now be negative (but not so large that wages paid decline).

Assuming F' exists, the optimal piece rate contract is the saddle path solution to the differential equation system (8)-(10). Let $(\theta^\infty, \Pi^\infty, U^\infty)$ denote the stationary point of the dynamical system (8)-(10); i.e. $(\theta^\infty, \Pi^\infty, U^\infty)$ solves:

$$[\theta^\infty]^\sigma = \frac{\lambda}{\rho \sigma} F'(U^\infty) \Pi^\infty \quad (12)$$

$$\Pi^\infty = \frac{1 - \theta^\infty}{\delta + \phi - \rho + \lambda(1 - F(U^\infty))}. \quad (13)$$

There are two types of optimal contracts; those whose piece rate value converges to U^∞ from above and those whose value converge to U^∞ from below. Figure 1 depicts the corresponding contracts $\theta^*(.)$ in tenure space.

Consider first the optimal contract for the firm offering the least generous contract, i.e., $U_0 = \underline{U}$. Further, assume $\underline{U} < U^\infty$. As shown in Figure 1, optimal $\theta(.) \equiv \theta^{s1}(.)$ increases with tenure and converges to the limit value θ^∞ . As piece rates increase with tenure, it follows $U \equiv U^{s1}$ increases with tenure (and converges to U^∞) (while continuation profit Π decreases with tenure and converges to Π^∞). Consider now the optimal contract offered by firms offering the most generous contract, i.e., $U_0 = \bar{U}$. Further, assume $\bar{U} > U^\infty$. Although the wage paid increases with tenure, the corresponding piece rate $\theta(.) \equiv \theta^{s2}(.)$ decreases with tenure and converges to θ^∞ from above. This is also illustrated in Figure 1. The two optimal contracts, $\theta^{s1}(.)$ and $\theta^{s2}(.)$, defined above will be termed the lower and upper baseline piece rate scales respectively.

Figure 1: Baseline Piece Rate Scales

Consider now a firm that offers a contract which yields an initial piece rate value U_0 such that $\underline{U} < U_0 < U^\infty$. As depicted in Figure 1, define t_0 as the point on the lower baseline contract where $U^{s1}(t_0) = U_0$. Optimality of the lower baseline piece rate scale now yields a major simplification: the optimal contract yielding this U_0 is simply the continuation contract starting at point t_0 on the lower baseline piece rate

scale; *i.e.*, the optimal contract $\theta^*(\tau|U_0)$ is $\theta^{s1}(t_0 + \tau)$ where the piece rate paid at tenure τ corresponds to point $(t_0 + \tau)$ on the lower baseline piece rate scale. Suppose instead $\bar{U} > U_0 > U^\infty$. This time the optimal contract yielding U_0 is the continuation contract starting at point t_0 on the upper baseline piece rate scale where $U^{s2}(t_0) = U_0$.

Thus for any $U_0 \in [\underline{U}, U^\infty]$, the optimal contract can be described by $\theta^{s1}(\cdot)$ and a starting time $t_0 \geq 0$. Further for $U_0 \in [U^\infty, \bar{U}]$, the optimal contract can be described by $\theta^{s2}(\cdot)$ and a starting time $t_0 \geq 0$. Hence, the distribution of optimal contracts with $U_0 \in [\underline{U}, \bar{U}]$ can be described by $(\theta^{s1}(\cdot), \Psi^1(\cdot), \theta^{s2}(\cdot), \Psi^2(\cdot))$ where Ψ^i is the distribution of starting times associated with $\theta^{si}(\cdot)$.

Of course it may happen that $\bar{U} = U^\infty$ in which case only the lower baseline scale exists. In fact we shall show this is a consequence of a Market Equilibrium which we now define.

4 MARKET EQUILIBRIUM

Above we have shown for any $U_0 \in [\underline{U}, \bar{U}]$ an optimal contract corresponds to a saddle path solution to the differential equation system (8)-(10). In what follows, however, equation (5) in Theorem 1 is much more useful as it describes the solution to the differential equation (8).

For any starting value $U_0 \in [\underline{U}, \bar{U}]$, the optimal contract corresponds to a starting point t_0 on one of the piece rate scales where $U^{si}(t_0) = U_0$, with corresponding maximized profit $\Pi^{si}(t_0)$ and piece rate paid $\theta^{si}(t_0)$. By substituting out t_0 , we can thus define $\theta = \hat{\theta}(U_0)$ as the piece rate paid when the worker enjoys U_0 on the baseline piece rate scales, and $\Pi = \hat{\Pi}(U_0)$ as the firm's continuation profit. Using the conditions of Theorem 1, Claim 1 identifies $\hat{\Pi}(U)$ and $\hat{\theta}(U)$.

Claim 1

For $U \in [\underline{U}, \overline{U}]$, $\widehat{\Pi}$ evolves according to the differential equation

$$\frac{d\widehat{\Pi}}{dU} = -\widehat{\theta}^\sigma \quad (14)$$

while $\widehat{\theta}$ satisfies

$$\begin{aligned} & \frac{[\widehat{\theta}]^{1-\sigma}}{1-\sigma} + \widehat{\theta}^{-\sigma} \left[1 - \widehat{\theta} + [\rho - \phi - \delta - \lambda(1 - F(U))] \widehat{\Pi} \right] \\ &= [\delta + \phi - \rho(1 - \sigma)]U - \delta U^U - \lambda \int_U^{\overline{U}} [1 - F(U_0)] dU_0. \end{aligned} \quad (15)$$

Proof: This follows directly from Theorem 1 and the definitions of $\widehat{\theta}$ and $\widehat{\Pi}$.

