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# Minimum Wage and Employer Variety <br> Priyaranjan Jha, Antonio Rodriguez-Lopez 

## Impressum:

CESifo Working Papers
ISSN 2364-1428 (electronic version)
Publisher and distributor: Munich Society for the Promotion of Economic Research - CESifo GmbH
The international platform of Ludwigs-Maximilians University's Center for Economic Studies and the ifo Institute
Poschingerstr. 5, 81679 Munich, Germany
Telephone +49 (0)89 2180-2740, Telefax +49 (0)89 2180-17845, email office@cesifo.de Editor: Clemens Fuest
https://www.cesifo.org/en/wp
An electronic version of the paper may be downloaded

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# Minimum Wage and Employer Variety 


#### Abstract

Exploiting minimum wage variation within multi-state commuting zones, we document a negative relationship between minimum wages and establishment counts in the United States. To explain this finding, we construct a heterogeneous-firm model with a monopsonistic labor market and endogenous firm variety. The decentralized equilibrium underprovides the mass of firms compared to the outcome achieved by a welfare-maximizing planner. A binding minimum wage further reduces the mass of firms, exacerbating the distortion. Workers value employer variety, and thus, by reducing firm variety the minimum wage reduces workers' welfare even if the average wage increases. Based on estimated elasticities, our model predicts that a 10 percent minimum wage hike reduces workers' welfare by 1:87 percent.


JEL-Codes: J380, J420.
Keywords: minimum wage, number for firms, love of employer variety.

Priyaranjan Jha<br>University of California, Irvine / USA<br>pranjan@uci.edu

Antonio Rodriguez-Lopez<br>University of California, Irvine / USA<br>jantonio@uci.edu

First version: September 2021
This version: April 2022
We thank David Neumark for helpful comments and suggestions.

## 1 Introduction

There is a large body of empirical research on the labor market implications of minimum wages, with the main focus being on the impact of the minimum wage on employment and average wages (see Neumark and Shirley, 2021 and Manning, 2021 for recent surveys). Although the evidence is mixed, studies that do not find a negative employment response to minimum wages (see, e.g., Card and Krueger, 1994) often mention that a potential explanation is that labor markets are monopsonistic: facing an upward sloping labor supply, firms offer a wage that is below their marginal labor cost, and thus a minimum wage could lead to an increase in employment. This analysis, however, is incomplete because it assumes a fixed number of firms, and this number can be affected by a minimum wage. Simply put, a binding minimum wage increases firms' costs, which may lead to the exit of firms and reduce entry incentives, causing a decline in the mass of firms. This paper empirically analyzes the relationship between minimum wages and the number of firms, and studies the welfare implications of minimum wages when employer variety matters.

In section 2, we document a negative and statistically significant relationship between minimum wages and establishment counts in the United States. Using yearly U.S. data at the commuting zone-state level for the 1990-2016 period, we build on the cross-border design of Dube, Lester, and Reich (2010)—DLR hereafter-and estimate specifications that exploit minimum wage variation within multi-state commuting zones while controlling for time-varying spatial heterogeneity at the local level. ${ }^{1}$ For the overall U.S. economy, we find a significant minimum wage elasticity of establishment counts of -0.091 . After splitting U.S. establishments into 20 industries, we find negative and statistically significant elasticities not only in the two lowest-wage industries (restaurants and retail trade), but also in four mid-wage industries including the primary sector. Moreover, we find statistically significant evidence of long-term effects of minimum wage effects on U.S. establishments, with an estimated four-year elasticity of -0.224 .

Previous literature has found evidence that minimum wages affect establishments' entry and exit dynamics. Luca and Luca (2019), for example, use Yelp ratings data from San Francisco restaurants

[^0]and find that minimum wage hikes increase the exit of 3.5 -star restaurants. Relatedly, using a crossborder county-pair approach, Aaronson, French, Sorkin, and To (2018) find that minimum wage hikes increase both the entry and exit of limited service restaurants, but the effect is larger on exit. As well, using U.S. establishment-level data at the county-industry level, Chava, Oettl, and Singh (2019) find that increases in the federal minimum wage increase exit rates and reduce entry rates. On the other hand, Rohlin (2011) finds that minimum wage hikes reduce entry in low-education U.S. industries but does not increase exit of existing businesses. In spite of their differences, all these studies imply a net reduction in the number of establishments after a minimum wage increase, which is consistent with our empirical results. Compared to these studies, our identification strategy is based on exploiting minimum wage variation within multi-state commuting zones.

