CESifo WORKING PAPERS

7044
2018

May 2018

Is there always a Trade-off between Insurance and Incentives? The Case of Unemployment with Subsistence Constraints

Juliana Mesén Vargas, Bruno Van der Linden

CESifo

Impressum:

CESifo Working Papers
ISSN 2364-1428 (electronic version)
Publisher and distributor: Munich Society for the Promotion of Economic Research - CESifo GmbH
The international platform of Ludwigs-Maximilians University's Center for Economic Studies and the ifo Institute
Poschingerstr. 5, 81679 Munich, Germany
Telephone +49 (0)89 2180-2740, Telefax +49 (0)89 2180-17845, email office@cesifo.de
Editors: Clemens Fuest, Oliver Falck, Jasmin Gröschl
www.cesifo-group.org/wp

An electronic version of the paper may be downloaded
· from the SSRN website: www.SSRN.com
· from the RePEc website: www.RePEc.org
· from the CESifo website: www.CESifo-group.org/wp

CESifo *Working Paper No. 7044*
Category 4: Labour Markets

Is there always a Trade-off between Insurance and Incentives? The Case of Unemployment with Subsistence Constraints

Abstract

This article analyzes the behavioral effects of unemployment benefits (UB) and it characterizes their optimal level when jobless people, who can carry out a subsistence activity, only survive if they have access to a minimum consumption level. Our model shows that if the level of UB is low enough, increasing its level or providing liquidity to the agent can decrease the duration in unemployment. Extensive numerical simulations indicate that the relationship between the level of the benefits and the probability of finding a formal job is frequently inverse U-shaped. We show that rewriting the insurance gain of the Baily-Chetty formula in terms of sufficient statistics requires specific modeling assumptions. The optimal replacement rate is generally higher than when subsistence is ignored.

JEL-Codes: D910, H210, J640, J650.

Keywords: liquidity effect, scarcity, monetary costs, optimal insurance.

Juliana Mesén Vargas
IRES Université catholique de Louvain
Belgium - 1348 Louvain-la-Neuve
juliana.mesenvargas@uclouvain.be

Bruno Van der Linden
FNRS; IHRES
Université catholique de Louvain
Belgium - 1348 Louvain-la-Neuve
bruno.vanderlinden@uclouvain.be

30th April 2018
This paper is a revised version of the IZA DP 11034 of September 2017. We would like to thank Robin Boadway, Pierre Cahuc, Johannes Johnen, Andrey Launov, Alan Manning, François Maniquet, Rigas Oikonomou, Johannes Schmieder, Robert Shimer and Klaus Wälde for useful conversations, and the participants to the Search and Matching Workshop 2017 in Kent University and to the CESifo Area Conference 2018 “Employment and Social Protection” for their comments. The usual disclaimer applies.

1 Introduction

Unemployment insurance is not present in a number of countries (Vodopivec, 2013, Bosch and Esteban-Pretel, 2015) and, where it is in place, the coverage and the level of benefits are sometimes low (Kupets, 2006 and Matsaganis et al., 2014[1]). This raises the question of the subsistence of jobless people. This article analyzes the behavioral effects of unemployment benefits (UB) and it characterizes their optimal level when jobless people only survive if they have access to a minimum or subsistence consumption level in each period. Even though the existence of subsistence constraints has been recognized in the economic literature,[2] to the best of our knowledge, the design of unemployment insurance schemes has not explicitly integrated daily subsistence requirements.[3] This paper also looks at the impact of providing liquidity to the agents (irrespectively of their employment status, and that should not be repaid through specific taxes).

Our model shows that if the level of UB is low enough, increasing its level can *decrease* the duration in unemployment; for higher levels of UB we reach the standard property that increasing UB increases duration. Our model also shows that if the level of UB is low enough, providing some liquidity can actually *decrease* the duration in unemployment; for higher levels of UB we obtain the standard property that liquidity increases duration (Chetty, 2008). Furthermore, compared to a framework where minimum consumption is ignored, the optimal replacement rate is generally higher. We also show that the optimal level of UB satisfies the Baily-Chetty formula (Baily, 1978, Chetty, 2006), but contrary to Chetty (2008), in our model the gain from insurance cannot be rewritten using sufficient statistics; we show that such decomposition is not general, it actually requires specific modeling assumptions.

Some authors have assumed that the factors affecting the chance of finding a job are not summarized by a scalar variable (van den Berg and van der Klaauw, 2006 distinguish formal and informal search effort; Caliendo et al., 2015, distinguish search effort and locus of control). We emphasize that exiting to a job requires two inputs : some job-search effort(s) and cognitive resources.

According to Mullainathan, Shafir and co-authors, (Shah et al., 2012 , Mullainathan and Shafir, 2013, Mani et al., 2013, Shah et al., 2015, and Schilbach et al., 2016) who develop a number of experiments both in the United States and in developing countries, the cognitive capacity or "bandwidth" of agents is limited. "Bandwidth measures our computational capacity, our ability to pay attention, to make good decisions, to stick with our plans, and to resist temptations" (Mullainathan and Shafir, 2013, p.41).

[1] For OECD countries, additional evidence can be found by visiting http://www.oecd.org/els/benefits-and-wages-statistics.htm.

[2] In the literature of development economics, see for instance: Dercon (1998) and Zimmerman and Carter (2003) about the role of subsistence constraints on assets accumulation for the poor and Bhalotra (2007) about the link between subsistence constraints and child work. In the literature on social insurance it has been mentioned by Chetty (2006) and Chetty and Looney (2006).

[3] As will soon be clear, this goes beyond the assumption that the marginal utility of consumption becomes huge when the level of consumption tends to zero. Pavoni (2007) analyzes the design of unemployment insurance when the planner must respect a lower bound on the expected discounted utility of the agent. The unemployed agent decides whether to search, or not (binary decision) subject to the scheme proposed by the planner.

When the subsistence of the individual needs to be guaranteed and UB are low or absent, the unemployment risk is not covered by private insurers[4] and credit markets are imperfect of absent, the person needs a behavioral margin: a daily life activity (for example, looking for discounts in the supermarket, fixing old clothes, etc) and / or a casual informal activity (for example, selling home-made food, subsistence farming, etc) that allow the person to increase her consumption out of the same level of UB.

Performing these activities, "taxes" the cognitive capacity of the agent, and leaves less cognitive resources available for job search. Mullainathan, Shafir and co-authors state: "We suggest that cognitive load arises because people are more engaged with problems where scarcity is salient. This consumes attentional resources and leaves less for elsewhere." Shah et al. (2012). Consequently, in our model the exit probability from unemployment to a formal job is affected by job search effort and also by the cognitive resources available for this task. Given that cognitive resources are limited, dealing with subsistence reduces the cognitive resources available for job search, and therefore has a negative impact on the probability of exiting unemployment. This is an intuitive, yet neglected, consideration, whose consequences are at the heart of our analysis. In the sequel, we mention alternative "structural models" compatible with the same theoretical framework.

Related Literature

As we mentioned, in our model, when UB are low, an increase in its level can decrease the duration in unemployment. For higher values of the UB, we re-encounter the standard effect, i.e that increasing the level of UB increases duration. Several studies in the literature show that increments in the level of the UB increase duration in unemployment (See Tatsiramos and van Ours, 2014 for a survey). Nevertheless, none of these studies focuses on modifications of the UB for levels that are below or very close to the subsistence requirements. We found two papers which analyze the impact of UB in a low-income sample. LaLumia (2013) estimates a hazard model for a sample of people eligible to the earned income tax credit (EITC) in the United States. She finds that the effect of UB is never significant for women, and for men it is significant and positive in some of her specifications. Kupets (2006), develops a duration analysis for Ukraine. She finds that the receipt of UB does not have a significant effect on duration for agents who carry out subsistence activities. We will comment in more detail these papers in section 4.1.

In our model, when UB are low, providing some liquidity to the agents can actually increase their job finding probability. For higher values of UB, we re-encounter the standard effect, i.e that providing liquidity or cash transfers to agents increase their duration in unemployment. In fact, several studies (Card et al., 2007, Chetty, 2008, Basten et al., 2014) report that the probability of finding a job decreases when cash-constrained agents receive cash transfers (severance payments or annuities of any kind). On the other hand, several recent studies show that cash transfers to people who live in poverty (conditional cash transfer (CCT), usually conditional on family structure, and/or maintaining kids on school, or unconditional cash transfers (UCT)) do not have a negative effect on employment outcomes or may even have positive ones (Banerjee et al., 2017, analyzes seven CCT and UCT, Barrientos and Villa, 2015

[4]There is a literature about the lack of plausibility of private unemployment insurance, see for instance Easley et al. (1985), or more recently Hendren (2017).

analyzes a CCT in Colombia,[5] Franklin, forthcoming, analyzes a short-time subsidy for unemployed people in Ethiopia, moreover Baird et al., 2018 surveys a number of papers that analyze the effect of cash transfers on adult labor outcomes in low and middle income countries). LaLumia (2013) finds that the receipt of EITC refunds on men doesn't significantly affect their duration in unemployment (but it increases the expected duration in unemployment for women). We will comment in more detail the effect that liquidity has on the probability of finding a job in section 4.2.

Our setup is formally similar to a framework in which job search requires effort and a *flow* expenditure of money. The framework in which job search requires both money and effort (or time) has been largely ignored by the literature, with some exceptions, namely: Barron and Mellow (1979), Tannery (1983) and Schwartz (2015). The two first papers assume that search requires *time* and money. Barron and Mellow (1979) does not assume any complementarity between time and money. Tannery (1983) criticizes that assumption but does not develop a theoretical analysis. Schwartz (2015) assumes that looking for a job requires effort and money. He assumes that job search can be influenced through search capital, which requires monetary expenditures to be maintained; in his framework, the monetary expenditure is *not* a flow per period; he develops a theoretical analysis for a simple two period setting, and he produces a numerical analysis.

Some papers consider that job search requires *only* monetary expenditures, namely: Ben-Horim and Zuckerman (1987), Decreuse (2002), Mazur (2016). These papers, as ours, highlight the positive effect that UB *can have* on the duration in unemployment. Nevertheless, if job search only requires money, the cost of search is a decreasing function of cash-on-hand. In this specification providing liquidity to the agents *always*[6] increases the probability of finding a job, which is at odds with empirical evidence which finds that cash transfers increase duration (Chetty, 2008, Card et al., 2007, Basten et al., 2014), and with empirical evidence that shows that richer agents experience longer unemployment spells (Algan et al., 2003, Lentz and Tranaes, 2005, Lentz, 2009 and Centeno and Novo, 2014).

Finally, the literature about the design of UB has always put forward the trade-off caused by it. The standard view is that the role of UB is to smooth consumption, the price being a distortion of incentives. See among many others Frederiksson and Holmlund (2006), Tatsiramos and van Ours (2014), Spinnewijn (2015), Schmieder and Watcher (2016). Our model suggests that for some low values of UB, this trade-off may not be present: increasing the level of this benefit increases the possibilities of the agent to smooth consumption and *also* increases her probability of finding a job.

[5]These CCT or UCT usually last for long periods of time, and do not change with the income level, Banerjee et al., 2017 state: "Once a household becomes eligible for any of the programs that we study, the amount of benefit that one receives is the same regardless of actual income level and lasts at least a period between 2 and 9 years, depending on the program. This differs from many U.S. transfer programs (e.g. EITC, SNAP), where the stipend depends (either positively or negatively) on family income, and is updated frequently"

[6]The effect of providing liquidity to the agent, regardless of the employment status, is in principle ambiguous. Nevertheless, one can show that for a utility function that exhibits constant relative risk aversion (CRRA), providing liquidity to the agent increases job search effort and therefore decreases the expected duration in unemployment. If the utility function exhibits constant absolute risk aversion (CARA), providing liquidity to the agent has no effect on job search effort. These results are available from the authors upon request.

This implies that for low levels of UB there is no behavioral cost. There could instead be a behavioral gain. At the optimal level of UI, there is obviously a trade-off between insurance and incentives. It is however unclear whether the optimal level of UI is higher when the subsistence constraint is taken into account because the introduction of the subsistence activity creates an opportunity of self insurance against the loss in income induced by unemployment.

Some papers have looked at the design of unemployment insurance when jobless people can have access to informal jobs. Alvarez-Parra and Sanchez (2009) study the optimal time profile of UB when job-search effort and in-work effort in the hidden labor market are private information and perfect substitutes. A key result of their paper is that at the start of the spell the optimal level of UB should be generous enough to deter participation to the hidden economy. Espino and Sanchez (2015) address the same question under the assumption that the optimal profile of UB should prevent informal employment. In contrast, the positive analysis of our paper encompasses cases where the level of UB is too low to guarantee survival so that a subsistence activity (be it an informal job or a daily life activity) is needed. When we turn to the normative analysis we consider a flat benefit (with or without finite entitlement) and we also consider a range of environments (e.g. with access to borrowing) that those papers ignore. Gonzalez-Rozada and Ruffo (2016) extend Shimer and Werning (2007) to the case where all insured unemployed have an additional exogenous source of untaxed income. They also develop a sufficient statistics approach. Long and Polito (2017) look at the time profile of UB when the marginal cost of job search is higher if the unemployed works informally. In their setting, participation to the informal market is a binary choice that can be monitored without error by the Unemployment Insurance (UI) agency. An unemployed caught working informally is sanctioned with a given probability. We do not follow this route for several reasons. First, for us the subsistence activity is not necessarily violating the rules of the UI agency. Second, observing those activities is costly and can lead to errors. Finally, many countries outside the OECD lack institutions able to implement such a monitoring of the behavior of jobless people. Some other papers adopt a Mortensen-Pissarides framework in the presence of an informal sector and look at the impact of the introduction of UI on equilibrium unemployment and the share of formal, informal wage employment and self employment (see e.g. Margolis et al., 2014, Bosch and Esteban-Pretel, 2015 and Charlot et al., 2016).

The paper is organized as follows: In section 2 we start by presenting two standard results of the literature. Then we introduce our baseline model and do comparative statics. We further introduce three extensions, and comment the differences and similarities between our baseline model and a model in which job search requires both search and monetary expenditures. In section 3, we solve the planner's problem and find the Baily-Chetty formula (Baily, 1978 and Chetty, 2006). We also discuss the conditions that would allow to write the gain of insurance in terms of sufficient statistics. In section 4 we solve the baseline model and its extensions numerically. We show that when UB are low our model questions the two standard properties with which we started the paper and we discuss some empirical results found in the literature consistent with these findings. Finally, we analyze how the subsistence consumption level and the "technology" of the subsistence activity affect the optimal level of UB.

2 Positive Analysis

In this section we start by presenting two standard results of the literature: (1) A higher level of UB increases the expected duration unemployment; (2) Providing liquidity to the agent increases the expected duration in unemployment. Then, we analyze the behavior of the unemployed in our baseline model, which incorporates subsistence requirements and a subsistence activity. Next we introduce three extensions to our baseline model: Finite entitlement to a flat UB, the presence of incomplete financial markets and stochastic wage offers. Finally we point out the similarities and differences between our baseline model and a model in which finding a job requires both job search effort and flow monetary expenditures.