By construction, each firm's optimized steady state flow profit by offering $U_0 \in [\underline{U}, \overline{U}]$ is

$$\Omega^*(U_0) = \lambda \widehat{\Pi}(U_0) [\overline{ue} \int_{x=0}^{\infty} y_0 e^{\rho x} dN(x) + (1 - \overline{ue}) \int_{U'=\underline{U}}^{U_0} \int_{x=0}^{\infty} y_0 e^{\rho x} dH(x, U')]. \quad (16)$$

We now formally define a Market Equilibrium.

A **Market Equilibrium** is a distribution of optimal contract offers, with corresponding value distribution $F(U)$, such that optimal job search by workers and steady state turnover implies the constant profit condition:

$$\begin{aligned} \Omega^*(U_0) &= \overline{\Omega} > 0 \text{ if } dF(U_0) > 0, \\ \Omega^*(U_0) &\leq \overline{\Omega}, \text{ otherwise,} \end{aligned} \quad (17)$$

The constant profit condition requires that all optimal contracts U_0 which are offered by firms in an equilibrium must make the same profit $\overline{\Omega} > 0$, and all other contracts must make no greater profit. Below for any distribution of contract offers F , we first use steady state turnover arguments to determine the equilibrium unemployment rate $\overline{ue}$ and distribution functions N and H . Identifying a Market Equilibrium then requires finding $F(\cdot)$ so that the above constant profit condition is satisfied. We perform this task using a series of lemmas. Lemma 1 describes a standard result.

Lemma 1. A Market Equilibrium implies:

- (a) $\underline{U} = U^u$;
- (b) $\overline{ue} = (\phi + \delta)/(\lambda + \phi + \delta)$.

Part (a) establishes that the lowest value offer $\underline{U}$ extracts all search rents from the unemployed. Part (b) identifies the steady state unemployment rate given all unemployed workers accept their first job offer.

With Lemma 1 in hand, we can now characterize steady state $N(x)$ and $H(x, U)$. As all unemployed workers accept the first job offer received, and employed workers never quit into unemployment, obtaining the steady state distribution of experience across unemployed workers is straightforward. Standard turnover arguments establish

$$N(x) = 1 - \frac{\lambda\delta}{(\phi + \lambda)(\phi + \delta)} e^{-\frac{\phi(\phi + \delta + \lambda)x}{(\phi + \lambda)}}. \quad (18)$$

Let $N_0 = N(0)$ which describes the proportion of unemployed workers who have never had a job and so have zero experience. (18) implies $N_0 > 0$. For $x > 0$, the distribution of experience across unemployed worker is described by the exponential distribution.

Standard turnover arguments also establish that the distribution of experience across all employed workers is

$$H(x, \overline{U}) = 1 - e^{-\frac{\phi(\phi + \delta + \lambda)x}{(\phi + \lambda)}}. \quad (19)$$

In contrast to N , note that $H(0, \overline{U}) = 0$: in a steady state the measure of employed workers with zero experience must be zero. Lemma 2 now characterizes $H(\cdot)$ for all $x > 0$, $U \in [\underline{U}, \overline{U}]$.

Lemma 2. For $x > 0$ and $U \in [\underline{U}, \overline{U}]$, $H = H(x, U)$ satisfies the partial differential equation:

$$[\phi + \delta + \lambda(1 - F(U))]H + \frac{\partial H}{\partial x} + \dot{U} \frac{\partial H}{\partial U} = (\phi + \delta)F(U)N(x),$$

where along the baseline piece rate scale $\dot{U} = \dot{U}(U)$ is given by:

$$\dot{U} = \widehat{\theta}^{-\sigma} [(1 - \widehat{\theta}) - [\delta + \phi - \rho + \lambda(1 - F(U))]\widehat{\Pi}] \quad (20)$$

and H satisfies the boundary conditions

$$\begin{aligned} H(0, U) &= 0 \text{ for all } U \in [\underline{U}, \overline{U}]; \\ H(x, \underline{U}) &= 0 \text{ for all } x \geq 0. \end{aligned}$$

Although H is described by a relatively straightforward first order partial differential equation, a closed form solution does not exist. Nevertheless it is still possible to characterize fully a Market Equilibrium.

Substituting out $\overline{ue}$ (obtained in Lemma 1) and $N(x)$ (given by (18)) in (16), straightforward algebra implies the constant profit condition requires finding an F such that

$$\widehat{\Pi}(U_0) \left[\frac{\phi(\phi + \delta - \rho)}{\phi(\phi + \delta + \lambda) - \rho(\phi + \lambda)} + \frac{\lambda}{\lambda + \phi + \delta} \int_{U'=\underline{U}}^{U_0} \int_{x'=0}^{\infty} e^{\rho x'} \frac{\partial^2 H(x', U')}{\partial x \partial U'} dx' dU' \right] = \frac{\overline{\Omega}}{\lambda y_0} \quad (21)$$

for all $U_0 \in [\underline{U}, \overline{U}]$, with H given by Lemma 2. By solving for the last term in the square bracket above, the proof of Theorem 2 shows the constant profit condition reduces to the following simple condition.

Theorem 2. In any Market Equilibrium, the constant profit condition is satisfied if and only if

$$\widehat{\Pi} = \frac{1}{\phi + \delta - \rho} \sqrt{(1 - \bar{\theta})(1 - \widehat{\theta})} \text{ for all } U_0 \in [\underline{U}, \overline{U}], \quad (22)$$

where $\bar{\theta} = \widehat{\theta}(\overline{U})$ is the highest piece rate offered in the market.

Putting $\rho = 0$ finds this solution is the same as that found in Burdett and Coles (2003). Here of course, the Market Equilibrium depends on the rate of learning-by-doing.