To understand the mechanisms through which minimum wages affect firm variety, in section 3 we expand the monopsonistic labor market framework to endogenize the number of firms in a setting with heterogeneous firms. In our model, changes in the number of firms affect welfare because workers love variety of employers: the larger the number of firms a worker could choose to work for, the higher the worker's welfare is. Whereas the role of the number of firms is well understood for consumers' welfare - more firms imply a larger variety of goods - and the Dixit-Stiglitz model with love-of-variety preferences is the workhorse framework in industrial organization and international trade, the role of the number of firms in workers' welfare has received less attention. Card, Cardoso, Heining, and Kline (2018) discuss a model where workers have idiosyncratic preferences for employers due to factors such as location, work hours, and work culture. As first pointed out by Thisse and Toulemonde (2010), in such a setting the larger the mass of employers the greater the maximized expected utility of workers. ${ }^{2}$

Using a Melitz-type structure, we find that the decentralized equilibrium and the social planner's problem yield similar firm sizes, so that in spite of a monopsonistic labor market, there is no misallocation of resources across firms. ${ }^{3}$ However, the mass of firms and total employment are smaller in the decentralized equilibrium than in the planner's solution, as a result of firms not taking into account the positive effect that the creation of an extra firm has on labor supply and welfare. In this setting, a binding minimum wage wipes out the least productive firms, affecting the allocation of

[^1]labor across firms, and reducing the total mass of employers. Since the mass of firms was suboptimal in the decentralized equilibrium, a binding minimum exacerbates the existing distortion and reduces total employment and welfare, even if the average wage increases.

## 2 Minimum Wages and the Number of Establishments: Empirical Assessment

This section documents a negative and statistically significant relationship between minimum wages and the number of establishments in the United States.

### 2.1 Data

From the Census's County Business Patterns (CBP) we obtain county-industry yearly establishment counts from 1990 to 2016, as well as annual payroll and employment. ${ }^{4}$ We follow Jha, Neumark, and Rodriguez-Lopez (2022), who use the detailed programs of Acemoglu, Autor, Dorn, Hanson, and Price (2016), to process the CBP data into 479 industries and 722 commuting zones, but also splitting commuting zones by state. This yields 866 commuting zone-state entities, with 585 coming from single-state commuting zones, $130 \times 2$ from two-state commuting zones, and $7 \times 3$ from three-state commuting zones. ${ }^{5}$ For our estimation strategy we focus on the 281 entities from the 137 multi-state commuting zones. These 137 zones-which account for 29.8 percent of U.S. employment and for 29 percent of U.S. establishments - contain 151 unique pairs: 130 pairs from the two-state commuting zones, and 21 pairs from the 7 three-state commuting zones. ${ }^{6}$

Whereas most minimum wage studies focus on the restaurant industry (including DLR and Jha, Neumark, and Rodriguez-Lopez, 2022), here we look at the effects of minimum wages on the overall number of establishments, as well as for 20 industries that encompass the entire U.S. economy. In the classification of Acemoglu, Autor, Dorn, Hanson, and Price (2016), we use industries 5812 (restaurants) and 5210 (retail trade), and aggregate the remaining 477 industries into 18 industries. Table 1 shows nominal earnings per worker, earnings rankings, and establishment and employment

[^2]shares in U.S. totals for each of the 20 industries in 1990 and 2016. Table 1 sorts industries based on earnings per worker in 1990 (from lowest to highest), and below we use this ranking to identify each industry (e.g., industry 1 refers to Restaurants and industry 15 refers to Metals).

In Table 1 we see that earnings-per-worker rankings by industry are very similar in both years, with the five lowest-earnings industries keeping the same order. Restaurants have by far the lowest earnings, which is the reason why most minimum wage studies focus on that industry-it is the industry were minimum wages are more likely to bind in a wide scale. ${ }^{7}$ Nevertheless, most industries will be affected by minimum wages, as different firms within an industry pay different wages, and firms hire workers in different occupations and skill levels.