2.1 Standard Job Search Model [SM]

The "standard model" [SM] is a partial equilibrium job search model in a stationary discrete-time setting. Infinitely-lived, homogeneous and hand-to-mouth unemployed workers choose their search effort intensity, $s \in \mathbb{R}_+$. The instantaneous utility is separable in consumption and search effort. $\lambda(s)$ denotes the cost of job search effort and it is assumed that $\lambda(0) = 0$, $\lambda_s > 0$, $\lambda_{ss} \geq 0$.[7] Unemployed workers are entitled to a flat unemployment benefit, b, with no time limit. Hence, there's no room for an "entitlement effect" (Mortensen, 1977). In each period the consumption of the unemployed agent, c^u, is equal to b. It is further assumed that the agent is risk averse, implying that her utility function is increasing and concave in consumption $c \in \mathbb{R}_+$: $u_c(c) > 0$, $u_{cc}(c) < 0$. In each period job offers arrive with a probability $P(s)$ and it is assumed that $P(0) = 0$, $P_s > 0$, $P_{ss} \leq 0$. The net wage associated to a job offer is equal to $w - \tau$, where w is the gross wage, and τ is the level of taxes needed to finance the UB scheme; the consumption when employed, c^e, is equal to $w - \tau$.[8] The disutility of the in-work effort is normalized to zero and it is assumed that the employed agent loses her job with an exogenous probability ϕ.

The agent discounts the future at a rate $\beta = \frac{1}{1+r}$ where r is the interest rate. The timing is as follows: the unemployed chooses s in the current period, if she receives an offer, she starts working in the *next* period.

In the "Standard Model" [SM], the lifetime value V^U in unemployment (respectively V^E in employment) verifies the following Bellman equation:

$$[SM] = \begin{cases} V^U = \max\limits_{s} \quad u(c^u) - \lambda(s) + \beta[P(s)V^E + (1 - P(s))V^U] \\ V^E = u(c^e) + \beta[\phi V^U + (1 - \phi)V^E] \end{cases} \tag{1}$$

where $u(c^u) \equiv u(b)$, $u(c^e) \equiv u(w - \tau)$.

Subject to: $V^E - V^U \geq 0$, $s \geq 0$.

[7] For any function $f(x, y)$, f_x designates the first-order partial derivative and f_{xy} the second-order one.

[8] As in Chetty (2008) or Hopenhayn and Nicolini (1997), we consider a degenerate distribution of wage offers. Moreover, as it is standard, the wage is the only feature that characterizes the job.

We recall two well-known properties of an interior solution to Problem [SM]:

(1) Increasing b increases D, the expected duration in unemployment, where $D = \sum_{t=0}^{\infty}(1-P)^t = \frac{1}{P}$.

(2) Providing liquidity to the agent increases the duration in unemployment. This was pointed out by Chetty (2008).

To analyze the effect of liquidity, Chetty (2008) introduces an annuity A in a set-up essentially equal to the [SM] just presented. This annuity is a lump-sum income (independent from the UB scheme) received by the agent regardless of her employment status, so that $c^u = b + A$ and $c^e = w - \tau + A$. In Chetty's model, providing liquidity to the agent always has a negative effect on the probability of finding a job, and therefore it unambiguously increases expected duration in unemployment.

2.2 Baseline Model [BM]

Our baseline model, [BM], incorporates four differences into the standard model [SM]. First, the agent has a subsistence requirement $c_{min} \geq 0$, which means that her total consumption in each period has to be greater than or equal to c_{min}. To the best of our knowledge, a requirement $c_{min} > 0$ is never taken into account in the literature about UB. Second, we assume that the unemployed agent can carry out a subsistence activity by exerting effort $a \in \mathbb{R}_+$. This activity (looking for discounts in shops, fixing old clothes, selling home-made food, subsistence farming and the like) is even needed if $b < c_{min}$. Third, we assume that effort a can (*but need not*) be costly, meaning that a is now an argument of the cost $\lambda(\cdot)$ with $\lambda_a \geq 0$ and $\lambda_{aa} \geq 0$; we also assume that the marginal cost of job-search effort cannot strictly decrease when more effort is devoted to guarantee subsistence: $\lambda_{sa} \geq 0$. Fourth, the job finding probability P is a function of s and a. Following the scarcity literature (Shah et al., 2012 , Mullainathan and Shafir, 2013, Mani et al., 2013, Shah et al., 2015, and Schilbach et al., 2016) we assume that cognitive capacity is limited. Dealing with subsistence, which is a pressing activity, taxes this cognitive capacity, meaning that less cognitive capacity is left for job search. Formally, the effort devoted to the subsistence activity has a negative effect on the job finding probability: for the same level of job search effort, the job finding probability is lower the higher the quantity of effort devoted to the subsistence activity, i.e, $P_a < 0$ with in addition $P_{aa} \leq 0$. Furthermore, the marginal effect of job-search on the exit probability cannot strictly increase when more effort is devoted to guarantee subsistence: $P_{as} \leq 0$.[9]

We assume a Stone-Geary relationship between consumption and the level of utility: $u(c - c_{min})$. The consumption level when unemployed becomes $c^u = b + g(a)$, where $g(a)$ is the subsistence activity, with: $g(0) = 0$, $g_a > 0$, $g_{aa} \leq 0$. We further assume that $g(a) \equiv 0$ when the agent is employed, meaning that the agent does not carry out the subsistence activity when employed.[10]

[9] van den Berg and van der Klaauw (2006) consider a model with two job search search channels (formal and informal). Contrary to our setting, in their paper the two channels act independently in the following sense: one leads to a formal job and the other one to an informal job.

[10] Otherwise devoting effort to the subsistence activity would have negative effects on the productivity

All along the paper, in accordance with Alvarez-Parra and Sanchez (2009) and contrary to Long and Polito (2017), we assume that a and s are not observable by the UI agency. Therefore there are no fines nor punishments associated to $g(a)$ or to the lack of s.[11]

The Bellman equations of the the unemployed, and employed agent in the "Baseline Model" [BM] are defined as:

$$[BM] = \begin{cases} V^U = \max\limits_{s,a} \quad u(c^u) - \lambda(s,a) + \beta[P(s,a)V^E + (1 - P(s,a))V^U] \\ V^E = u(c^e) + \beta[\phi V^U + (1-\phi)V^E] \end{cases} \tag{2}$$

where $u(c^u) \equiv u(b + g(a) - c_{min})$, $u(c^e) \equiv u(w - \tau - c_{min})$, $\lambda_a \geq 0, \lambda_{aa} \geq 0, \lambda_{as} \geq 0$, $P_a < 0$, $P_{aa} \leq 0$, $P_{as} \leq 0$, $P_s > 0, P_{ss} \leq 0$, $P(0,a) = 0$.

Subject to: $b + g(a) \geq c_{min}$, $w - \tau \geq c_{min}$, $V^E - V^U \geq 0$, $a \geq 0$ and $s \geq 0$.

Our specification is motivated by findings from the scarcity literature, from which we extract four stylized facts: (1) Scarcity captures the mind automatically:[12] in our model if $b < c_{min}$ the agent *must* devote some effort (and therefore, cognitive resources) to subsistence, and in that sense, scarcity captures the mind automatically. (2) Scarcity makes us better at solving problems related with scarcity (*focus* effect):[13] in our model by devoting effort to the subsistence activity the agent is able to increase her consumption.[14] (3) Scarcity leaves less bandwidth (less attention or cognitive resources) to other aspects of our life (*tunnel* effect):[15] in our model devoting effort to subsistence leaves less cognitive resources available for job search, and therefore affects P negatively: $P_a < 0$ and $P_{as} \leq 0$. (4) None of these characteristics are personal traits: *any* person faced with scarcity would act in this way:[16] we model homogeneous agents, we do not claim that just one type (namely "agents with intrinsic characteristics that predict poverty") behave in this way.

Note that even when we interpret a and s as effort devoted to the subsistence activity

of the employed agent, and this should also be analyzed. In such a setup, the probability of losing the job, ϕ, would be a function of a. Given our focus on the problem of the unemployed, such an analysis is beyond the scope of this paper.

[11] On the difficulty of observing job search effort without errors, see for instance Cockx et al. (2018).

[12] "Scarcity captures our mind automatically. And when it does, we do not make trade-offs using a careful cost-benefit calculus. We tunnel on managing scarcity both to our benefit and to our detriment"), pg. 34-35 Mullainathan and Shafir (2013).

[13] "The very lack of available resources makes each expense more insistent and more pressing. A trip to the grocery store looms larger, and this month's rent constantly seizes our attention. Because these problems feel bigger and capture our attention, we engage more deeply in solving them. This is our theory's core mechanism: Having less elicits greater focus." Shah et al. (2012)

[14] One could also capture this effect by having that $g(a,b)$ with $g_a > 0$ and $g_b < 0$, that is, the smaller the b the higher is the ability of the agent to transform effort into consumption. Having $g(a,b)$ instead of $g(a)$ reinforces our findings. The development is available from the authors upon request.

[15] "Focusing on something that matters to you makes you less able to think about other things you care about. Psychologists call this *goal inhibition*. Goal inhibition is the mechanism underlying tunneling.", pg.31 Mullainathan and Shafir (2013).

[16] "Being poor means coping not just with a shortfall of money, but also with a concurrent shortfall of cognitive resources. The poor, in this view, are less capable not because of inherent traits, but because the very context of poverty imposes load and impedes cognitive capacity. The findings, in other words, are not about poor people, but about any people who find themselves poor." Mani et al. (2013).

and to job search, respectively, they could also be interpreted as *time* devoted to these activities. In a framework with time, the agent enjoys consumption and leisure. If one assumes that her utility function is separable in these two arguments and that time is not a binding constraint,[17] then such a framework could be encompassed by the baseline model [BM] where $\lambda = \lambda(a+s)$ is strictly increasing and convex, and $P_a = P_{aa} = 0$.

Comparative Statics in the Baseline Model The first order conditions of this maximization program, if the solution is interior, are:[18]

$$G_a \equiv u_c(c^u)g_a - \lambda_a + \beta P_a[V^E - V^U] = 0 \tag{3}$$
$$G_s \equiv -\lambda_s + \beta P_s[V^E - V^U] = 0 \tag{4}$$

where $V^E - V^U = \frac{u(c^e)-u(c^u)+\lambda(s,a)}{1-\beta[1-P(s,a)-\phi]}$.

We are particularly interested in the reaction of the agent when b changes, i.e, in $\frac{da}{db}$ and in $\frac{ds}{db}$. In general, an increment in b induces ambiguous effects on s and on a, which implies that the standard property of the literature $\frac{dP}{db} < 0$ is not *necessarily* met. In what comes, we discuss the condition under which the quantity of effort devoted to the subsistence activity decreases when b increases, $\frac{da}{db} < 0$, and we comment on the fact that the quantity on effort devoted to job search when b increases almost always decreases, $\frac{ds}{db} < 0$.[19]

The marginal effect of the UB level on attention devoted to job search The following expression summarizes the necessary and sufficient conditions under which an increase in b causes a reduction in the effort devoted to the subsistence activity, a, i.e, such that $da/db < 0$:[20] (see Appendix A.1 for the general formula)

$$\underbrace{-u_{cc}(c^u)g_a > \beta \frac{\partial(V^E - V^U)}{\partial b}}_{\textit{necessary condition}} \underbrace{(P_a - P_s(\frac{\lambda_{as}}{\lambda_{ss}} + \frac{P_{as}}{P_{ss}}))}_{\textit{sufficient condition}} \tag{5}$$

[17] Several studies highlight that unemployed agents do not devote more than a few hours per week (or even less) to look for a job. For instance, Krueger and Muller (2010) report that the average unemployed person searches 4 minutes a day in Nordic countries, 10 minutes in the rest of Europe and 30 minutes in North America (see also Manning, 2011 for a synthesis of five studies, and more recently Aguiar et al., 2013). Accordingly, jobless people have plenty of time left and hence we do not assume that time is a binding constraint for the unemployed.

[18] Corner solutions are discussed in Appendix A.1.

[19] Here, we consider the marginal effect of b keeping τ constant. In the numerical analysis we adjust τ so as to compensate the increment in b.

[20] If $\lambda_{ss} = 0$, $\frac{1}{\lambda_{ss}}$ must be replaced by $\frac{-P_s}{\lambda_s P_{ss}}$ in the inequality (5). If $P_{ss} = 0$, $\frac{P_s}{P_{ss}}$ must be replaced by $\frac{-\lambda_s}{\lambda_{ss}}$ in the inequality (5), see Appendix A.1 for the details.

When b increases, two different forces affect a. Consider first the left hand side (LHS) of the inequality: it tells us that when b increases the marginal utility gain of effort devoted to the subsistence activity is smaller. This is because the marginal utility of consumption is decreasing (concave utility). This effect goes in the direction of reducing a. We call this an *income effect*: having additional money ($db > 0$), reduces the marginal utility of further consumption.

Consider now the right hand side (RHS) of the inequality: $\beta \frac{\partial (V^E - V^U)}{\partial b} < 0$ implies that an increment in b distorts the relative value of being employed vs. being unemployed.[21] This affects a through two channels, a direct one, $P_a < 0$, and an indirect one through the effect of the change in b on s, $-P_s(\frac{\lambda_{as}}{\lambda_{ss}} + \frac{P_{as}}{P_{ss}}) \leq 0$. The direct channel: since employment is less attractive, the negative effect that a has on P is marginally less detrimental for the utility of the agent. The indirect channel: An increase in b has a negative direct impact on s (The partial derivative of the FOC of s with respect to b, G_{sb}, is negative; see in Appendix A.1), given the interactions between s and a ($\lambda_{as} \geq 0$, $P_{as} \leq 0$) this affects the optimal level of a. On the one hand, given the reduction of s, the marginal cost of a becomes smaller. On the other hand, given the reduction in s, a is now marginally less detrimental to $P(s,a)$. Both the direct and the indirect effects go in the direction of increasing a. We call this a *substitution effect*: increasing b distorts the relative value of being employed vs. being unemployed. In the numerical exercise of section 4 we find, for a broad set of parameters, that the income effect always dominates the substitution effect, i.e, $\frac{da}{db} \leq 0$.

The marginal effect of the UB level on search effort The total expression for $\frac{ds}{db}$ is equation (29) in Appendix A.1. All forces in that equation, except one, push it to be negative. The only force against is due to the interaction between a and s. When $\frac{da}{db} < 0$, the quantity of effort devoted to the subsistence activity decreases with b. If in addition $P_{as} < 0$ and $\lambda_{as} > 0$, these two effects push s upwards. This is only possible, of course, when $\frac{da}{db} < 0$. Nevertheless, in the numerical exercise for the baseline model [BM], this effect is never big enough to compensate for the fact that a higher b makes employment less attractive as compared with unemployment.

2.3 Extensions to the Baseline Model [BM] and Monetary Cost of Job Search [MC]

In this section we introduce three extensions to the baseline model [BM] in which we abandon the stylized stationary setup we had so far. The aim of these extensions is to allow for a more realistic framework. In all the extensions time is finite and the agent lives for T periods (from period 0 to period $T-1$). In the fist extension we assume that the agent is entitled to the UB for $B < T$ periods, we call it "model with finite entitlement" [FE]. In the second one, we allow for the presence of incomplete financial markets: the agent starts her life with an exogenous level of assets, she can save and get indebted up to a certain limit L, and she has to repay her debt at the end of period $T-1$, we call it "model with incomplete financial markets" [FM]. In the

[21] This effect is of course reinforced if we consider that financing a higher b requires higher taxes, and thus the net wage $w - \tau$ is smaller.

third one, we assume a sequential search model when there is a distribution of wage offers and no recall (McCall, 1970): when the agent receives an offer she has to decide whether to accept it or to reject it. We call this model "stochastic wage offers" [SWO]. In Appendix A.1.2 we develop the three theoretical frameworks, and in section 4 we solve them numerically.