5 Existence and Characterization of a Market Equilibrium.

The approach to solving for a Market Equilibrium is to hypothesize an equilibrium value for $\bar{\theta}$ and then use backward induction to map out the equilibrium outcomes.

The free choice of $\bar{\theta}$ is then tied down by the requirement $U^U = \underline{U}$ (Lemma 1a).

Conditional on an equilibrium value for $\bar{\theta}$, Lemma 3 now determines the corresponding equilibrium support of offers $[\underline{U}, \bar{U}]$ and finds the (unique) closed form solution for equilibrium $\hat{\theta}(\cdot)$.

Lemma 3. For any equilibrium value $\bar{\theta} \in (0, 1)$, a Market Equilibrium implies $\hat{\theta}(\cdot)$ is given by the implicit function

$$\frac{\sqrt{(1 - \bar{\theta})}}{2(\phi + \delta - \rho)} \int_{\bar{\theta}}^{\bar{\theta}} \frac{1}{(1 - \theta')^{1/2} [\theta']^\sigma} d\theta' = [\bar{U} - U] \quad (23)$$

for all $U \in [\underline{U}, \bar{U}]$ where $\bar{U}, \underline{U}$ satisfy

$$\frac{[\bar{\theta}]^{1-\sigma}}{1-\sigma} = [\phi - \rho(1 - \sigma)]\bar{U} + \delta[\bar{U} - \underline{U}] \quad (24)$$

$$(1 - \underline{\theta}) = \left[\frac{\phi + \delta - \rho + \lambda}{\phi + \delta - \rho} \right]^2 (1 - \bar{\theta}) \quad (25)$$

and $\underline{\theta} \equiv \hat{\theta}(\underline{U})$ is the lowest piece rate paid in the market; i.e.,

$$\frac{\sqrt{(1 - \bar{\theta})}}{2(\phi + \delta - \rho)} \int_{\underline{\theta}}^{\bar{\theta}} \frac{1}{(1 - \theta')^{1/2} [\theta']^\sigma} d\theta' = \bar{U} - \underline{U}.$$

Lemma 3 establishes the following important corollary.

Corollary: A Market Equilibrium implies $\bar{U} = U^\infty$.

The higher baseline piece rate scale in Figure 1 implied piece rates paid might (optimally) fall with tenure. A Market Equilibrium, however, rules out this possibility. In particular lemma 3 establishes that equilibrium $\hat{\theta}$ must satisfy (23) and differentiation implies

$$\frac{d\hat{\theta}}{dU} = 2(\phi + \delta - \rho)\bar{\theta}^\sigma$$

at $U = \bar{U}$ and so is finite. Conversely optimal contracting implies $\hat{\theta}$ must satisfy (15) and differentiation finds

$$\frac{d\hat{\theta}}{dU} = \frac{\frac{\lambda[\bar{\theta}^{1-\sigma}]}{\sigma} F'(\bar{U})\bar{\Pi} - \rho\bar{\theta}}{\bar{\theta}^{-\sigma}[1 - \bar{\theta} - [\delta + \phi - \rho]\bar{\Pi}]}$$

at $U = \bar{U}$. As Theorem 2 implies $\bar{\Pi} = \hat{\Pi}(\bar{U}) = (1 - \bar{\theta})/(\phi + \delta - \rho)$, the denominator in the above equation is therefore zero. Hence finiteness requires the numerator must also be zero; i.e. $\lambda \bar{\theta}^{1-\sigma} F'(\bar{U}) \bar{\Pi} / \sigma = \rho \bar{\theta}$. This immediately implies $d\theta/dt = dU/dt = d\Pi/dt = 0$ at $\bar{U}$ and so $\bar{U} = U^\infty$.

It is now straightforward to establish existence of a Market Equilibrium. Note that $\underline{\theta} \geq 0$ and (25) imply the relevant case is $\bar{\theta} \geq 1 - \left[\frac{\phi + \delta - \rho}{\phi + \delta - \rho + \lambda} \right]^2$. Conditional on an equilibrium value $\bar{\theta} \in (1 - \left[\frac{\phi + \delta - \rho}{\phi + \delta - \rho + \lambda} \right]^2, 1)$, it is trivial to show a solution to the equations in Lemma 3 for $\hat{\theta}, \underline{U}, \bar{U}$ always exists, is unique, is continuous in $\bar{\theta}$ and implies $0 < \underline{\theta} < \bar{\theta}$ and $\underline{U} < \bar{U}$. Note that Theorem 2 then uniquely determines equilibrium $\hat{\Pi}(\cdot)$. To determine equilibrium F , define the surplus function

$$S(U) = \int_U^{\bar{U}} [1 - F(U')] dU'.$$

As $U^U = \underline{U}$ in a Market Equilibrium, (15) implies equilibrium S is determined by the linear differential equation

$$\frac{[\hat{\theta}]^{1-\sigma}}{1-\sigma} + \hat{\theta}^{-\sigma} \left[1 - \hat{\theta} + [\rho - \phi - \delta + \lambda \frac{dS}{dU}] \hat{\Pi} \right] = [\delta + \phi - \rho(1 - \sigma)]U - \delta \underline{U} - \lambda S \quad (26)$$

for all $U \in [\underline{U}, \bar{U}]$ with initial value $S(\bar{U}) = 0$. Using the solutions above for $\hat{\theta}, \hat{\Pi}$, and $\underline{U}$, and noting Theorem 2 implies $\hat{\Pi} \geq (1 - \bar{\theta})/(\phi + \delta - \rho) > 0$, this initial value problem uniquely determines S , and thus $F(U)$. The final step, then, is to note a Market Equilibrium must also satisfy $U^U = \underline{U}$ where U^U is given by (2). This identifies a fixed point problem which ties down the equilibrium value of $\bar{\theta}$.