Moreover, our baseline model [BM] is formally similar to a model in which looking for a job requires job search effort and monetary expenditures (model [MC]). In fact, both models would be equivalent if (1) $c_{min} = 0$, (2) $g(a)$ is replaced by $-m$, the monetary expenditure, with $P(s,a)$ replaced by $P(s,m)$ where now $P_m > 0$, i.e spending money in job search increases the probability of finding a job and if (3) $\lambda(a,s)$ is replaced by $\lambda(s)$ for all levels of a, that is, if there's no direct cost of the effort devoted to the subsistence activity. In Appendix A.1.2 we develop this setting theoretically and in section 4 we solve it numerically.

3 Optimal Unemployment Insurance

3.1 The Planner's Problem

We consider here the baseline model [BM], a setting with a hand-to-mouth and infinitely lived agent. The optimal level of the flat benefit b maximizes the lifetime utility of the unemployed subject to a budget-balanced condition for the Government (that is, the agent covers all the expected costs of the UB scheme).[22]

To construct the budget-balanced condition we transpose the approach of Shimer and Werning (2007) to a discrete time setup. The idea is that the net actualized cost of the job seeker should be null. Let C^U be the net actualized cost of the UB scheme for a job seeker, and C^E be the net actualized cost of a wage earner written in a recursive way. For simplicity, we write P instead of $P(s,a)$:

$$C^U = b + \beta[P\,C^E + (1-P)C^U] \tag{6}$$
$$C^E = -\tau + \beta[\phi\,C^U + (1-\phi)C^E] \tag{7}$$

The net actualized cost of the job seeker should be zero. Then, $C^E = \frac{-\tau}{1-\beta(1-\phi)}$. Plugging this last expression and $C^U = 0$ in (6), gives us:

$$\frac{b}{\beta P} = \frac{\tau}{1-\beta(1-\phi)}$$

The expected duration of *one episode* of unemployment is equal to $D = \sum_{t=0}^{\infty}(1-P)^t = \frac{1}{P}$.

[22] As is standard in the literature and contrary to Lawson (2017), we do not consider the financing of non-UI spending.

Considering this, τ can be written as:[23]

$$\tau = \frac{1-\beta(1-\phi)}{\beta} b\, D \tag{8}$$

We are now ready to compute the optimal level of b, i.e, the one that maximizes V^U subject to (8).

$$\max_b V^U = \quad u(c^u) - \lambda(s,a) + \beta[PV^E + (1-P)V^U] \tag{9}$$

The problem is stationary, therefore, V^U can be written as:

$$V^U = \frac{1-\beta(1-\phi)}{(1-\beta)(1-\beta+\beta\phi+\beta P)}\left(u(c^u) + \frac{\beta P}{1-\beta(1-\phi)}u(c^e) - \lambda(s,a)\right)$$

We need to look only at the direct impact of a change of b, because the envelope conditions eliminate the first-order effects of the behavioral responses (Chetty, 2006). Deriving the previous expression with respect to b gives:

$$\frac{dV^U}{db} = \quad \frac{1-\beta(1-\phi)}{(1-\beta)(1-\beta+\beta\phi+\beta P)}\left(u'(c^u) - \frac{\beta P}{1-\beta(1-\phi)}u'(c^e)\frac{d\tau}{db}\right) \tag{10}$$

Take $\frac{dV^U}{db} = 0$, and note from (8) that $\frac{d\tau}{db} = \frac{1-\beta(1-\phi)}{\beta}\left(\frac{-1}{P^2}\frac{dP}{db}b + \frac{1}{P}\right)$. Plugging this in (10) and simplifying gives:

$$0 = u'(c^u) - u'(c^e)\left(\frac{-1}{P}\frac{dP}{db}b + 1\right) \tag{11}$$

Note that the elasticity of duration with respect to b, i.e $\varepsilon_{D,b}$ is equal to $\frac{-b}{P}\frac{dP}{db}$. So, the optimal level of b verifies the following implicit equation:

$$\frac{u'(c^u) - u'(c^e)}{u'(c^e)} = \varepsilon_{D,b} \tag{12}$$

This is the Baily-Chetty formula (Baily, 1978 and Chetty, 2006). Its interpretation is the standard one, the LHS of the equation is equal to the marginal *gain* of b: consumption smoothing. The RHS, in turn, captures the moral hazard costs of benefit provision due to behavioral response; it is typically assumed that a higher b reduces the job search effort of the agent, causing her to remain longer in unemployment, this negative reaction to the distorted incentives is captured by the RHS.[24]

[23] This is the quantity of taxes that has to be paid during one episode of employment to cover the costs of one episode of unemployment. Job destruction, i.e, $\phi \neq 0$, means that there will be *several* employment and unemployment spells. Nevertheless, since time is infinite, this formula remains valid: the *total* expenditure in unemployment will be paid during the *total* time the agent is employed.

[24] Schmieder and von Watcher (2017) highlight that the RHS can be written as the behavioral cost of changing b divided by the mechanical cost of changing b, where the mechanical cost is defined as "by how much the policy change actually increases the transfer to the unemployed in the absence of

Appendix A.2.2 generalizes this analysis in a non-stationary setup. The resulting formula has only slight modifications, the most important being that, since $c_t \neq c_{t+1}$, then what is relevant is the *average* consumption when employed and when unemployed.

If the underlying model is the standard model [SM] -or a model like the one of Chetty (2008)-, the previous formula can be rewritten as:

$$\frac{\text{liquidity effect}}{\text{moral hazard effect}} = -bD(\text{liquidity effect} + \text{moral hazard effect}) \tag{13}$$

where liquidity effect $= \frac{\partial P}{\partial \text{A}}$ and moral hazard effect $-\frac{\partial P}{\partial w}$.

The decomposition of the LHS is put forward by Chetty (2008), the decomposition of RHS is evident since $\varepsilon_{D,b} = -bD\frac{dP}{db}$, and $\frac{dP}{db}$ = liquidity effect + moral hazard effect. Several comments are in order. First, from this expression it is very clear that *conditionally* on $\varepsilon_{D,b}$, the higher the liquidity effect, the higher the optimal level of b, and in this sense "if an agent chooses a longer duration primarily because he has more cash on hand (as opposed to distorted incentives), we infer that UI benefits bring the agent closer to the social optimum" Chetty (2008). Note, however, that unconditionally, a higher liquidity effect does not necessarily imply a higher optimal level of b, because the liquidity effect affects both sides of (13) in the same direction. Second, as Chetty, 2008 and Chetty, 2009 highlight, the "sufficient statistics" approach is very useful, but since all the inputs ($\varepsilon_{D,b}$, the moral hazard effect and the liquidity effect) are endogenous to the level of b, an empirical analysis that follows this sufficient approach applies only locally. Third, the "sufficient statistics" approach is less model dependent than other alternatives (structural estimation or numerical simulations), as Chetty (2008) claims. Nevertheless, it should be noticed that the LHS decomposition crucially depends on some modeling assumptions: (1) the probability of finding a job, P, cannot be affected by more than one variable: When b changes, all variables except for one, should remain constant; (2) The cost of search needs to be separable from consumption. If one of these two assumptions is not verified, it is no longer possible to re-write the LHS of the Baily-Chetty formula using sufficient statistics, i.e, as the ratio of the liquidity effect and the moral hazard effect. In our setting (baseline model [BM] and its extensions) these two conditions are not satisfied: devoting attention to job search has a cost that is not separable from consumption and the probability of finding a job is affected by two choice variables (P is a function of a and s), meaning that the decomposition in sufficient statistics is not possible (See Appendix A.2.1 for the proof).[25]

behavioral responses".

[25] Gerard and Gonzaga (2016) also report that the decomposition is not possible in their setting because, as we do, they consider several choice variables. If one is willing to assume that when b changes one of the two variables remains constant -as Chetty (2008) does when he incorporates the reservation wage (a second variable) in his setup- then the decomposition remains possible, if the variable that changes has a cost which is separable from consumption.

3.2 Interpretation and the role of c_{min} and $g(a)$

Starting from our baseline model [BM], the Baily-Chetty formula, can be written as:

$$\frac{u'(b+g(a)-c_{min})-u'(w-\tau-c_{min})}{u'(w-\tau-c_{min})} = \varepsilon_{D(a,s),b} \tag{14}$$

Even if the formula for the optimal b is the standard one, our baseline model [BM] incorporates two new elements with respect to the standard model [SM]: c_{min} and $g(a)$, which introduce changes both to the LHS and to the RHS of the equation. In the following paragraphs we study the impact of each of them separately.

The role of c_{min}: If we consider the standard model [SM], and we introduce a subsistence requirement, the LHS of (12) will be higher when preferences exhibit decreasing absolute risk aversion, which is a common assumption (See for instance Mas-Colell et al., 1995 p.193). Regarding the RHS, which can be written as: $\varepsilon_{D,b} = \frac{-b}{P}\frac{dP}{db} = \frac{b}{P}\frac{dP}{ds}(\frac{-ds}{db})$, one can show that in the presence of c_{min}, s is higher,[26] and thus $P(s)$ is higher, this causes the two first terms of this expression to be lower, but it is not clear whether $\frac{-ds}{db}$ is also lower in the presence of c_{min}, meaning that the effect over the RHS is ambiguous.[27]

The role of $g(a)$: If we take the standard model [SM] and (1) add the subsistence activity $g(a)$, (2) consider a specification for $P(s,a)$ such that if the agent devotes no effort to the subsistence activity, i.e $a = 0$, the function reduces to the same function of the standard model $P(s)$ (for example $E\, s^{\beta_1} e^{-\beta_2 a}$), then the optimal level of b will be *lower* in the resulting model as compared with the [SM], ceteris paribus. This is because the resulting model is more general, in the sense that the agent always has the option of devoting zero effort to the subsistence activity and by doing so to go back to the standard model [SM]. In a sense, the subsistence activity has a self-insurance role, because it allows to increase consumption when the agent is unemployed.[28]

4 Numerical Exercise

In this section we solve the optimization problem numerically. First, we show that the property of a hump-shaped $P(s,a)$ is present in the baseline model [BM]; it is robust to a wide number of parametrizations, and to the extensions introduced in section 2.3. Second, we show that in our baseline model [BM] and in its extensions, providing liquidity to the agent when the level of b is low, can increase the probability of finding a job, instead, when the level of b is high, we re-encounter the standard property, that is, providing liquidity to the agent decreases the probability of finding a job. Third, we analyze the effect of $g(a)$ and c_{min} on the optimal level of b.

[26] Consider the standard model [SM], The FOC is: $G_s \equiv -\lambda_s + \beta P_s(V^E - V^U) = 0$, and $\frac{ds}{dc_{min}} = -\frac{G_{s,c_{min}}}{G_{s,s}}$. We know that $G_{ss} < 0$, and $G_{s,c_{min}} = \frac{\beta P_s}{1-\beta[1-P(s)-\phi]}(-u'(c^e)+u'(c^u)) > 0$, therefore $\frac{ds}{dc_{min}} > 0$.

[27] Recall that the standard model with subsistence requirements, without any mechanism to cope with those subsistence requirements, is only defined for levels of $b > c_{min}$.

[28] In a setup with home production Taskin (2011) finds a similar result.

	Description	Functional Form	
$u(c^u)$	Utility Function	$\frac{c^{1-\sigma}}{1-\sigma}$	Chetty (2008)
$\lambda(s,a)$	Cost of Search effort	$e^{(\mu_1 s+\mu_2 a)}-1$	Cockx et al. (2018)
$g(a)$	Subsistence Production	$G\,a^{\gamma}$	Our choice
$P(s,a)$	Prob. of finding a job	$E\,s^{\beta_1}e^{-\beta_2 a}$	Our choice
		Parameters (baseline)	
ϕ	Job Destruction rate	0.00443	Shimer and Werning (2007)
r	Interest rate	0.001	Shimer and Werning (2007)
β	Discount rate	0.999	$1/1+r$
E	Coefficient in front of $P(s,a)$	0.2	
β_1	Exponent of s in $P(s,a)$	0.5	
β_2	Exponent of a in $P(s,a)$	0.5	
w	Wage	100	
c_{min}	Subsistence level	20	
σ	RRA	1.75	Chetty (2008)
μ_1	Parameter of s in $\lambda(s,a)$	0.3	
μ_2	Parameter of a in $\lambda(s,a)$	0.3	
G	Scale parameter of $g(a)$	22	
γ	Exponent if $g(a)$ is isoelastic	0.8	

Table 1: Functional Forms and Parameters

The benchmark parametrization takes the functions and parameters specified in Table 1. We take the time unit to be a week. The values of ϕ and r are taken from Shimer and Werning (2007). We assume a constant relative risk aversion (CRRA) utility function where σ (the RRA) is taken from Chetty (2008). Due to lack of evidence, it is hard to pinpoint the values for the other parameters. Nevertheless, the chosen parametrization applied to the baseline model [BM] gives, for the optimal level of b (which is $b = 0.62w$, i.e, a gross replacement rate (RR) of 0.62) an expected duration of one episode of unemployment equal to of 18.13 weeks, which is reasonable.[29] A sensitivity analysis for other 42 specifications is provided in Table 2.

4.1 Impact of b on the Duration in Unemployment

In this section we numerically solve the baseline model [BM], its extensions ([FE], [FM] and [SWO]) and the model with monetary costs of job search [MC], and we analyze the relationship between the level of b and the expected duration in unemployment. Solving the baseline model [BM] numerically we find that the relationship between P and the level of b is hump-shaped: when b is low enough, increasing it increases the probability of finding a job; instead, when b is big enough, increasing it, reduces the probability of finding a job. This property is robust to the presented extensions of the model. In this section we also comment some empirical results found in the literature.

[29] Chetty (2008) calibrates his model for the US to have an average unemployment duration of 15.8 weeks.

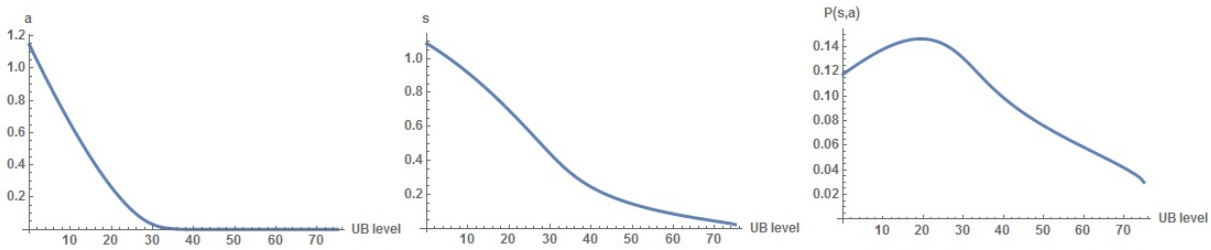

Figure 1: **Baseline Model [BM]**: The three graphs show the optimal level of a, s and $P(s,a)$ respectively, in the baseline model [BM] for different values of b. The functions and parameters are the ones presented in Table 1.

Baseline Model [BM]: In section 2.2 we showed that in the baseline model [BM] an increment in b has an ambiguous effect on P, the probability of finding a job, contrary to the standard job search model [SM], where increasing b unambiguously reduces P. Here, contrary to what was done in section 2.2, we analyze budget-balanced changes of b, that is, whenever b changes, τ changes accordingly; this implies that formula 5 in section 2.2 has one modification: the term $\frac{\partial(V^E - V^U)}{\partial b}$ has to be replaced with $\frac{d(V^E - V^U)}{db}$, i.e the partial derivative is replaced by a total derivative.

In the left panel of Fig. 1, when b is 0, the agent devotes a high effort a to the subsistence activity. When b increases, the *income effect* dominates the *substitution effect* (see section 2.2), meaning that the agent devotes less effort to subsistence. In the central panel of Fig. 1 the quantity of job search effort s monotonically decreases when b increases for all the range of levels of b. Finally, in the right panel of Fig. 1, $P(s,a)$ is hump-shaped. When the value of b is small enough, below 19 in this graph, an increase in b *increases* the probability of finding a job. In this range, the quantity of effort devoted to the subsistence activity strongly declines with b. This frees cognitive resources and allows the agent to be more concentrated on the job search process. This effect is big enough to compensates the reduction in the job search effort itself. From $b = 19$ onwards, this is no longer the case. Even if the quantity of effort devoted to the subsistence activity keeps on decreasing, this reduction is no longer enough to compensate the reduction in job search effort, causing $P(s,a)$ to decrease when b increases.

Changing the values of the parameters changes the levels of b for which $P(s,a)$ is maximal. Nevertheless, the *qualitative shape* of the graphs remains the same for a broad set of parameters. Table 2 reports the results for 42 different specifications. In this table, the 13 first columns show the values of the parameters, and the last four the results."argmax P", is the level of b for which $P(s,a)$ reaches the maximum (the equivalent to 19 in the previous graph). In all but two of the specifications of Table 2, when $c_{min} > 0$ the hump-shape of $P(s,a)$ is preserved. It is not preserved when β_2, the exponent of the isoelastic a in $P(s,a)$ is very low (equal to 0.1) and when G, the scale parameter of $g(a)$, is very high (equal to 70). In the first case, the negative slope of $P(s,a)$ for all values of b is explained because for any level of job search effort, the negative effect on the job finding probability of devoting effort to the subsistence activity is very small. So even if a always decreases (strictly for low values of b, weakly for high values of b) when b increases, this effect is dominated by $\frac{ds}{db} < 0$. In the second case, the agent has a very big capacity to self-insure, this implies that by devoting a small quantity of effort to the subsistence activity she is able to meet the subsistence require-

ments, and thus that the negative effects of this activity on the job finding probability are very limited and always dominated by $\frac{ds}{db} < 0$.

Even though there is a large evidence showing that duration increases when b increases, see Tatsiramos and van Ours (2014) for a survey, to the best of our knowledge none of the original studies this paper cites has looked at the effects of b when its level is "low", i.e below subsistence requirements. The closest one among those is Lalive et al. (2006), which analyzes the effect of a rise in UBs in Austria in 1989 of 4.6 percentage points, starting from a replacement rate of 41%, to people with *low* wages (below 12 610 ATS, the median was 16 400 ATS), who on top of the UB receive family allowances. They found using a diff-in-diff approach that the increment in the UB increased duration by 0.38 weeks (from 20.60 -treated- to 20.97 -control- weeks), which implies an elasticity of about 0.15.[30] The analyzed people are probably above the subsistence level, (because the pre-reform level of the UB is already substantial and because on top of that they have family allowances). Nevertheless, the effect of an increase of UB is very small. The rest of the studies, which do not consider low income people, have estimates which are higher, and range between 0.35 and 1.7.

LaLumia (2013) estimates a hazard model for a sample of people eligible to the earned income tax credit (EITC) in the United States. She has a sample of 5881 unemployment spells, 2173 men and 3708 women, by construction this is a low income sample. 23% of the unemployment spells in her sample involve the receipt of UB. On average, individuals in her sample are eligible for about $150 weekly UB measured in 2007 real dollars. She finds that the effect of UB on women is non significant in any specification. For men, in some of her specifications the effect of UB on the hazard rate is positive and significant, and in others it is not significant.

Kupets (2006) makes a duration analysis for Ukraine, using the Ukranian Longitudinal Monitoring Survey for the years 1998-2002. The level of UB is low, of around 25-28% of the official average wage. Only 4.6% of the sample reported UB to be their main source of support, 13.9% of the sample states that casual activities or subsistence farming constitute their main source of subsistence. She finds that: "The estimate of the variable on receipt of unemployment benefits fails to reject our hypothesis of insignificant effect of unemployment benefits on reemployment probability in the case of the total sample of unemployed. However, the effect of unemployment benefits is found to be significant and negative if we take only "standard" unemployed without any income from casual work". Moreover, she finds a negative effect of the presence of casual work on the finding rate probability, she states: "On the other hand, those usually unemployed persons who are occasionally engaged in unreported activities or subsistence farming tend to search for regular jobs less intensively and, therefore, they are less likely to receive a job offer."

Moreover, Morris and Wilson (2014) studies the impact of a reduction in the level of unemployment assistance "Newstart" in Australia ("The Newstart payment at AUD255.25 per week for a single person (March 2014) is well below the poverty line even when government rent assistance is included.") using a survey and in-depth interviews, they state: "Insufficient income contributed to stress, and it added to circumstances in which interviewees struggled to maintain their confidence in a job interview (if they even reached that point). Physical appearance particularly suffered; interviewees told

[30] In their sensitivity analysis they use a RDD and find that the effect is even smaller, of 0.31 weeks.

of how difficult it was to keep themselves groomed, appropriately attired and motivated".

All this suggests that the impact of b on the probability of finding a job may vary according to the actual level of the UB, and that if the level of UB is very low the effect of increasing it is not necessarily negative.

For the coming three extensions, unless stated otherwise, we use the functions and parameters specified on Table 1, with one exception: For simplicity (as Hopenhayn and Nicolini, 1997, Chetty, 2008, Shimer and Werning, 2008, Schmieder et al., 2012, Kolsrud et al., 2015, Kroft and Notowidigdo, 2016) we consider that employment is an absorbing state ($\phi = 0$). We take the time unit to be a week and we set $T = 200$ (from $t = 0$ to $t = 199$), as the total quantity of time.

Finite Entitlement [FE]: The model with finite entitlement considers the case in which the agent is entitled to a flat benefit b for a number of periods B strictly smaller than T. We solve this problem numerically, using the functions and parameters of Table 1, moreover, we set to $B = 100$ (from $t = 0$ to $t = 99$).[31] To show how the behavior of the agent changes when the end of entitlement is approaching, in Fig. 2 we report the optimal choice of the agent in several periods (period 0, 24, 74 and 99). As can be observed, the graph at the beginning of the unemployment spell (period 0) looks very similar to the graph for the case where we had stationarity (Fig.1), in particular the hump-shape of $P(s, a)$ is preserved. In period 99, the last period in which the agent receives b, $\frac{d(V^E_{t+1} - V^U_{t+1})}{db} = 0$ this causes s to have a weakly positive slope for all b (see equation (31) in the Appendix A.1.2).

Incomplete Financial Markets [FM]: The model with incomplete financial markets considers the case in which the agent starts her life with an exogenous level of assets k_0, and she can get indebted up to a certain binding limit L. We assume that she has to repay the debt at the end of the last period. We solve this problem numerically, using the functions and parameters of Table 1, moreover, we assume that the agent starts the unemployment spell with an exogenous level of assets $k_0 = 0$, and we allow her to get indebted up to 200, that is, up to two times the gross wage. In each period the agent chooses a_t and s_t, moreover, she also chooses the optimal level of assets for the next period, k_{t+1} from a grid of different values of assets that goes from -200 to 0. In previous simulations we had a grid of assets with positive values, to allow the agent to save. Nevertheless, the optimal k policy function of the agent never included savings. In Fig. 3, we report the optimal choices of a_t, s_t and the probability of finding a job $P(s_t, a_t)$ at the beginning of the unemployment spell. As Fig. 3 shows, the hump shape of the exit rate from unemployment is preserved in this context.

Stochastic Wage Offers [SWO]: The model with stochastic wage offers considers the case in which the distribution of offers is not degenerate and is known. If an offer is received, the agent follows a stopping rule: she accepts the job offer if the wage is

[31] Both B and b could be part of the optimal unemployment insurance design (see for instance Hopenhayn and Nicolini, 1997), nevertheless in this paper we look at the optimal level of b conditional on B, as Baily (1978), Chetty (2006) and Chetty (2008) do.

ϕ	r	β	E	β_1	β_2	w	c_{min}	σ	μ_1	μ_2	G	γ	argmax P	Gross RR*	Net RR*	c_u^*/c_e^*
0.00443	0.001	0.999	0.2	0.5	0.5	100	20	1.75	0.3	0.3	22	0.8	19	0.62	0.66	0.66
			0.4										19	0.65	0.67	0.67
			0.6										19	0.66	0.67	0.67
			0.8										19	0.66	0.67	0.67
			1										19	0.66	0.67	0.67
				0.1									31	0.8	0.83	0.83
				0.3									24	0.68	0.72	0.72
				0.7									18	0.59	0.62	0.62
				1									19	0.62	0.64	0.64
					0.1								0	0.62	0.66	0.66
					0.3								13	0.62	0.66	0.66
					0.7								22	0.62	0.66	0.66
					1								24	0.62	0.66	0.66
						50							16.5	0.69	0.72	0.73
						80							18.4	0.64	0.68	0.68
						130							19.5	0.6	0.64	0.64
						150							19.5	0.6	0.65	0.65
							0						0	0.57	0.61	0.61
							5						5	0.59	0.63	0.63
							10						10	0.6	0.64	0.64
							15						14	0.61	0.65	0.65
								0.5					33	0.55	0.55	0.58
								1					30	0.63	0.64	0.65
								1.5					24	0.63	0.65	0.65
								2					15	0.6	0.66	0.66
								2.5					10	0.53	0.68	0.68
									0.1				19	0.64	0.66	0.66
									0.5				19	0.61	0.66	0.66
									0.7				19	0.6	0.66	0.66
									0.9				19	0.59	0.65	0.65
										0.1			24	0.62	0.66	0.66
										0.5			18	0.62	0.66	0.66
										0.7			17	0.62	0.66	0.66
										0.9			17	0.62	0.66	0.66
											20		20	0.62	0.66	0.66
											30		16	0.62	0.66	0.66
											50		6	0.62	0.66	0.66
											70		0	0.62	0.66	0.66
												0.1	2	0.53	0.56	0.70
												0.2	5	0.57	0.60	0.69
												0.4	10	0.61	0.65	0.67
												0.6	15	0.62	0.66	0.66
												0.9	22	0.62	0.66	0.66

Table 2: Sensitivity Analysis for the Baseline Model [BM]: This table reports the results for 42 different specifications. The 13 first columns show the values of the parameters, and the last five the results."argmax P', is the level of b for which $P(s,a)$ reaches the maximum."Gross RR*" gives, for each specification, the optimal gross replacement rate: $\frac{b}{w}$, respectively "Net RR*", the optimal net replacement rate $\frac{b}{w-\tau}$. Finally, "c_u^*/c_e^*" gives the ratio of the consumption in unemployment $c_u^* = b+g(a)$ divided by the consumption in employment $c_e^* = w - \tau$, when b is the optimal one.

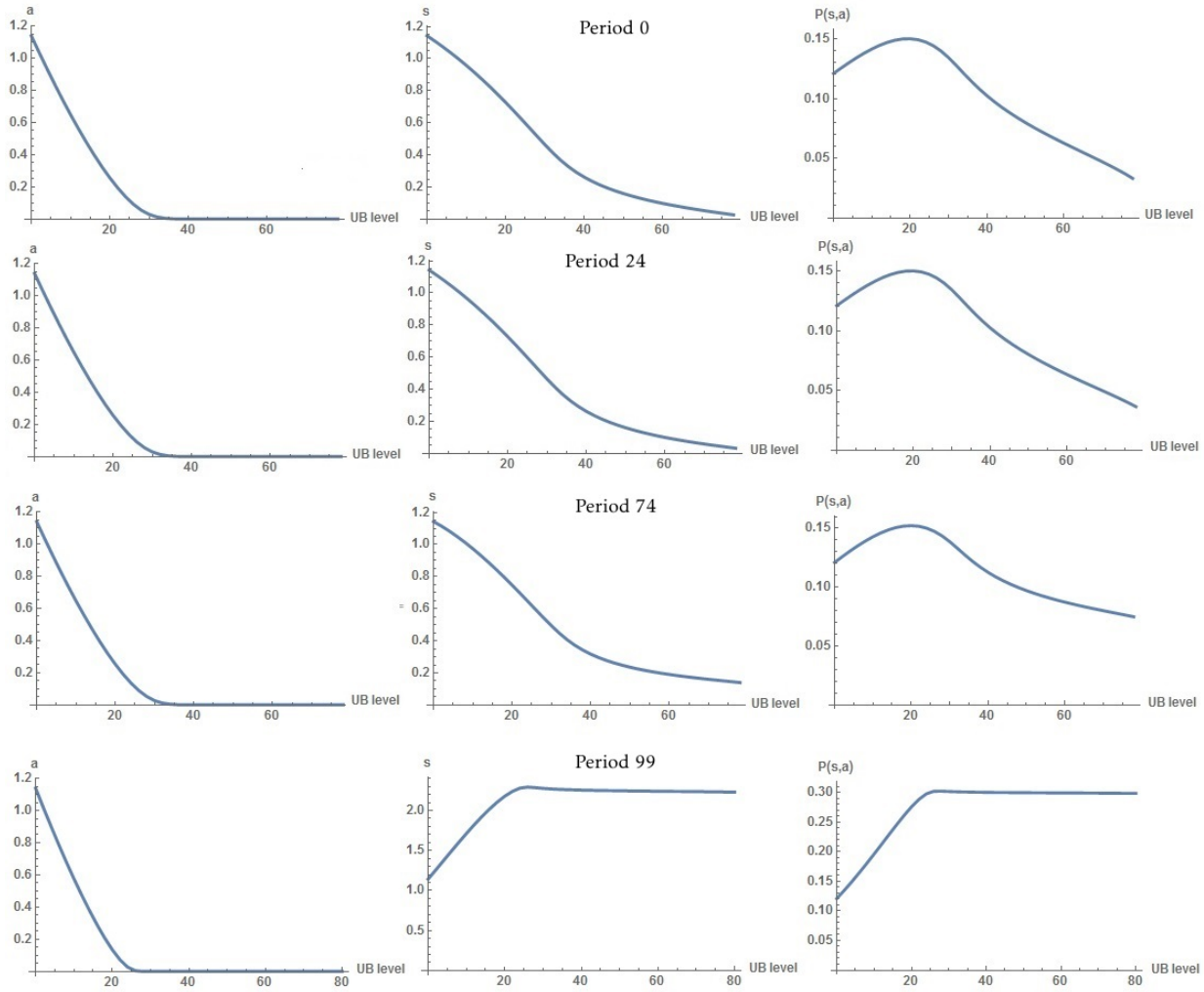

Figure 2: **Finite Entitlement [FE]**: Each column has three graphs that show the optimal level of a_t, s_t and $P(s_t, a_t)$ respectively, in the model finite entitlement [FE] for different values of b. We report in each line the results for period 0, 24, 74 and 99, respectively. The functions and parameters are the ones presented in Table 1, except for ϕ which is now equal to zero. We set $T = 200$, the total quantity of time, and $B = 100$, the number of periods in which the agent is entitled to the flat benefit b.

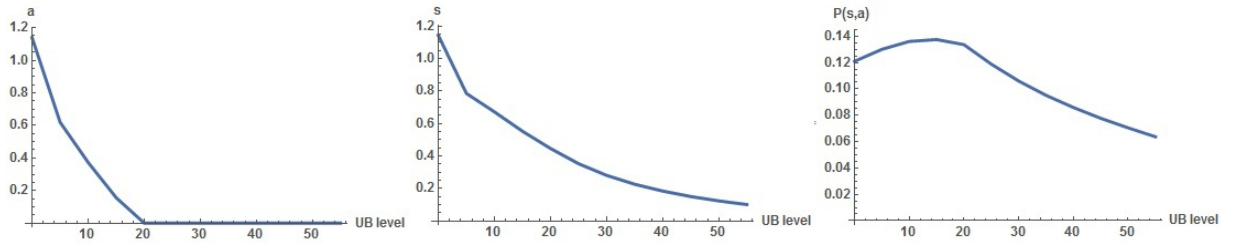

Figure 3: **Incomplete Financial Markets [FM]**: The three graphs show the optimal level of a_t, s_t and $P(s_t, a_t)$ respectively, at the beginning of the unemployment spell, in the model with incomplete financial markets [FM] for different values of b. The functions and parameters are the ones presented in Table 1, except for ϕ which is now equal to zero, moreover we allow the agent to get indebted up to 200 (two times the wage) and we assume that the agent has to repay her debt at the and of the $T = B = 200$ periods.