Theorem 3. [Existence and Characterization]. For $\sigma > 0$, a Market Equilibrium exists characterised by a $\bar{\theta} \in (1 - \left[\frac{\phi + \delta - \rho}{\phi + \delta - \rho + \lambda} \right]^2, 1)$ with

(A) the support of offers $[\underline{U}, \bar{U}]$ (and corresponding $\underline{\theta}$) given by (24)-(25), where over that support,

(B) $\hat{\theta}(\cdot)$ is given by (23), $\hat{\Pi}(\cdot)$ is given by (22), $S(\cdot)$ is the solution to the initial value problem (26) with $S(\bar{U}) = 0$;

(C) U^U is given by (2) and satisfies $U^U = \underline{U}$.

6 Empirical Implications and Conclusion

The analysis generalizes straightforwardly to the case that workers are heterogenous. In particular note that the equilibrium characterization in Theorem 3 does not depend on y_0 . Assume instead then that each new entrant has productivity y_0 drawn from some population distribution A . Theorem 3 continues to describe the Market Equilibrium: all workers continue to use the same turnover strategies, the unemployment rate and distribution of experience is the same for each type y_0 , and the equilibrium set of optimal piece rate contracts is unchanged. The only difference is that steady state flow profit is now

$$\Omega^*(U_0) = \lambda \hat{\Pi}(U_0) \int_{\underline{y}}^{\bar{y}} \left[\overline{ue} \int_{x=0}^{\infty} y_0 e^{\rho x} dN(x) + (1 - \overline{ue}) \int_{U'=\underline{U}}^{U_0} \int_{x=0}^{\infty} y_0 e^{\rho x} dH(x, U') \right] dA(y_0) \quad (27)$$

for all $U_0 \in [\underline{U}, \bar{U}]$. By defining $\mu = \int_{\underline{y}}^{\bar{y}} y_0 dA(y_0)$, all the previous arguments go through but with y_0 now replaced by μ .

Although a trivial theoretical extension, the extension to worker heterogeneity is clearly crucial for empirical work. If y_i denotes the initial productivity of worker i , then a Market Equilibrium implies the wage earned by this worker after x years experience, with tenure τ at firm j offering contract $\theta_j(\cdot)$ is:

$$\log w_{ij}(x, \tau) = \log y_i + \log \theta_j(0) + \rho x + \log \frac{\theta_j(\tau)}{\theta_j(0)}. \quad (28)$$

The observed wage thus depends on the worker fixed effect $\log y_i$, the firm fixed effect $\log \theta_j(0)$ (which describes firm j 's starting piece rate paid to new hires), experience effect x and the tenure effect at firm j . Of course a Market Equilibrium not only identifies the distribution of starting piece rates $\theta_j(0)$ across all firms j , it also determines the within-firm tenure effects $\theta_j(\tau)/\theta_j(0)$.

In contrast Altonji and Williams (2005) points out that, in the applied literature, the standard wage regression equation is of the form

$$\log w_{ij}(x, \tau) = \rho x + \beta_2 \tau + \varepsilon_{ijt}$$

where β_2 measures the return to tenure and the error term

$$\varepsilon_{ijt} = y_i + \phi_{ij} + u_{it} + \nu_{ijt}$$

contains both a worker fixed effect y_i and a random match payoff ϕ_{ij} between worker i and firm j . The remaining error terms suppose these key residuals might vary randomly over time.

A key difference between these two approaches is that the wage equation (28) contains a firm fixed effect, $\log \theta_j(0)$. This fixed effect is central to our explanation of quit turnover: a quit occurs whenever an employee at firm j on piece rate $\theta_j(\tau)$ receives an outside offer from a different firm k which offers starting piece rate $\theta_k(0) > \theta_j(\tau)$.

The standard empirical approach instead assumes there is unobserved match heterogeneity. The difficulty then is that with endogenous quit turnover, the unobserved match value is positively correlated with experience and tenure: the former as workers with long experience have had more time to find a good match, the latter as matches with high value are likely to survive to long tenures. Controlling for this endogeneity problem is clearly problematic (see for example the classic papers Topel (1991), Altonji and Shakotko (1991) and more recently Dustmann and Meghir (2005) which identifies the return to experience by instead focussing on workers laid-off through plant closure).

An additional empirical issue is that the estimated return to tenure, β_2 above, is assumed to be firm-independent. The theory here not only shows this is unlikely but numerical examples find the (firm specific) tenure effect on wages is always negatively correlated with the firm fixed effect; i.e. tenure effects are larger at low wages. Or in other words, the (lower) baseline piece rate scale is concave (as drawn in Figure 1).

There seem to be two principal reasons for this. First, note that optimal contracting implies wages evolve according to (11), i.e

$$\frac{d}{dt} \log(w(t)) = \frac{\lambda F'(U) \Pi}{\sigma \theta^\sigma}, \quad (29)$$

within an employment spell. Firms which offer a lower starting piece rate enjoy a higher expected profit per new hire Π (but in equilibrium attract fewer hires). (29)

implies greater profit Π implies wages rise more quickly with tenure: the firm has a greater incentive not to lose the worker to an outside offer. Second, numerical work always finds that the equilibrium job offer distribution is tightly bunched at the lower end of the distribution. Indeed there is always a mass of firms which offer $U = \underline{U}$. Strong competition for workers at the bottom end of the wage distribution again leads firms to raise wages relatively quickly with tenure. Of course when the worker's earned piece rate is close to the top end of the distribution, and so the worker is unlikely to receive a more favourable outside offer, there is little incentive for the firm to keep raising its piece rate paid.