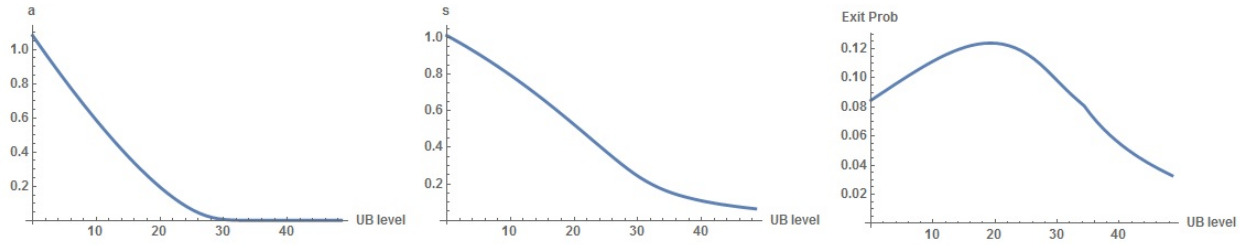

Figure 4: **Stochastic Wage Offers [SWO]**: The three graphs show the optimal level of a_t, s_t and $P(s_t, a_t)*(1-H(x_t))$ respectively, at the beginning of the unemployment spell, in the model with stochastic wage offers for different values of b. The functions and parameters are the ones presented in Table 1, except for ϕ which is now equal to zero, and $\sigma = 2$. We set $T = B = 200$, the total quantity of time. We assume that wages are Pareto distributed with parameters $w_{min} = 66.66$ and $\alpha = 3$.

above her reservation wage (an additional choice variable), otherwise she rejects it. We solve this problem numerically, using the functions and parameters of Table 1, moreover we assume that wages are Pareto distributed with minimum possible value $w_{min} = 66.66$ and shape parameter $\alpha = 3$, so that the average wage is equal to 100. We set the coefficient of relative risk aversion $\sigma = 2$ because an integer allows us to find a closed form expression for V_t^U, which simplifies the numerical analysis. In Fig. 4 we report the optimal choices of a_t, s_t and the exit probability out of unemployment $P(s_t, a_t) * (1 - H(x_t))$ at the beginning of the unemployment spell, where $H(x_t)$ is the cumulative distribution function of the Pareto distribution, evaluated at the optimal reservation wage x_t. As Fig. 4 shows, the hump shape of the exit probability out of unemployment is preserved when wage offers are stochastic.

Monetary Costs of Job search [MC]: Even without subsistence requirements, in a framework in which looking for a job requires effort and money, the relationship between b and the probability of finding a job can also be hump-shaped. To show this we solve this stationary problem numerically using the functions and parameters of Table 1, where now instead of a we have m: money devoted to job search and we change three things: (1) the probability of finding a job is now $P(s, m) = Es^{\beta_1}(m/10)^{\beta_2}$, which is a positive function of m; (2) Instead of $g(a)$ we have now $-m$[32] (note that the parameters G and γ are no longer needed) and finally (3) $c_{min} = 0$, that is, there are no subsistence requirements.

To have a hump-shaped $P(s, m)$, the monetary expenditure needs to have an important contribution to the job finding probability $P(s, m)$, that is β_2 cannot be negligible compared with β_1. In Fig. 5, $\beta_1 = \beta_2 = 0.5$, this is enough to generate the hump-shape. Nevertheless, if $\beta_2 = 0.2$, for instance, then we would not have the hump-shape any more, and $P(s, m)$ would always be decreasing with respect to b.

[32]There is very few data about how much money is spent in job search. One of the few estimates is the one of Stephenson (1976) who finds that white youth use 25% of their income to find work. Schwartz (2015) uses a baseline expenditure of 30% of the level of the UB.

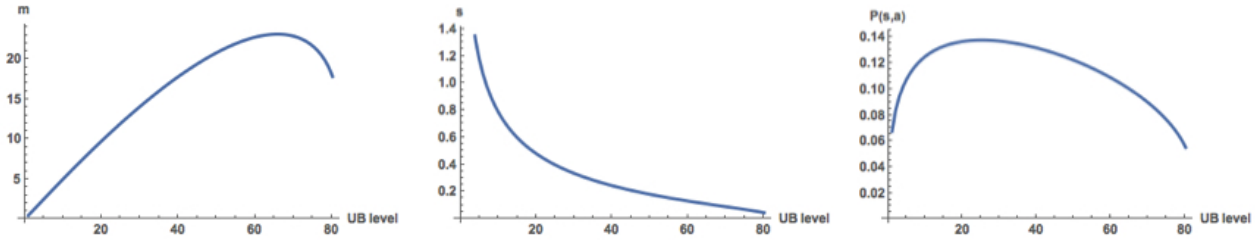

Figure 5: **Monetary Costs of Job Search [MC]**: The three graphs show the optimal level of m, s and $P(s,m)$ respectively, in the model with monetary costs of job search [MC] for different values of b. The functions and parameters are the ones presented in Table 1 with four changes: (1) the probability of finding a job is now $P(s,m) = Es^{\beta_1}(m/10)^{\beta_2}$, (2) Instead of $g(a)$ we have now $-m$, where m is the quantity of money spent in job search (3) $c_{min} = 0$ and finally (4) we set $\beta_1 = \beta_2 = 0.5$.

4.2 Liquidity Effect

Providing an annuity to the agent in each period, regardless of her employment status, increases the expected duration in unemployment in the standard model [SM]. In this section we question this property in the baseline model [BM], its extensions ([FE], [FM] and [SWO]) and the model with monetary costs of job search [MC] numerically. Additionally, we comment some empirical results found in the literature.

Let us start by analyzing the effect of an annuity in the baseline model [BM]. We analyze the effect of the annuity for each possible budget-balanced level of b. Consider Fig. 6, where all the functions and the parameters are the ones described in Table 1. In this graph we show which is the effect of providing liquidity to the agent. To do that we compare two cases: (1) the only income of the agent is b (the continuous line) and (2) on top of b the agent receives an annuity of 10 (the dashed line). Both curves intersect in a point close to $b = 15$. When b is above 15, providing liquidity to the unemployed decreases her expected probability of finding a job (the dashed line is below the continuous line). Nevertheless, when b is below 15, providing an annuity to the agent *increases* her probability of finding a job (the dashed line is above the continuous line). When b is low enough, subsistence is only guaranteed by a relatively high level of effort a. Then the introduction of the annuity reduces a to an extent that more than compensate the standard negative effect of an annuity on s. This is no more the case when b is under but sufficiently close to the subsistence level. Then the effort a needed to reach the threshold c_{min} is mild and the impact of introducing the annuity on a does no more outweigh its effect on s.

We now check whether the above numerical properties are robust in two senses. First, Fig. 6 has been derived for an annuity of 10. The qualitative properties of Fig. 6 hold true as long as the annuity is at most equal to 35% of the wage. When the annuity is above 35% of the gross wage, the annuity increases expected duration, even if b is low. In this case, we are back to the standard property found in previous papers quoted in the introduction.

Second, we check whether Fig. 6 remains valid for extensions of the model [BM]. We provide the numerical results for the extensions ([FE], [FM] and [SWO]) and for the model with monetary costs of job search [MC]. The parametrization for each model is the one used in the previous subsection, where the effect of b on the expected duration

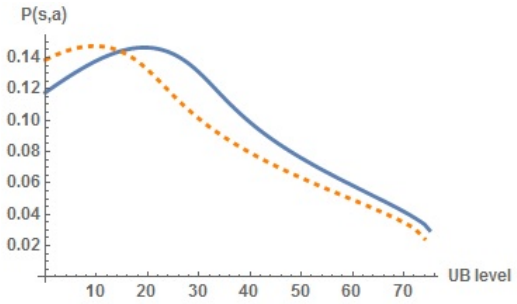

Figure 6: **Liquidity Effect [BM]**: This graph shows the optimal value of $P(s,a)$ for different values of b. The continuous line is generated with the functions and parameters showed in Table 1. The dashed line uses the same functions and parameters, the only difference being that the agent receives an annuity of 10 regardless of her employment status.

was analyzed. Fig. 7 shows the results. For the extensions to the baseline model [BM], the intuition is the same as before. For low levels of b subsistence is not guaranteed: providing money to the agent when b is low allows her to reduce the effort devoted to the subsistence activity and therefore to increase the cognitive resources devoted to job search. For the model with monetary costs [MC] the intuition is the following: when the level of b is very low, the marginal utility of consumption is very high, which causes that just a small amount of money is devoted to job search; the presence of the annuity relaxes this trade-off and allows the agent to devote more money to job search.

There is some recent evidence showing that when people are close to subsistence levels of consumption, providing money may help them to leave unemployment: Franklin (forthcoming) develops an experiment in Ethiopia where he gives money (intended to cover transportation costs) to young jobless people. He finds that four months after the start, people who received the subsidy were seven percentage points more likely to have a permanent work; the effect was stronger for relatively poor and cash constrained people. Barrientos and Villa (2015) find, using a regression discontinuity design, that a conditional anti-poverty cash transfer in Colombia (conditional on maintaining kids in school) [33] had positive effects on the level of employment of adult males. On the same line, Banerjee et al. (2017) analyze the effect of conditional and unconditional cash transfers to low income families of seven different programs in developing countries on work outside the household (which includes casual or permanent employment, and excludes any self-employed activity), after pooling the samples they do not find evidence of a negative effect, moreover, when treating each program separately in some cases they find a positive effect. This evidence is not in line with the [SM] or a model like the one of Chetty (2008) in which providing an annuity to the agent always has negative effects on the probability of finding a job.

4.3 The Optimal level of b

In section 3.2 we showed that the new elements of the baseline model [BM] (c_{min} and $g(a)$) have an ambiguous effect on the optimal level of b. In this section we first com-

[33] The program is called "Familias en Acción", "Familias en Accion was introduced in 2001 by the government of Colombia with the aim of strengthening human capital investment among children in poorest households in rural areas and small towns" Barrientos and Villa (2015).

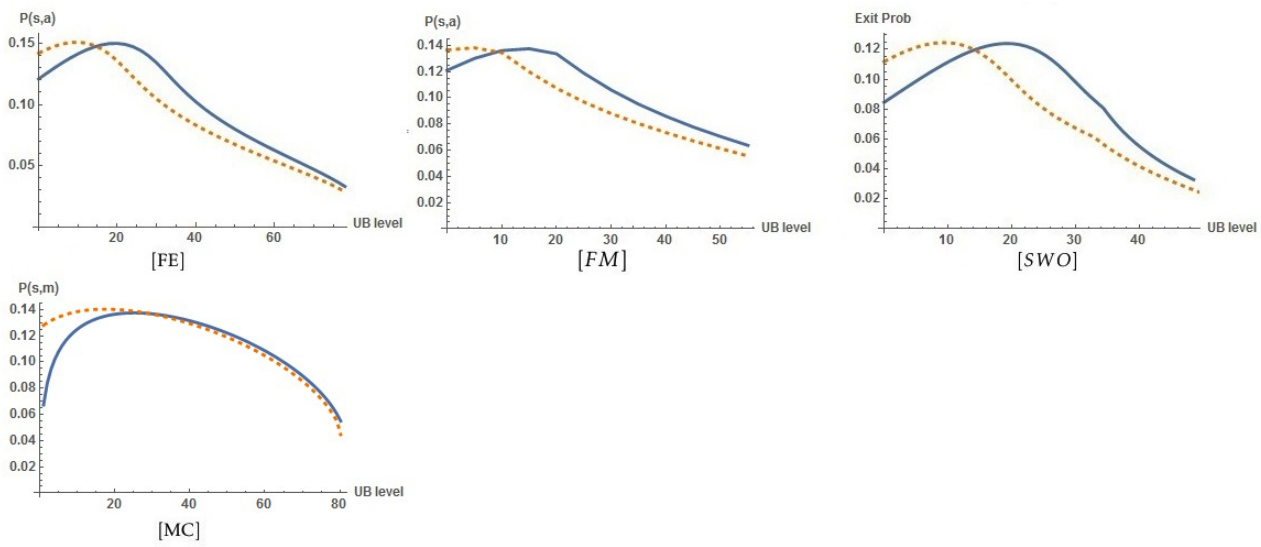

Figure 7: **Liquidity Effect**: These graphs show the optimal value of P for different values of b, for the extensions:[FE], [FM] and [SWO] (For [SWO] instead of reporting P, we report $P*(1-H(x))$ for the optimal x). We also include the results for the model with monetary costs [MC]. The continuous line is generated with the functions and parameters discussed in the previous section for each model, the dashed line is generated with the same parameters except for the fact that the agent receives an annuity of 10 regardless of her employment status.

ment Table 2 to see the impact of c_{min} and the shapes of $\lambda(s,.)$ and $g(.)$ on the optimal level of b, b^*. Then, we compare the b^* obtained in the [BM] with the one of the [SM].

Table 2 displays different indicators when b verifies the optimality condition (12). "Gross RR*" is the optimal gross replacement rate: $\frac{b}{w}$ where in the simulations $w = 100$, "Net RR*", is the optimal net replacement rate $\frac{b}{w-\tau}$, "c_u^*/c_e^*" is the ratio of the consumption in unemployment $c_u^* = b + g(a)$ divided by the consumption in employment $c_e^* = w - \tau$, at b^*. Note that, in general, the level of "Net RR*" is very similar to the level of "c_u^*/c_e^*". This is because $g(a)$, is very close to zero when b is optimal.

As can be observed, the optimal gross replacement rate is, in most of the cases, between 0.55 and 0.72. Several other studies have computed the optimal value of b in different contexts and with different assumptions, but they tend to find replacement rates close to 0.50-0.60 (see for instance Pavoni, 2007 and Chetty, 2008).

Let us now analyze the impact of c_{min} and the shapes of $\lambda(s,.)$ and $g(.)$ on b^*. It can be seen that higher levels of c_{min} imply higher levels of b^*. Four parameters of Table 2 are linked to a: β_2, μ_2, G, and γ. As can be observed, the optimal level of b doesn't change with β_2, μ_2 or G. This is because $a \approx 0$ for levels of b above 60 in these specifications, therefore changing the parameters associated with a has no implications on b^*. Instead, when γ changes, the optimal level of b changes, because for low levels of γ, a is not negligible even for high values of b. In that case, b^* increases when γ increases, which is intuitive, because the value of $g(a)$ for a given a is smaller the higher the γ (for values of $a < 1$). Therefore higher values of γ reduce the self-insurance capacity of the agent.

Our numerical exercise shows that the optimal gross replacement rate in the standard model [SM] is 0.57 in the baseline case of Table 1. Table 2 shows the optimal replace-

ment rate in the baseline model [BM] for the different parameters linked to a (β_2, μ_2, G, γ) and for different levels of c_{min}. In all cases, except in one, the optimal replacement rate is higher or equal in the [BM] as compared with the [SM]. The only exception is the case in which $\gamma = 0.1$. When $\gamma = 0.1$, low levels of a are able to generate a high $g(a)$, therefore this constitutes an important margin of self-insurance which reduces b^*.