The approach taken here also yields a theory of cross section wage dispersion which is consistent with the distribution of wage/age profiles across individual workers. Specifically the model has an overlapping generation structure - where different individuals enter the labour market at different dates - and heterogeneous outcomes where an individual's wage depends not only on accumulated experience but also on luck in finding well paid employment. Equilibrium turnover implies interesting sorting effects: higher wage firms not only attract and retain more workers, but also, in steady state, enjoy a more experienced and thus more productive workforce (see Burdett et al (2010)). Of course these sorting effects have a direct impact on equilibrium contract competition. Such sorting also significantly increases wage inequality: young workers not only have little work experience, they also typically earn low piece rates as starting offers are rarely generous and internal promotion takes time. Indeed reservation piece rate (values) of the unemployed are particularly low as (i) experience is valuable and an employee can still search for better paid employment while employed, and (ii) expectations of promotion within a firm generates a "foot-in-the-door" effect as described in Burdett and Coles (2003).

It should also be noted that the transition functions from job to job and between unemployment and employment can be easily obtained in equilibrium. Most of these are constant through time. The quit flow from one job to another job, however, decreases with tenure; i.e. at any given firm, there is negative duration dependence in its employees' job-to-job hazard rate. This testable prediction distinguishes our

approach from the one taken by Bagger et al (2010). In that framework a worker always quits whenever he/she contacts a more productive firm; i.e. at any given firm, its employees' job-to-job hazard rate is duration independent.

Finally we comment on our restriction that the piece rate contract $\theta(\tau)$ is not conditioned on prior experience x_0 ; i.e. what happens if we allow more general contracts $\theta = \theta(.|x_0)$? First note that equation (29), which describes how wages evolve within the employment spell, will continue to hold: it describes the optimal (local) trade-off between smoother wages and reduced quit incentives. The fundamental difference is that if contract offers discriminate by prior experience then the distribution of outside offers is described by $F(U|x_0)$. Clearly this extension significantly complicates any equilibrium analysis: it then needs to characterise a continuum of outside offer distributions. Such an extension, however, would have two clear implications. First it implies workers with the same productivity but different prior experience are offered different contracts. Such discrimination is potentially illegal - it allows firms to discriminate against, say, highly talented women who return to the workplace after a spell of child-rearing. Second the wage equation must be extended as

$$\log w_{ij}(x, \tau|x_0) = \log y_i + \log \theta_j(0|x_0) + \rho x + \log \frac{\theta_j(\tau|x_0)}{\theta_j(0|x_0)}$$

where x_0 describes the worker's prior experience at the point of hire. But this equation can be rearranged as

$$\log \hat{w}_{ij}(\tau, x_0) = \log y_i + [\log \theta_j(0|x_0) + \rho x_0] + \left[\log \frac{\theta_j(\tau|x_0)}{\theta_j(0|x_0)} + \rho \tau \right],$$

where the second term describes the prior experience effect and the last term describes the tenure effect (interacted with prior experience). Clearly identifying the return to experience ρ becomes more problematic with such discrimination.

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7 Appendix.

Proof of Theorem 1. Define $\Phi(t) = e^{\rho t} \psi(t|\cdot)$. The firm's optimal contract solves

$$\max_{\theta(\cdot) \geq 0} \int_0^\infty \Phi(t)[1 - \theta(t)]dt$$

where (1) and (3) in the text imply:

$$\dot{\Phi} = [\rho - \phi - \delta - \lambda(1 - F(U))]\Phi \quad (30)$$

$$\dot{U} = [\delta + \phi - \rho(1 - \sigma)]U - \frac{\theta^{1-\sigma}}{1 - \sigma} - \delta U^U - \lambda \int_U^{\bar{U}} [1 - F(U_0)]dU_0 \quad (31)$$

and with starting values

$$\Phi(0) = 1; U(0) = U_0.$$

Define the Hamiltonian

$$\begin{aligned} H = & \Phi[1 - \theta] + \mu_\Phi[\rho - \phi - \delta - \lambda(1 - F(U))]\Phi \\ & + \mu_U \left[[\delta + \phi - \rho(1 - \sigma)]U - \frac{\theta^{1-\sigma}}{1 - \sigma} - \delta U^U - \lambda \int_U^{\bar{U}} [1 - F(U_0)]dU_0 \right]. \end{aligned}$$

where μ_Φ, μ_U denote the costate variables associated with the state variables Φ, U . Whenever the corner constraint $\theta \geq 0$ is not binding, the Maximum Principle implies the necessary conditions for a maximum are:

$$\frac{\partial H}{\partial \theta} = -\Phi - \mu_U \theta^{-\sigma} = 0 \quad (32)$$

and

$$\frac{d\mu_\Phi}{dt} = -[1 - \theta(t)] - \mu_\Phi[\rho - \phi - \delta - \lambda(1 - F(U))]. \quad (33)$$

The standard approach also identifies a differential equation for μ_U but we cannot use that approach as we do not assume F is differentiable. Instead no discounting implies the additional constraint

$$H = 0$$

(e.g. p298, Leonard and Long (1992)) and this condition is sufficient to establish the Theorem.