5 Conclusion

The available theory of job-search is developed in a very streamlined setting. This has the advantage of providing a number of clear-cut testable predictions. On this basis and given the accumulated empirical evidence, it is commonly accepted that a rise in the level of unemployment compensation lowers the probability of finding a job. It is also well accepted that providing cash irrespectively of the employment status has the same qualitative effect. However, the stylized nature of job-search theory sets aside a number of day-to-day problems encountered during joblessness. This paper has put forward the need to cover a minimal level of consumption in an otherwise standard job-search problem. Under realistic assumptions about the absence of private unemployment insurance and about imperfect capital markets, a minimal consumption level cannot be guaranteed when benefits are very low or absent (a feature shared by many countries). Through some subsistence activities, the jobless individual can tackle scarcity. These unpleasant activities can take a time which is no more available for searching a formal job. Alternatively, performing those activities limits cognitive capacities available for job-search. Providing a higher level of benefit can then relax the constraints imposed by those limits. The paper has privileged the second interpretation because some empirical evidence suggest that the time constraint is not central for job-seekers. However, both interpretations are compatible with the theoretical settings proposed in this paper.

We have shown that a rise in benefits (restricted to the unemployed or also given in case of employment) can raise the exit probability to a job. This property is established numerically in a range of standard job-search settings. Qualitatively, this occurs when benefit levels are low enough. These properties are not counter-factual. For, most empirical evaluations of the impact of benefits do not focus on the low-income jobless population or study the impact of unemployment insurance systems that are fairly generous. The few papers we have found dealing with this population and considering low benefits actually provide evidence that all in all goes in the direction predicted by our model.

This paper has also studied the optimal level of unemployment benefits. From an analytical point of view, we retrieve the standard Baily-Chetty formula. Our theoretical contribution consists in highlighting that writing the gain from insurance as the ratio of the liquidity effect to the moral hazard effect (Chetty, 2008) cannot be done without imposing restrictive and, to the best of our understanding, often unnoticed modeling assumptions. Finally, our numerical exercise indicates that the optimal replacement ratio is typically higher in our setting in comparison with a standard job-search model. The optimal level of benefits is also typically such that the agent is not or not much de-

voting effort to subsistence activities. From these properties, we conjecture that many actual unemployment insurance systems are suboptimal.

A Appendix

A.1 Positive Analysis

A.1.1 The Baseline Model [BM]

The first order conditions are already stated in the main text (3, 4). The second order derivatives are:

$$
\begin{aligned}
G_{ss} &\equiv -\lambda_{ss} + \beta P_{ss}(V^E - V^U) < 0 && (15)\\
G_{sa} &\equiv -\lambda_{as} + \beta P_{sa}(V^E - V^U) < 0 && (16)\\
G_{as} &\equiv -\lambda_{as} + \beta P_{sa}(V^E - V^U) < 0 && (17)\\
G_{aa} &\equiv u_{cc}(c^u) g_a^2 + u_c(c^u) g_{aa} - \lambda_{aa} + \beta P_{aa}(V^E - V^U) < 0 && (18)\\
G_{sb} &\equiv \beta P_s \frac{\partial (V^E - V^U)}{\partial b} = \frac{-\beta P_s}{1 - \beta[1 - P(a,s) - \phi]} u_c(c^u) < 0 && (19)\\
G_{ab} &\equiv u_{cc}(c^u) g_a + \beta P_a \frac{\partial (V^E - V^U)}{\partial b}\\
&= u_{cc}(c^u) g_a - \frac{\beta P_a}{1 - \beta[1 - P(a,s) - \phi]} u_c(c^u) \gtrless 0 && (20)\\
G_{sw} &\equiv \beta P_s \frac{\partial (V^E - V^U)}{\partial w} = \frac{\beta P_s}{1 - \beta[1 - P(a,s) - \phi]} u_c(c^e) > 0 && (21)\\
G_{aw} &\equiv \beta P_a \frac{\partial (V^E - V^U)}{\partial w} = \frac{\beta P_a}{1 - \beta[1 - P(a,s) - \phi]} u_c(c^e) < 0 && (22)\\
G_{sA} &\equiv \beta P_s \frac{\partial (V^E - V^U)}{\partial A} = \frac{\beta P_s}{1 - \beta[1 - P(a,s) - \phi]} [u_c(c^e) - u_c(c^u)] < 0 && (23)\\
G_{aA} &\equiv u_{cc}(c^u) g_a + \beta P_a \frac{\partial (V^E - V^U)}{\partial A}\\
&= u_{cc}(c^u) g_a + \frac{\beta P_a}{1 - \beta[1 - (P(a,s) - \phi]} [u_c(c^e) - u_c(c^u)] \gtrless 0 && (24)
\end{aligned}
$$

where $V^E - V^U = \frac{1}{1-\beta[1-P(s,a)-\phi]}(u(c^e) - u(c^u) + \lambda(s,a))$.

The following conditions are sufficient to guarantee that a solution, if any, to the system (3, 4) is a unique maximum: $G_{ss} < 0$ (so that P_{ss}, λ_{ss} cannot simultaneously be zero), $G_{aa} < 0$ and $G_{ss}G_{aa} - G_{as}^2 > 0$.

Totally differentiating the FOC (3, 4) with respect to s and b leads to:

$$\begin{cases} G_{ss}ds + G_{sa}da + G_{sb}db = 0 \\ G_{as}ds + G_{aa}da + G_{ab}db = 0 \end{cases} \tag{25}$$

Hence:

$$\frac{da}{db} = \frac{-G_{ss}G_{ab} + G_{as}G_{sb}}{G_{ss}G_{aa} - G_{as}^2} \tag{26}$$

$$\frac{ds}{db} = \frac{-G_{aa}G_{sb} + G_{sa}G_{ab}}{G_{ss}G_{aa} - G_{as}^2} \tag{27}$$

Where, the denominator of both expressions needs to be positive by the second order conditions.

The sign of $\frac{da}{db}$:

Since the denominator needs to be positive, let's concentrate on the numerator of $\frac{da}{db}$:

$$-\underbrace{[-\lambda_{ss} + \beta P_{ss}(V^E - V^U)]}_{\text{Gss: (-)}}\underbrace{[u_{cc}(c^u)g_a + \beta P_a \frac{\partial(V^E - V^U)}{\partial b}]}_{\text{Gab}} + \underbrace{\beta P_s \frac{\partial(V^E - V^U)}{\partial b}}_{\text{Gsb: (-)}}\underbrace{[-\lambda_{as} + \beta P_{sa}(V^E - V^U)]}_{\text{Gas: (-)}}$$

Note first that having $G_{ab} < 0$ is a necessary condition to have $\frac{da}{db} < 0$, nevertheless it is not sufficient. In what comes, we look for a sufficient condition for $\frac{da}{db} < 0$.

The previous expression can be re-written as:

$$\begin{aligned} &\underbrace{\lambda_{ss}u_{cc}(c^u)g_a}_{\text{1: (-)}} + \underbrace{\beta \frac{\partial(V^E - V^U)}{\partial b}[P_a\lambda_{ss} - P_s\lambda_{as}]}_{\text{2: (+)}} \\ &\underbrace{-\beta P_{ss}[V^E - V^U]u_{cc}(c^u)g_a}_{\text{3: (-)}} \underbrace{-\beta^2 \frac{\partial(V^E - V^U)}{\partial b}[V^E - V^U][P_aP_{ss} - P_sP_{as}]}_{\text{4: (+)}} \end{aligned} \tag{28}$$

The expression above is negative if the terms $1 + 2 < 0$ and $3 + 4 < 0$.

First condition: $1 + 2 < 0$

$\lambda_{ss}u_{cc}(c^u)g_a + \beta \frac{\partial(V^E - V^U)}{\partial b}[P_a\lambda_{ss} - P_s\lambda_{as}] < 0$ iff

$-u_{cc}(c^u)g_a > \beta \frac{\partial(V^E - V^U)}{\partial b}[P_a - P_s\frac{\lambda_{as}}{\lambda_{ss}}]$

Second condition: $3 + 4 < 0$

$-\beta P_{ss}[V^E - V^U]u_{cc}(c^u)g_a - \beta^2 \frac{\partial(V^E - V^U)}{\partial b}[V^E - V^U][P_aP_{ss} - P_sP_{as}] < 0$ iff

$P_{ss}u_{cc}(c^u)g_a + \beta \frac{\partial(V^E - V^U)}{\partial b}[P_aP_{ss} - P_sP_{as}] > 0$ iff

$u_{cc}(c^u)g_a + \beta\frac{\partial(V^E-V^U)}{\partial b}[P_a - \frac{P_s P_{as}}{P_{ss}}] < 0$ iff

$-u_{cc}(c^u)g_a > \beta\frac{\partial(V^E-V^U)}{\partial b}[P_a - P_{as}\frac{P_s}{P_{ss}}]$

Putting together the two conditions we get the sufficient condition (5) in the main text. If $P_{ss} = 0$, that is, if the probability of finding a job is linear with respect to s, the term 3 of expression (28) above disappears, and also a part of term 4. After some simplifications, and using the first order condition with respect to s, we are then left with this condition:

$-u_{cc}(c^u)g_a > \beta\frac{\partial(V^E-V^U)}{\partial b}[P_a - P_s\frac{\lambda_{as}}{\lambda_{ss}} + P_{as}\frac{\lambda_s}{\lambda_{ss}}]$

If $\lambda_{ss} = 0$, that is, if the cost of effort is linear with respect to s, the term 1 of expression (28) above disappears, and also a part of term 2. After some simplifications, and using the first order condition with respect to s, we are then left with this condition:

$-u_{cc}(c^u)g_a > \beta\frac{\partial(V^E-V^U)}{\partial b}[P_a - P_s(\frac{-\lambda_{as}P_s}{\lambda_s P_{ss}} + \frac{P_{as}}{P_{ss}})]$

The sign of $\frac{ds}{db}$:

Since the denominator needs to be positive, let's concentrate on the numerator of $\frac{ds}{db}$.

$$\underbrace{-\beta P_s\frac{\partial(V^E-V^U)}{\partial b}}_{\text{-Gsb: (+)}}\underbrace{[u_{cc}(c^u)g_a + u_c(c^u)g_{aa} + \beta P_{aa}(V^E-V^U)]}_{\text{Gaa: (-)}}$$
$$+\underbrace{[-\lambda_{as} + \beta P_{sa}(V^E-V^U)]}_{\text{Gsa: (-)}}\underbrace{[u_{cc}(c^u)g_a + \beta P_a\frac{\partial(V^E-V^U)}{\partial b}]}_{\text{Gab}} \tag{29}$$

Note that $ds/db > 0$ *could* be possible only when G_{ab} is negative, which is a necessary condition to have $da/db < 0$. But, even in that case, there are several terms pushing in the direction of having $ds/db < 0$.

Corner Solutions:

The previous analysis assumed that $a > 0$ and $s > 0$, i.e, that the optimum is interior. Let's analyze now the possibility of having corner solutions:

- Note first that choosing $a = 0$ when $b < c_{min}$ is not possible. In that case, the agent needs to generate some subsistence consumption.
- If $b > c_{min}$ and if the agent chooses $a = 0$, then the problem becomes exactly equal the standard model [SM], and hence (4) is the unique FOC (the only difference with respect to the standard model being the presence of c_{min}).
- We avoid having $s = 0$ by imposing $\lambda_s(0,a) < \beta P_s(0,a)[V^E - V^U]$ for all possible values of a. Except for the presence of a, this inequality is standardly assumed (explicitly or not) in the job search literature.

A.1.2 Extensions to the baseline model [BM]

In this section we start by presenting the three extensions to the baseline model [BM]. In all of them time is finite and equal to T periods (from $t = 0$ to $t = T - 1$). Since time is finite, the environment is not stationary anymore. The structure of the problem, nevertheless, remains very similar. First, we present the model with finite entitlement [FE], where the agent is entitled to a flat b during B periods, $B < T$. Second, we incorporate incomplete financial markets into the setting with finite horizon and flat b for T periods. Finally, we assume that there is a distribution of wage offers (McCall, 1970), in this environment the agent chooses a reservation wage, x_t, below which job offers are rejected. We finish the section by presenting the stationary model with monetary costs of job search in which looking for a job requires both job search effort and also a flow expenditure.

Model with Finite entitlement [FE]

Using the same notations as before, the lifetime values in unemployment and in employment solve respectively the following Bellman equations:

$$[FE] = \begin{cases} V_t^U = \max\limits_{s_t, a_t} \quad u(c_t^u) - \lambda(s_t, a_t) + \beta[P(s_t, a_t)V_{t+1}^E + (1 - P(s_t, a_t))V_{t+1}^U] \\ V_t^E = u(c_t^e) + \beta[\phi V_{t+1}^U + (1 - \phi)V_{t+1}^E] \end{cases} \tag{30}$$

where $c_t^u = b + g(a_t)$ if $t \leq B - 1$ and $c_t^u = g(a_t)$ if $B - 1 < t < T$, $c_t^e = w - \tau$.

Subject to: $c_t^u \geq c_{min}$, $V_{t+1}^E - V_{t+1}^U \geq 0$, $a_t \geq 0$, $s_t \geq 0$ and $V_T^U = V_T^E = 0$

The First Order Conditions:

$$\begin{aligned} G_a &\equiv u_c(c_t^u)g_a(a_t) - \lambda_a + \beta P_a[V_{t+1}^E - V_{t+1}^U] = 0 \\ G_s &\equiv -\lambda_s + \beta P_s[V_{t+1}^E - V_{t+1}^U] = 0 \end{aligned}$$

Which are the same as in the stationary case (except from the fact that now the timing for V^U and V^E is relevant). The same happens with the second order partial derivatives:

$$\begin{aligned} G_{ss} &\equiv -\lambda_{ss} + \beta P_{ss}(V_{t+1}^E - V_{t+1}^U) \\ G_{sa} &\equiv -\lambda_{as} + \beta P_{sa}(V_{t+1}^E - V_{t+1}^U) \\ G_{as} &\equiv -\lambda_{as} + \beta P_{sa}(V_{t+1}^E - V_{t+1}^U) \\ G_{aa} &\equiv u_{cc}(c_t^u)g_a(a_t)^2 + u_c(c_t^u)g_{aa}(a_t) - \lambda_{aa} + \beta P_{aa}(V_{t+1}^E - V_{t+1}^U) \\ G_{sb} &\equiv \beta P_s \frac{\partial(V_{t+1}^E - V_{t+1}^U)}{\partial b} \\ G_{ab} &\equiv u_{cc}(c_t^u)g_a(a_t) + \beta P_a \frac{\partial(V_{t+1}^E - V_{t+1}^U)}{\partial b} \end{aligned}$$

And, therefore, a sufficient condition to have $da/db < 0$ is the same as before:

$$-u_{cc}(c_t^u)g_a(a_t) > \beta \frac{\partial(V_{t+1}^E - V_{t+1}^U)}{\partial b}\left(P_a - P_s(\frac{\lambda_{as}}{\lambda_{ss}} + \frac{P_{as}}{P_{ss}})\right)$$

Note, nevertheless, that the expression $\frac{\partial(V_{t+1}^E - V_{t+1}^U)}{\partial b}$ is different from the expression that we had before. While the expression is relatively simple when employment is an absorbing state, it gets more complicated when $\phi \neq 0$.

Equivalently, $ds/db < 0$ is equal to:

$$\underbrace{-\beta P_s \frac{\partial(V_{t+1}^E - V_{t+1}^U)}{\partial b}}_{\text{-Gsb: (+)}} \underbrace{[u_{cc}(c_t^u)g_a(a_t)^2 + u_c(c_t^u)g_{aa}(a_t) - \lambda_{aa} + \beta P_{aa}(V_{t+1}^E - V_{t+1}^U)]}_{\text{Gaa: (-)}} + \underbrace{[-\lambda_{as} + \beta P_{sa}(V_{t+1}^E - V_{t+1}^U)]}_{\text{Gsa: (-)}} \underbrace{[u_{cc}(c_t^u)g_a(a_t) + \beta P_a \frac{\partial(V_{t+1}^E - V_{t+1}^U)}{\partial b}]}_{\text{Gab}} \tag{31}$$

Model with Incomplete Financial Markets [FM]

Consider now the problem where the time horizon is finite and equal to T (from $t = 0$ to $t = T - 1$) and the agent is entitled to a flat benefit for $B = T$ periods. The difference now is that agents have access to an asset traded on an imperfect credit market. For simplicity (as Hopenhayn and Nicolini, 1997, Chetty, 2008, Shimer and Werning, 2008, Schmieder et al., 2012, Kolsrud et al., 2015, Kroft and Notowidigdo, 2016) we consider that employment is an absorbing state ($\phi = 0$). Using the same notations as before, and denoting by k_t the level of assets in each period, the lifetime values in unemployment and in employment solve respectively the following Bellman equations:

$$[FM] = \begin{cases} V_t^U = \max\limits_{s_t, a_t, k_{t+1}} & u(c_t^u) - \lambda(s_t, a_t) + \beta[P(s_t, a_t)V_{t+1}^E + (1 - P(s_t, a_t))V_{t+1}^U] \\ V_t^E = \max\limits_{k_{t+1}} & u(c_t^e) + \beta V_{t+1}^E \end{cases} \tag{32}$$

where $c_t^u = b + g(a_t) + (1 + r)k_t - k_{t+1}$ and $c_t^e = w - \tau + (1 + r)k_t - k_{t+1}$.

Subject to: $c_t^u \geq c_{min}$, $V_{t+1}^E - V_{t+1}^U \geq 0$, $a_t \geq 0$, $s_t \geq 0$, $V_T^U = V_T^E = k_T = 0$ and $k_{t+1} \geq L$. This last condition can be interpreted as a capital market imperfection.[34]

Since $\phi = 0$ the setup is deterministic when the agent is employed. The optimal consumption path satisfies the Euler equation:

$$u_c(c_t^e) = \beta(1 + r)u_c(c_{t+1}^e)$$

We assume that $\beta = \frac{1}{1+r}$, this implies that the agent entering in employment in period t keeps the same level of consumption until T.

[34] As highlighted by Chetty (2008), it is easy to show that V_t^E is concave, because there is no uncertainty following reemployment; however, V_t^U *could be* convex. Nevertheless, this is not the case in our simulations -non concavity never arises in Chetty (2008) nor in Lentz and Tranaes (2005) either.

In order to find c_t^e, let us consider the budget constraint of the employed agent hired in period t with an initial level of assets of k_t: $c_t^e = w-\tau+(1+r)k_t-k_{t+1}$. This expression can be rewritten as: $k_t = \frac{c_t^e-(w-\tau)+k_{t+1}}{1+r}$. By iterating forward (that is, by replacing $k_{t+1} = \frac{c_{t+1}^e-(w-\tau)+k_{t+2}}{1+r}$ on the previous expression, and then replacing k_{t+2}, etc...) and since $k_T = 0$, we have that:

$$k_t(1+r) = c_t^e - (w-\tau) + \frac{c_t^e-(w-\tau)}{1+r} + ... + \frac{c_t^e-(w-\tau)}{(1+r)^{(T-1)-t}} \quad = [c_t^e-(w-\tau)] \sum_{j=0}^{(T-1)-t} \frac{1}{1+r}$$

which implies that, as long as r is different from zero:

$$c_t^e = k_t \left(\frac{r}{1-(\frac{1}{1+r})^{(T-1)-t+1}} \right) + w - \tau$$

Now, c_t^e is a function of t because it depends on the moment in which the agent starts working: If the agent is recruited in $t+1$ her constant level of consumption when employed is different from the one she would have if she was hired in t.

Moreover, since consumption is constant from the moment in which the agent is employed, we can write:

$$V_t^E = \sum_{j=0}^{(T-1)-t} \beta^j u(c_t^e) \quad = u(c_t^e) \frac{1-\beta^{(T-1)-t+1}}{1-\beta}$$

In unemployment, the First Order Conditions can be written as:

$$\begin{aligned} G_{a_t} &\equiv u_c(c_t^u) g_a(a_t) - \lambda_a + \beta P_a [V_{t+1}^E - V_{t+1}^U] = 0 \\ G_{s_t} &\equiv -\lambda_s + \beta P_s [V_{t+1}^E - V_{t+1}^U] = 0 \\ G_{k_{t+1}} &\equiv -u_c(c_t^u) + \beta \left(P(s_t,a_t) \frac{\partial V_{t+1}^E}{\partial k_{t+1}} + (1-P(s_t,a_t)) \frac{\partial V_{t+1}^U}{\partial k_{t+1}}) \right) = 0 \end{aligned}$$

where:

$$\frac{\partial V_{t+1}^E}{\partial k_{t+1}} = u_c(c_{t+1}^e) \frac{1-\beta^{(T-1)-t}}{1-\beta} \frac{\partial c_{t+1}^e}{\partial k_{t+1}} \quad = u_c(c_{t+1}^e) \frac{1-\beta^{(T-1)-t}}{1-\beta} \frac{r}{1-(\frac{1}{1+r})^{(T-1)-t}} = \frac{u_c(c_{t+1}^e)}{\beta}$$

and:

$$\frac{\partial V_{t+1}^U}{\partial k_{t+1}} = u_c(c_{t+1}^u)(1+r) \quad = \frac{u_c(c_{t+1}^u)}{\beta}$$

Which allows to re-write $G_{k_{t+1}}$ as:

$$G_{k_{t+1}} \equiv -u_c(c_t^u) + P(s_t,a_t) u_c(c_{t+1}^e) + (1-P(s_t,a_t)) u_c(c_{t+1}^u) = 0$$

The comparative statics are now more complex, since we have three choice variables. In section 4, we will solve this problem numerically.

Model with Stochastic Wage Offers [SWO]

Consider now the problem where the time horizon is finite and equal to T (from $t = 0$ to $t = T - 1$) and the agent is entitled to a flat benefit for $B = T$ periods. The difference now is that wage offers are stochastic (McCall, 1970). The distribution of wage offers is known, we denote the support of the distribution by $[\underline{w}, \overline{w}]$ $(0 \leq \underline{w} < \overline{w})$, the cumulative distribution function (CDF) by $H(w)$ and the probability density function (PDF) by $h(w)$. If an offer is received, the agent has to decide to accept it or not (no recall). Then, the agent follows a stopping rule: if the wage offer is higher than the reservation wage, x_t, she accepts the offer, otherwise, she rejects it. Using the same notations as before, the lifetime values in unemployment and in employment solve respectively the following Bellman equations:

$$[SWO] = \begin{cases} V_t^U = \max\limits_{s_t, a_t, x_t} \quad u(c_t^u) - \lambda(s_t, a_t) + \beta[P(s_t, a_t)V_{t+1}^\theta + (1 - P(s_t, a_t))V_{t+1}^U] \\ V_t^E = u(c_t^e) + \beta V_{t+1}^E \end{cases} \tag{33}$$

where $V_{t+1}^\theta = E_w max\{V_{t+1}^E(w), V_{t+1}^U\} = \int_0^{x_t} V_{t+1}^U dH(w) + \int_{x_t}^{\bar{w}} V_{t+1}^E(w) dH(w)$

Subject to: $c_t^u \geq c_{min}$, $a_t \geq 0$, $s_t \geq 0$, $V_T^U = V_T^E = 0$.

V_t^U can be rewritten as:

$$V_t^U = \max_{s_t, a_t, x_t} \quad u(c_t^u) - \lambda(s_t, a_t) + \beta \left[P(s_t, a_t) \int_{x_t}^{\bar{w}} (V_{t+1}^E(w) - V_{t+1}^U) dH(w) + V_{t+1}^U \right]$$

The First Order Conditions can be written as:

$$G_{a_t} \equiv u_c(c_t^u) g_a(a_t) - \lambda_a + \beta P_a \int_{x_t}^{\bar{w}} (V_{t+1}^E(w) - V_{t+1}^U) dH(w) = 0 \tag{34}$$

$$G_{s_t} \equiv -\lambda_s + \beta P_s \int_{x_t}^{\bar{w}} (V_{t+1}^E(w) - V_{t+1}^U) dH(w) = 0 \tag{35}$$

$$G_{x_t} \equiv \beta P(s_t, a_t) \left(V_{t+1}^E(x) - V_{t+1}^U \right) h(x_t) = 0 \tag{36}$$

The comparative statics are now more complex, since we have three choice variables. In section 4, we will solve this problem numerically.

Model with Monetary Costs of Job Search [MC]

Consider now again a stationary setup, with infinite time horizon. In this setup looking for a job requires both job search effort, s, but also a flow expenditure, m. The the lifetime values in unemployment and in employment solve respectively the following

Bellman equations:

$$[MC] = \begin{cases} V^U = \max\limits_{s,m} \quad u(c^u) - \lambda(s) + \beta[P(s,m)V^E + (1 - P(s,m))V^U] \\ V^E = u(c^e) + \beta[\phi V^U + (1-\phi)V^E] \end{cases} \tag{37}$$

Where $u(c^u) = u(b-m)$, $u(c^e) = u(w-\tau)$ and m is the quantity of money devoted to job search.

Subject to: $V^E - V^U \geq 0$ and $s \geq 0$.

If the direct cost of the effort devoted to the subsistence activity is zero, problems [BM] and [MC] can be seen as equivalent if one ignores c_{min}. When c_{min} is taken into account in [BM], the difference between the two setups is deeper than it appears at first glance, because $b - m \leq b$ and subsistence cannot be guaranteed if $b < c_{min}$.

A.2 Optimal Unemployment Insurance

A.2.1 Impossibility to write $\frac{u_c(c^u)-u_c(c^e)}{u_c(c^e)} = \frac{\textbf{liquidity effect}}{\textbf{moral hazard effect}}$

In our baseline model

$$\begin{aligned} \frac{\text{liquidity effect}}{\text{moral hazard effect}} &= \frac{P_a \frac{da}{dA} + P_s \frac{ds}{dA}}{-(P_a \frac{da}{dw} + P_s \frac{ds}{dw})} \\ &= \frac{P_a[-G_{ss}G_{aA} + G_{as}G_{sA}] + P_s[-G_{aa}G_{sA} + G_{sa}G_{aA}]}{-(P_a[-G_{ss}G_{aw} + G_{as}G_{sw}] + P_s[-G_{aa}G_{sw} + G_{sa}G_{aw}])} \end{aligned} \tag{38}$$

Which cannot be reduced to $\frac{u_c(c^u)-u_c(c^e)}{u_c(c^e)}$.

Nevertheless, if we assume that when b changes only s changes (a remains constant), then the previous expression becomes:

$$\frac{\text{liquidity effect}}{\text{moral hazard effect}} = \frac{P_s \frac{ds}{dA}}{-P_s \frac{ds}{dw}} = \frac{\frac{-G_{sA}}{G_{ss}}}{\frac{G_{sw}}{G_{ss}}} = \frac{-G_A}{G_{sw}} = \frac{u_c(c^u) - u_c(c^e)}{u_c(c^e)} \tag{39}$$

Instead, if we assume that when b changes only a changes (s remains constant), then (38) becomes:

$$\frac{\text{liquidity effect}}{\text{moral hazard effect}} = \frac{P_a \frac{da}{dA}}{-P_a \frac{da}{dw}} = \frac{\frac{-G_{aA}}{G_{aa}}}{\frac{G_{aw}}{G_{aa}}} = \frac{-G_{aA}}{G_{aw}} = \frac{-u_{cc}(c^u)g_a}{\frac{\beta P_a u_c(c^e)}{1-\beta[1-P-\phi]}} + \frac{u_c(c^u) - u_c(c^e)}{u_c(c^e)} \tag{40}$$

This shows that, $\frac{u_c(c^u)-u_c(c^e)}{u_c(c^e)} = \frac{\text{liquidity effect}}{\text{moral hazard effect}}$ if one assumes that only one choice variable changes when b changes *and* this variable is such that the utility function is separable in consumption and the cost of this variable (39). Instead, $\frac{u_c(c^u)-u_c(c^e)}{u_c(c^e)} \neq \frac{\text{liquidity effect}}{\text{moral hazard effect}}$ if there are two choice variables that change when b changes (38) *or* if

there is just one variable that changes, but such that the utility function is not separable in consumption and the cost of this variable (40).

A.2.2 Optimal UI in a non-stationary setting

In this section we assume that time is finite, and equal to T (from $t = 0$ to $t = T - 1$). For simplicity (as Chetty, 2008, Schmieder et al., 2012, Kolsrud et al., 2015, Kroft and Notowidigdo, 2016) we assume that there is no job destruction ($\phi = 0$).

Because of the envelope conditions, the following analysis is independent of the underlying structure of the model behind it (see Chetty, 2006 and Chetty, 2008), in particular on whether or not the agent is allowed to save, or whether or not she chooses a reservation wage in a context of stochastic wage offers. In the development below, we assume that there is finite entitlement, meaning that the UB is paid during B periods where $B < T$ (If one wants to assume that $B = T$, it suffices to replace B for T everywhere).

On top of the underlying model, our analysis for the optimal UB differs from the one of Chetty (2008) in two respects: (1) $\beta = \frac{1}{1+r} \neq 1$ and more importantly (2) our timing assumption: in our model, if the agent finds a job in t, she starts working in $t+1$.

The optimal level of UB is the level of b that maximizes the inter-temporal utility of the job seeker subject to the budget balanced condition. Formally:

$$\max_b V_0^U = \quad u(c_0^u) - \lambda(s_0, a_0) + \beta[P_0 V_1^E + (1 - P_0) V_1^U]$$

Subject to: $D_B\, b = (T - D)\,\tau$, where D is the expected duration in unemployment, $D = 1 + \sum_{t=0}^{T-2} \prod_{i=0}^{t} (1 - P_i)$ and D_B is equal to the expected *compensated* duration in unemployment $D_B = 1 + \sum_{t=0}^{B-2} \prod_{i=0}^{t} (1 - P_i)$. In these expressions P is a short notation for $P(s, a)$.