Integrating (33) yields:

$$\begin{aligned}\mu_{\Phi}(t) &= \int_t^{\infty} e^{-\int_t^s [\delta + \phi - \rho + \lambda(1 - F(U(\tau)))] d\tau} (1 - \theta(s)) ds + A_0 e^{\int_0^t [\phi + \delta + \lambda(1 - F(V(x))) - \rho] dx} \\ &= \Pi(t) + A_0 e^{\int_0^t [\phi + \delta + \lambda(1 - F(V(x))) - \rho] dx}\end{aligned}$$

where A_0 is the constant of integration and $\Pi(\cdot)$ is the firm's continuation profit as defined in the Theorem. As (32) implies $\mu_U = -\Phi\theta^{\sigma}$, then substituting out μ_U and μ_{Φ} in the definition of H , the restriction $H=0$ yields the optimality condition:

$$\begin{aligned}0 &= [1 - \theta] + \left[\Pi + A_0 e^{\int_0^t [\phi + \delta + \lambda(1 - F(U(\tau)))] d\tau} \right] [\rho - \phi - \delta - \lambda(1 - F(U))] \\ &\quad - \theta^{\sigma} \left[[\delta + \phi - \rho(1 - \sigma)]U - \frac{\theta^{1-\sigma}}{1 - \sigma} - \delta U^U - \lambda \int_U^{\bar{U}} [1 - F(U_0)] dU_0 \right]. \quad (34)\end{aligned}$$

Now the restriction $\phi > \rho$ ensures $\exp[\int_0^t [\phi + \delta + \lambda(1 - F(U(\tau)))] d\tau]$ grows exponentially as $t \rightarrow \infty$. As Π and U must be bounded (otherwise an employee or firm must be willing to make unboundedly large losses) then (34) implies $A_0 = 0$. (34) now yields (5) given in the Theorem. Using this to substitute out $\frac{\theta^{1-\sigma}}{1-\sigma}$ in (31) then yields (7).

Finally note (5) determines θ . As $\theta \rightarrow 0$, $\sigma > 0$ guarantees the left hand side of (5) becomes unboundedly large. As the right hand side of (5) is bounded it follows that $\sigma > 0$ implies $\theta \geq 0$ is never a binding constraint. This completes the proof of Theorem 1.

Proof of Lemma 1:

Lemma 1(a) follows from standard contradiction arguments. $\underline{U} < U^u$ is inconsistent with strictly positive profit (firms offering starting value $U_0 < U^u$ make zero profit), while $\underline{U} > U^u$ is inconsistent with the constant profit condition (offering $U_0 = \underline{U}$ is dominated by offering $U_0 = U^U$ as both offers only attract the unemployed and offering $U^u < \underline{U}$ generates greater profit per hire). Lemma 1(b) then follows from standard turnover arguments.

Proof of Lemma 2: Consider the pool of employed workers who have experience no greater than $x > 0$ and piece rate value no greater than U . Then for $U < U^{\infty}$, the

total outflow of workers from this pool, over any instant of time $dt > 0$, is

$$(1 - \bar{ue})H(x, U)[\phi + \delta + \lambda(1 - F(U))]dt + (1 - \bar{ue}) \int_{U'=\underline{U}}^U \int_{x'=x-dt}^x \frac{\partial^2 H}{\partial U \partial x} dU' dx' \\ + (1 - \bar{ue}) \int_{U'=U^s(t-dt)}^{U^s(t)} \int_{x'=0}^x \frac{\partial^2 H}{\partial U \partial x} dU' dx' + O(dt^2),$$

where the first term is the number who die, lose their job or quit through receiving a job offer with value greater than U , the second is the number who exit through achieving greater experience, while the third is the number who exit through internal promotion, where $U^s(t) = U$. The inflow is $\lambda \bar{ue} F(U) N(x) dt$ which is the number of unemployed workers with experience no greater than x who receive a job offer with value no greater than U . Setting inflow equal to outflow, using the solution for $\bar{ue}$ in lemma 1 and letting $dt \rightarrow 0$ implies H satisfies:

$$H(x, U)[\phi + \delta + \lambda(1 - F(U))] + \int_{U'=\underline{U}}^U \frac{\partial^2 H}{\partial U \partial x} dU' \\ + \dot{U} \int_{x'=0}^x \frac{\partial^2 H}{\partial U \partial x} dx' = (\phi + \delta) F(U) N(x).$$

Integrating thus yields

$$H(x, U)[\phi + \delta + \lambda(1 - F(U))] + \left[\frac{\partial H[x, U]}{\partial x} - \frac{\partial H[x, \underline{U}]}{\partial x} \right] \\ + \dot{U} \left[\frac{\partial H[x, U]}{\partial U} - \frac{\partial H[0, U]}{\partial U} \right] = (\phi + \delta) F(U) N(x).$$

But $H(0, U) = H(x, \underline{U}) = 0$ implies $\frac{\partial H[x, \underline{U}]}{\partial x} = \frac{\partial H[0, U]}{\partial U} = 0$ which with the above equation yields the stated solution. This argument but for $U > U^\infty$ establishes the same differential equation. This completes the proof of Lemma 2.

Proof of Theorem 2. The central step is to solve for

$$\int_{x'=0}^\infty \int_{U'=\underline{U}}^{U_0} e^{\rho x'} \frac{\partial^2 H(x', U')}{\partial x \partial U'} dx' dU'$$

with $H(\cdot)$ as described by Lemma 2.

First note that as the measure of employed workers with no experience is zero, then

$$\begin{aligned} \int_{x'=0}^{\infty} \int_{U'=\underline{U}}^{U_0} e^{\rho x'} \frac{\partial^2 H(x', U')}{\partial x \partial U'} dx' dU' &= \int_{x'>0} e^{\rho x'} \left[\int_{U'=\underline{U}}^{U_0} \frac{\partial^2 H(x', U')}{\partial x \partial U'} dU' \right] dx' \\ &= \int_{x'>0} e^{\rho x'} \frac{\partial H(x', U_0)}{\partial x} dx'. \end{aligned}$$

as $H_x(x', \underline{U}) = 0$. Thus (21) implies

$$\hat{\Pi}(U_0) \left[\frac{\phi(\phi + \delta - \rho)}{\phi(\phi + \delta + \lambda) - \rho(\phi + \lambda)} + \frac{\lambda}{\lambda + \phi + \delta} \int_{x'>0} e^{\rho x'} \frac{\partial H(x', U_0)}{\partial x} dx' \right] = \frac{\bar{\Omega}}{\lambda y_0} \quad (35)$$