Applying the envelope theorem, the derivative of the previous expression with respect to b gives:

$$\frac{dV_0^U}{db} = \quad u'(c_0^u) - \beta P_0 \frac{dV_1^E}{dw}\frac{d\tau}{db} + \beta(1 - P_0)\left[\frac{dV_1^U}{db} - \frac{dV_1^U}{dw}\frac{d\tau}{db}\right]$$

where $\frac{dV_1^J}{dw} = \sum_{t=1}^{T-1} \frac{dV_1^J}{dw_t}$, for $J \in \{E, U\}$ and $\frac{dV_1^U}{db} = \sum_{t=1}^{B-1} \frac{dV_1^U}{db_t}$

Which could be rewritten as:

$$\frac{dV_0^U}{db} = \quad u'(c_0^u) - \frac{d\tau}{db}\left[\beta P_0 \frac{dV_1^E}{dw} + \beta(1 - P_0)\frac{dV_1^U}{dw}\right] + \beta(1 - P_0)\frac{dV_1^U}{db} \tag{41}$$

We now need to find the values of $\frac{dV_1^E}{dw}$, $\frac{dV_1^U}{dw}$ and $\frac{dV_1^U}{db}$ to plug them in the expression above. We obtain the following derivatives for the value functions (assuming $T \geq B > 2$) :[35]

[35] Note that since $\beta = \frac{1}{1+r}$, and since employment is an absorbing state, the agent will have a constant level of consumption since the moment at which she starts to work.

$$
\begin{aligned}
\frac{dV_1^U}{db} &= u'(c_1^u) + \sum_{t=1}^{B-2} \beta^t \prod_{j=1}^{t} (1-P_j) u'(c_{t+1}^u) \\
\frac{dV_1^E}{dw} &= u'(c_1^e) \sum_{t=0}^{T-2} \beta^t \\
\frac{dV_1^U}{dw} &= P_1 u'(c_2^e) \sum_{t=2}^{T-1} \beta^{t-1} + \sum_{t=2}^{T-2} \left[\prod_{i=2}^{t} (1-P_{i-1}) P_t \, u'(c_{t+1}^e) \sum_{j=t+1}^{T-1} \beta^{j-1} \right]
\end{aligned}
$$

Now, let us compute the unconditional average marginal utility while employed:

$$
\begin{aligned}
E_{0,T-1} u'(c_t^e) &= \frac{1}{T-D} \left[P_0 \, u'(c_1^e) \sum_{t=1}^{T-1} \beta^t + (1-P_0) P_1 \, u'(c_2^e) \sum_{t=2}^{T-1} \beta^t + \ldots + \prod_{i=0}^{T-3} (1-P_i) P_{T-2} \, \beta^{T-1} u'(c_{T-1}^e) \right] \\
&= \frac{1}{T-D} \left[\beta \, P_0 \frac{dV_1^E}{dw} + \beta (1-P_0) \frac{dV_1^U}{dw} \right]
\end{aligned}
\tag{42}
$$

The unconditional average marginal utility while unemployed over the first B periods is equal to:

$$
\begin{aligned}
E_{0,B-1} u'(c_t^u) &= \frac{1}{D_B} \left[u'(c_0^u) + (1-P_0) \beta u'(c_1^u) + \ldots + \beta^{B-1} \prod_{t=0}^{B-2} (1-P_t) u'(c_{B-1}^u) \right] \\
&= \frac{1}{D_B} \left[u'(c_0^u) + \beta (1-P_0) \frac{dV_1^U}{db} \right]
\end{aligned}
\tag{43}
$$

Plugging (42) and (43) in (41) gives:

$$
\frac{dV_0^U}{db} = D_B \, E_{0,B-1} u'(c_t^u) - (T-D) \, E_{0,T-1} u'(c_t^e) \frac{d\tau}{db} \tag{44}
$$

where $\frac{d\tau}{db} = \frac{D_B}{T-D} \left(1 + \varepsilon_{D_B,b} + \varepsilon_{D,b} \frac{D}{T-D} \right)$, and $\varepsilon_{D_B,b} = \frac{dD_B}{db} \frac{b}{D_B}$, $\varepsilon_{D,b} = \frac{dD}{db} \frac{b}{D}$.

Plugging $\frac{d\tau}{db}$ in (44), simplifying and setting $\frac{dV_0^U}{db} = 0$ gives:

$$
\frac{E_{0,B-1} u'(c_t^u) - E_{0,T-1} u'(c_t^e)}{E_{0,T-1} u'(c_t^e)} = \varepsilon_{D_B,b} + \varepsilon_{D,b} \frac{D}{T-D} \tag{45}
$$

Consider $\sigma = \frac{T-D}{T}$, then the previous expression can be written as:

$$
\frac{E_{0,B-1} u'(c_t^u) - E_{0,T-1} u'(c_t^e)}{E_{0,T-1} u'(c_t^e)} = \frac{1}{\sigma} \left(\sigma \varepsilon_{D_B,b} + (1-\sigma) \varepsilon_{D,b} \right) \tag{46}
$$

Having $B < T$ has two implications: (1) The LHS of the formula takes the average consumption while unemployed and *entitled to b* minus the average consumption when employed and (2) the RHS is a weighted average of $\varepsilon_{D_B,b}$ and $\varepsilon_{D,b}$, because the cost of the insurance depends not only on the time the agent is unemployed and compensated (D_B) but also on the time the agent is not paying taxes (D). If $B = T$, that is, without finite entitlement, the previous expression becomes:

$$\frac{E_{0,T-1}u'(c_t^u) - E_{0,T-1}u'(c_t^e)}{E_{0,T-1}u'(c_t^e)} = \varepsilon_{D,b}\frac{T}{T-D} \tag{47}$$

Moreover, without finite entitlement and if $T = \infty$ we are back to the stationary case analyzed in the main text, where $E_{0,T-1}u'(c_t) = u'(c)$ -because consumption is constant-, and $\lim_{T\to\infty}\frac{T}{T-D} = 1$. This reduces the previous expression to the formula (12) in the main text.

References

Aguiar, M., Hurst, E., and Karabarbounis, L. (2013). Time use during the great recession. *American Economic Review*, 103(5):1664–1696.

Algan, Y., Cheron, A., and Hairault, J.-O. (2003). Wealth effect on labor market transitions. *Review of Economic Dynamics*, 6(1):156–178.

Alvarez-Parra, F. and Sanchez, J. M. (2009). Unemployment insurance with a hidden labor market. *Journal of Monetary Economics*, 56:954–967.

Baily, M. N. (1978). Some aspects of optimal unemployment insurance. *Journal of Public Economics*, 10(3):379–402.

Baird, S., McKenzie, D., and Özler, B. (2018). The effects of cash transfers on adult labor market outcomes. Policy Research Working Paper 8404, World Bank Group.

Banerjee, A., Hanna, R., Kreindler, G., and and, B. A. O. (2017). Debunking the stereotype of the lazy welfare recipient: Evidence from cash transfer programs worldwide. *World Bank Research Observer*, 32(2):155–184.

Barrientos, A. and Villa, J. M. (2015). Antipoverty transfers and labour market outcomes: Regression discontinuity design findings. *The Journal of Development Studies*, 51(9):1224–1240.

Barron, J. M. and Mellow, W. (1979). Search effort in the labor market. *The Journal of Human Resources*, 14(3):389–404.

Basten, C., Fagereng, A., and Telle, K. (2014). Cash-on-hand and the duration of job search: Quasi-experimental evidence from Norway. *The Economic Journal*, 124(576):540–568.

Ben-Horim, M. and Zuckerman, D. (1987). The effect of unemployment insurance on unemployment duration. *Journal of Labor Economics*, 5(3):386–390.

Bhalotra, S. (2007). Is child work necessary? *Oxford Bulletin of Economics and Statistics*, 69(1):29–55.

Bosch, M. and Esteban-Pretel, J. (2015). The labor market effects of introducing unemployment benefits in an economy with a high informality. *European Economic Review*, 75:1–17.

Caliendo, M., Cobb-Clarck, D. A., and Uhlendorff, A. (2015). Locus of control and job search strategies. *The Review of Economics and Statistics*, 97(1):88–103.

Card, D., Chetty, R., and Weber, A. (2007). Cash-on-hand and competing models of intertemporal behavior: New evidence from the labor market. *Quarterly Journal of Economics*, 122(4):1511–1560.

Centeno, M. and Novo, A. A. (2014). Do low-wage workers react less to longer unemployment benefits? Quasi-experimental evidence. *Oxford Bulletin of Economics and Statistics*, 76(2):185–207.

Charlot, O., Malherbet, F., and Ulus, M. (2016). Unemployment compensation and the allocation of labor in developing countries. *Journal of Public Economic Theory*, 18(3):385–416.

Chetty, R. (2006). A general formula for the optimal level of social insurance. *Journal of Public Economics*, 90(10):1879–1901.

Chetty, R. (2008). Moral hazard versus liquidity and optimal unemployment insurance. *Journal of Political Economy*, 116(2):173–234.

Chetty, R. (2009). Sufficient statistics for welfare analysis: A bridge between structural and reduced-form methods. *Annual Review of Economics*, 1:451–487.

Chetty, R. and Looney, A. (2006). Consumption smoothing and the welfare consequences of social insurance in developing economies. *Journal of Public Economics*, 90(12):2351–2356.

Cockx, B., Dejemeppe, M., Launov, A., and Van der Linden, B. (2018). Imperfect monitoring of job search: Structural estimation and policy design. *Journal of Labor Economics*, 36(1):75–120.

Decreuse, B. (2002). On the time sequence of unemployment benefits when search is costly. *Review of Labour Economics and Industrial Relations*, 16:609–633.

Dercon, S. (1998). Wealth, risk and activity choice: Cattle in western Tanzania. *Journal of Development Economics*, 55(1):1–42.

Easley, D., Kiefer, N., and Possen, U. (1985). An equilibrium analysis of optimal unemployment insurance and taxation. *The Quarterly Journal of Economics*, 100(1):989–1010.

Espino, E. and Sanchez, J. M. (2015). How does informal employment affect the design of unemployment insurance and employment protection? *Federal Reserve Bank of St. Louis Review*, 97(2):159–172.

Franklin, S. Location, search costs and youth unemployment: Experimental evidence from transport subsidies in Ethiopia. *Economic Journal*. forthcoming.

Frederiksson, P. and Holmlund, B. (2006). Improving incentives in unemployment insurance: A review of recent research. *Journal of Economic Surveys*, 20(3):357–386.

Gerard, F. and Gonzaga, G. (2016). Informal labor and the efficiency cost of social programs: Evidence from the brazilian unemployment insurance program. *NBER working paper series, WP 22608*.

Gonzalez-Rozada, M. and Ruffo, H. (2016). Optimal unemployment benefits in the presence of informal labor markets. *Labour Economics*, 41:204–227.

Hendren, N. (2017). Knowledge of future job loss and implications for unemployment insurance. *American Economic Review*, 107(7):1778–1823.

Hopenhayn, H. A. and Nicolini, J. P. (1997). Optimal unemployment insurance. *Journal of Political Economy*, 105(2):412–438.

Kolsrud, J., Landais, C., Nilsson, P., and Spinnewijn, J. (2015). The optimal timing of unemployment benefits: Theory and evidence from sweden. IZA Discussion Paper Series No. 9185.

Kroft, K. and Notowidigdo, M. J. (2016). Should unemployment insurance vary with the unemployment rate? Theory and evidence. *Review of Economic Studies*, 83(3):1092–1124.

Krueger, A. B. and Muller, A. (2010). Job search and unemployment insurance: New evidence from time use data. *Journal of Public Economics*, 94(3):298–307.

Kupets, O. (2006). Determinants of unemployment duration in Ukraine. *Journal of Comparative Economics*, 34(2):228–247.

Lalive, R., Ours, J. V., and Zweimuller, J. (2006). How changes in financial incentives affect the duration of unemployment. *Review of Economic Studies*, 73(4):1009–1038.

LaLumia, S. (2013). The EITC, tax refunds and unemployment spells. *American Economic Review*, 5(2):188–221.

Lawson, N. (2017). Fiscal externalities and optimal unemployment insurance. *American Economic Journal: Economic Policy*, 9(4):281–312.

Lentz, R. (2009). Optimal unemployment insurance in an estimated job search model with savings. *Review of Economic Dynamics*, 12(1):37–57.

Lentz, R. and Tranaes, T. (2005). Job seach and saving: Wealth effects and duration dependence. *Journal of Labor Economics*, 23(3):467–489.

Long, I. W. and Polito, V. (2017). Job search, unemployment protection and informal work in advanced economies. Cesifo Working paper No. 6763.

Mani, A., Mullainathan, S., Shafir, E., and Zhao, J. (2013). Poverty impedes cognitive function. *Science*, 341(6149):976–980.

Manning, A. (2011). *Handbook of Labor Economics*, volume IV, chapter 11: Imperfect Competition in the Labor Market, pages 976–1042. North Holland. Editors: David Card and Orley Ashenfelter.

Margolis, D., Navarro, L., and Robalino, D. (2014). Unemployment insurance, job search and informal employment. In Froelich, M., Kaplan, D., Pages, C., Rigolini, J., , and Robalino, D., editors, *Social Insurance and Labor Markets: How to Protect Workers while Creating Good Jobs*. Oxford University Press.

Mas-Colell, A., Whinston, M. D., and Green, J. R. (1995). *Microeconomic Theory*. Oxford University Press.

Matsaganis, M., Ozdemir, E., and Ward, T. (2014). The coverage rate of social benefits. Technical Report Research note 9/2013, Employment, Social Affairs and Inclusion, European Commission.

Mazur, K. (2016). Can welfare abuse be welfare improving? *Journal of Public Economics*, 141:11–28.

McCall, J. (1970). Economics of information and job search. *Quarterly Journal of Economics*, 84(1):113–126.

Morris, A. and Wilson, S. (2014). Struggling on the newstart unemployment benefit in Australia: The experience of a neoliberal form of employment assistance. *The Economic and Labour Relations Review*, 25(2):202–221.

Mortensen, D. (1977). Unemployment insurance and job decisions. *Industrial and Labor Relations Review*, 30(4):505–517.

Mullainathan, S. and Shafir, E. (2013). *Scarcity*. Times Books, Henry Holt and Company.

Pavoni, N. (2007). On optimal unemployment compensation. *Journal of Monetary Economics*, 54(6):1612–1630.

Schilbach, F., Schofield, H., and Mullainathan, S. (2016). The psychological lives of the poor. *American Economic Review: Papers and Proceedings*, 106(5):435–440.

Schmieder, J. and von Watcher, T. (2017). A context-robust measure of the disincentive cost of unemployment insurance. *American Economic Review: Papers and Proceedings*, 107(5):343–348.

Schmieder, J. and Watcher, T. V. (2016). The effects of unemployment insurance benefits: New evidence and interpretation. *Annual Review of Economics*, 8:547–581.

Schmieder, J., Watcher, T. V., and Bender, S. (2012). The effects of extended unemployment insurance over the business cycle: Evidence from regression discontinuity dessign estimates over 20 years. *The Quarterly Journal of Economics*, 127(2):701–752.

Schwartz, J. (2015). Optimal unemployment insurance: When search takes effort and money. *Labour Economics*, 36:1–17.

Shah, A. K., Mullainathan, S., and Shafir, E. (2012). Some consequences of having too little. *Science*, 338(6107):682–685.

Shah, A. K., Shafir, E., and Mullainathan, S. (2015). Scarcity frames value. *Psychological Science*, 26(4):402–412.

Shimer, R. and Werning, I. (2007). Reservation wages and unemployment insurance. *The Quarterly Journal of Economics*, 122(3):1145–1185.

Shimer, R. and Werning, I. (2008). Liquidity and insurance for the unemployed. *American Economic Review*, 98(5):1922–1942.

Spinnewijn, J. (2015). Unemployed but optimistic: Optimal insurance design with biased beliefs. *Journal of the European Economic Association*, 13(1):130–167.

Stephenson, S. P. (1976). The economics of youth job search behavior. *The Review of Economics and Statistics*, 58(1):104–111.

Tannery, F. J. (1983). Search effort and unemployment insurance reconsidered. *The Journal of Human Resources*, 18(3):432–440.

Taskin, T. (2011). Unemployment insurance and home production. Munich Personal RePEc Archive Paper No. 34878.

Tatsiramos, K. and van Ours, J. C. (2014). Labor market effects of unemployment insurance design. *Journal of Economic Surveys*, 28(2):284–311.

van den Berg, G. and van der Klaauw, B. (2006). Counseling and monitoring of unemployed workers: Theory and evidence from a concontrol social experiment. *International Economic Review*, 47(3):895–936.

Vodopivec, M. (2013). Introducing unemployment insurance to developing countries. *IZA Journal of Labor Policy*, 2(1):1–23.

Zimmerman, F. and Carter, M. R. (2003). Asset smoothing, consumption smoothing and the reproduction of inequality under risk and subsistence constraints. *Journal of Development Economics*, 71(2):233–260.