for all $U_0 \in [\underline{U}, \bar{U}]$. Differentiating wrt U_0 implies

$$\left[\frac{d\hat{\Pi}}{dU} \left[\frac{\phi(\phi + \delta - \rho)}{\phi(\phi + \delta + \lambda) - \rho(\phi + \lambda)} + \frac{\lambda}{\lambda + \phi + \delta} \int_{x'>0} e^{\rho x'} \frac{\partial H(x', U_0)}{\partial x} dx' \right] + \hat{\Pi} \left[\frac{\lambda}{\lambda + \phi + \delta} \int_{x'>0} e^{\rho x'} \frac{\partial^2 H(x', U_0)}{\partial x \partial U} dx' \right] \right] = 0 \text{ for all } U_0 \in [\underline{U}, \bar{U}]. \quad (36)$$

Consider now the integral in the second line. For $x > 0$, partial differentiation with respect to x of the pde for H , given by lemma 2, implies

$$\dot{U} \frac{\partial^2 H}{\partial x \partial U} = (\phi + \delta) F N'(x) - \left[[\phi + \delta + \lambda(1 - F)] \frac{\partial H}{\partial x} + \frac{\partial^2 H}{\partial x^2} \right],$$

where $\dot{U} = \dot{U}(U)$ is given by (20). Thus

$$\int_{x'>0} e^{\rho x'} \frac{\partial^2 H(x', U_0)}{\partial x \partial U} dx' = \frac{1}{\dot{U}} \int_{x'>0} e^{\rho x'} \left[(\phi + \delta) F N'(x) - \left[[\phi + \delta + \lambda(1 - F)] \frac{\partial H}{\partial x} + \frac{\partial^2 H}{\partial x^2} \right] \right] dx'. \quad (37)$$

Straightforward algebra using (18) finds

$$\int_{x'>0} e^{\rho x'} (\phi + \delta) F N'(x) dx = \frac{\phi \lambda \delta (\phi + \delta + \lambda) F}{(\phi + \lambda) [\phi(\phi + \delta + \lambda) - \rho(\phi + \lambda)]}$$

The second term in (37) is computed as follows:

$$\begin{aligned} &\int_{x'>0} e^{\rho x'} \left[[\phi + \delta + \lambda(1 - F)] \frac{\partial H}{\partial x} + \frac{\partial^2 H}{\partial x^2} \right] dx' \\ &= \int_{x'>0} e^{[\rho - [\phi + \delta + \lambda(1 - F)]]x'} \left\{ e^{[\phi + \delta + \lambda(1 - F)]x'} \left[[\phi + \delta + \lambda(1 - F)] \frac{\partial H}{\partial x} + \frac{\partial^2 H}{\partial x^2} \right] \right\} dx' \\ &= \left[e^{\rho x'} \frac{\partial H(x', U_0)}{\partial x} \right]_{0+}^{\infty} - \int_{x'>0} [\rho - [\phi + \delta + \lambda(1 - F)]] e^{\rho x'} \frac{\partial H(x', U_0)}{\partial x} dx' \end{aligned}$$

Putting $x = 0$ in the pde for H (see Lemma 2) implies

$$\frac{\partial H(0, U)}{\partial x} = (\phi + \delta)N_0 F(U).$$

Now as $x' \rightarrow \infty$, the conditional distribution of employee payoffs $H(U|x')$ converges to its ergodic distribution $H(U|\infty)$. As the distribution of experience is exponential with parameter $\phi(\phi + \delta + \lambda)/(\phi + \lambda)$ [see equation (19) in the text] then $\phi > \rho$ guarantees $\lim_{x' \rightarrow \infty} \exp(\rho x') \partial H / \partial x = 0$. Thus we obtain:

$$\begin{aligned} & \int_{x' > 0} e^{\rho x'} \left[[\phi + \delta + \lambda(1 - F)] \frac{\partial H}{\partial x} + \frac{\partial^2 H}{\partial x^2} \right] dx' \\ &= [\phi + \delta - \rho + \lambda(1 - F)] \int_{x' > 0} e^{\rho x'} \frac{\partial H(x', U_0)}{\partial x} dx' - (\phi + \delta)N_0 F \\ &= [\phi + \delta - \rho + \lambda(1 - F)] \int_{x' > 0} e^{\rho x'} \frac{\partial H(x', U_0)}{\partial x} dx' - \frac{\phi(\phi + \lambda + \delta)}{\phi + \lambda} F \end{aligned}$$

by definition of N_0 and (18). Inserting this solution into (37) yields an equation for $\int_{x' > 0} e^{\rho x'} \frac{\partial^2 H(x', U_0)}{\partial x \partial U} dx'$. Using that equation to substitute out $\int_{x' > 0} e^{\rho x'} \frac{\partial^2 H(x', U_0)}{\partial x \partial U} dx'$ in (36) then yields a closed form solution for $\int_{x' > 0} e^{\rho x'} \frac{\partial H(x', U_0)}{\partial x} dx'$. Using this expression for $\int_{x' > 0} e^{\rho x'} \frac{\partial H(x', U_0)}{\partial x} dx'$ in (35) and simplifying, the constant profit condition reduces (miraculously) to

$$\widehat{\Pi}^2 = \frac{[\phi(\phi + \delta + \lambda) - \rho(\phi + \lambda)] \bar{\Omega}}{\phi(\phi + \delta - \rho)[\delta + \phi - \rho + \lambda] \lambda y_0} (1 - \widehat{\theta}) \text{ for all } U_0 \in [\underline{U}, \bar{U}].$$

Finally we substitute out $\bar{\Omega}$ in this expression. Putting $U_0 = \bar{U}$ in (35), letting $\bar{\Pi} \equiv \widehat{\Pi}(\bar{U})$, substituting out $H(x, \bar{U})$ using (19) and some algebra establishes

$$\bar{\Pi} \left[\frac{\phi(\phi + \delta - \rho + \lambda)}{\phi(\phi + \delta + \lambda) - \rho(\phi + \lambda)} \right] = \frac{\bar{\Omega}}{\lambda y_0}. \quad (38)$$

Substituting out $\bar{\Omega}$ in the previous equation now yields

$$\widehat{\Pi}^2 = \frac{\bar{\Pi}}{(\phi + \delta - \rho)} (1 - \widehat{\theta}) \text{ for all } U_0 \in [\underline{U}, \bar{U}].$$

Setting $U_0 = \bar{U}$ implies

$$\bar{\Pi} = \frac{1 - \bar{\theta}}{\phi + \delta - \rho}, \quad (39)$$

and combining the last two expressions yields the Theorem. This completes the proof of Theorem 2.

Proof of Lemma 3. Using Theorem 2 to compute $d\hat{\Pi}/dU$ and using (14) in Claim 1 implies $\hat{\theta}(\cdot)$ satisfies

$$\frac{\phi(\phi + \delta - \rho) + \lambda\phi}{2\phi(\phi + \delta - \rho)[\delta + \phi - \rho + \lambda]} \sqrt{(1 - \bar{\theta})(1 - \hat{\theta})^{-1/2}\hat{\theta}^{-\sigma}} \frac{d\hat{\theta}}{dU} = 1$$

with $\hat{\theta} = \bar{\theta}$ at $U = \bar{U}$. Integrating implies (23). Putting $U = \bar{U}$ in (15) and using (39) in the Appendix implies (24). Noting $\partial H(x, \underline{U})/\partial x = 0$, then putting $U = \underline{U}$ in (35) and using (38), (39) and Theorem 2 yields (25). Finally putting $U = \underline{U}$ in (23) implies (24). This completes the proof of Lemma 3.

Proof of Theorem 3: By construction these are necessary conditions for a Market Equilibrium. Given any such solution, then by construction all optimal contracts which offer $U_0 \in [\underline{U}, \bar{U}]$ yield the same steady state flow profit. Consider now any deviating contract. Clearly, a suboptimal contract which offers $U_0 \in [\underline{U}, \bar{U}]$ yields lower profit. Further any contract which offers value $U_0 < \underline{U}$ yields zero profit as $U^U = \underline{U}$ and all workers reject such an offer. Finally any contract which offers $U_0 > \bar{U}$ attracts no more workers than an optimal contract which offers $\bar{U}$ while the latter contract earns strictly greater profit per hire.⁶ As no deviating contracts exist which yield greater profit, a solution to the above conditions identifies a Market Equilibrium.

We now establish existence of a solution when $\sigma > 0$. Given an arbitrary value for $\bar{\theta} \in (1 - \left[\frac{\phi + \delta - \rho}{\phi + \delta - \rho + \lambda}\right]^2, 1)$, let $\tilde{F}(\cdot|\bar{\theta})$ denote the solution for F implied by solving parts A,B of Theorem 3 above. Further define $\tilde{U}^U(\bar{\theta})$ as the solution for U^U where

$$\phi U^U = \frac{b^{1-\sigma}}{1-\sigma} + \lambda \int_{U^U}^{\bar{U}} [1 - \tilde{F}(\cdot|\bar{\theta})] dU_0; \quad (40)$$

i.e. $\tilde{U}^U(\bar{\theta})$ is the optimal reservation piece rate U^U of unemployed workers given offer distribution $\tilde{F}(\cdot|\bar{\theta})$. A Market Equilibrium requires finding a $\bar{\theta} \in (1 - \left[\frac{\phi + \delta - \rho}{\phi + \delta - \rho + \lambda}\right]^2, 1)$ such that $\tilde{U}^U(\bar{\theta}) = \underline{U}(\bar{\theta})$.

⁶Note the arguments in Burdett and Coles (2003) rule out a mass point in H at $U = \bar{U}$.

First note that as $\bar{\theta} \rightarrow 1$, (25) implies $\underline{\theta} \rightarrow 1$. As all piece rates θ paid must then lie in an arbitrarily small neighborhood around one, frictions ($\lambda < \infty$) and $b < 1$ imply $\tilde{U}^U < \underline{U}$. Instead consider the limit $\bar{\theta} \rightarrow \lambda(\lambda + 2[\phi + \delta - \rho]) / (\phi + \delta - \rho + \lambda)^2$ which, by (25), implies $\underline{\theta} \rightarrow 0$. $\sigma \geq 1$ implies the flow payoff by accepting the lowest $\underline{\theta}$ offer, $\underline{\theta}^{1-\sigma} / (1-\sigma)$, becomes unboundedly negative in this limit. As $\hat{\theta}(\cdot)$ is continuous and is less than $\bar{\theta}$, this implies $\underline{U} \rightarrow -\infty$ in this limit. But (40) implies $\phi \tilde{U}^U > \frac{b^{1-\sigma}}{1-\sigma}$ and thus $\tilde{U}^U > \underline{U}$ in this limit. As the solutions for $\hat{\theta}(\cdot)$, $\hat{\Pi}(\cdot)$, $S(\cdot)$ and $\underline{U}$ are all continuous in $\bar{\theta}$, continuity now implies a $\bar{\theta} \in (1 - \left[\frac{\phi + \delta - \rho}{\phi + \delta - \rho + \lambda} \right]^2, 1)$ exists where $\tilde{U}^U = \underline{U}$ and so identifies a Market Equilibrium. This completes the proof of Theorem 3.

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