In addition to CBP data, we obtain yearly working-age population at the commuting zone-state level from the Census Bureau's Population Estimates Program, while from Vaghul and Zipperer (2016) we obtain yearly minimum wage data at the state level, with the minimum wage defined as the largest of the federal minimum wage and the state minimum wage. ${ }^{8}$

In the end, our dataset includes industry-level and overall establishment counts (as well as employment and earnings per worker), working-age population, and minimum wage for each of the 281 commuting zone-state entities that make the 151 pairs from multi-state commuting zones. Similar to DLR, we arrange the data so that for each industry in each period there are 302 observations (two for each pair), with each observation identified by its commuting zone, state, and pair: 260 commuting zone-state entities appear once (from the 130 two-state commuting zones), whereas 21 appear twice (from the 7 three-state commuting zones). If an industry appears in all commuting zone-state entities in all years, the maximum number of observations would be $302 \times 27=8,154$. In our regressions below for different industries, the number of observations ranges between 5,346 and 8, 134 .

### 2.2 Econometric Specification and Main Results

DLR argue that conventional estimates of the minimum wage elasticity of employment-from twoway fixed effects specifications - are biased because they fail to account for spatial heterogeneity at the local level. To control for local economic conditions, they introduce a cross-state county-pair approach that exploits minimum wage variation within local economic areas.

Along these lines, but defining a local economic area as a pair within a multi-state commuting zone rather than as a pair of contiguous counties sharing a state border (Jha, Neumark, and Rodriguez-

[^3]Table 1: Earnings per worker, establishment shares, and employment shares of 20 U.S. industries, 1990 and 2016

| Industry | 1990 |  |  |  | 2016 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Earnings ranking | $\begin{gathered} \text { Yearly } \\ \text { earnings } \end{gathered}$ | Estab. share | Emp. <br> share | Earnings ranking | Yearly earnings | Estab. share | Emp. <br> share |
| Restaurants | 1 | 7.68 | 6.86\% | 7.21\% | 1 | 17.36 | 8.06\% | 9.37\% |
| Retail trade | 2 | 13.47 | 18.91\% | 13.94\% | 2 | 27.08 | 13.57\% | 12.81\% |
| Services | 3 | 14.06 | 19.37\% | 16.40\% | 3 | 33.02 | 20.73\% | 22.92\% |
| Textiles/apparel | 4 | 15.92 | 0.55\% | 1.99\% | 4 | 36.20 | 0.23\% | 0.31\% |
| Wood/furniture | 5 | 19.73 | 0.80\% | 1.36\% | 5 | 41.76 | 0.49\% | 0.68\% |
| Other manufacturing | 6 | 21.36 | 0.31\% | 0.44\% | 7 | 47.40 | 0.19\% | 0.19\% |
| Food/tobacco | 7 | 23.98 | 0.34\% | 1.62\% | 6 | 45.28 | 0.37\% | 1.31\% |
| Health services | 8 | 24.27 | 7.45\% | 9.83\% | 10 | 53.87 | 8.83\% | 12.78\% |
| Plastics/clay/stone | 9 | 24.72 | 0.54\% | 1.57\% | 8 | 49.80 | 0.35\% | 0.91\% |
| Primary | 10 | 25.10 | 1.95\% | 1.29\% | 9 | 52.35 | 2.59\% | 1.52\% |
| Construction | 11 | 25.22 | 10.12\% | $5.94 \%$ | 12 | 58.69 | 9.06\% | 5.13\% |
| Paper/printing | 12 | 26.94 | 1.19\% | 2.44\% | 14 | 63.76 | 0.63\% | 1.04\% |
| Wholesale trade | 13 | 27.97 | 8.02\% | 6.69\% | 16 | 66.68 | 6.23\% | 5.50\% |
| Finance/insurance/real estate | 14 | 28.00 | 9.24\% | 7.60\% | 19 | 86.09 | 11.21\% | 7.05\% |
| Metals | 15 | 28.31 | 0.76\% | 2.46\% | 11 | 54.19 | 0.54\% | 1.36\% |
| Transp./comm./elec./gas/sanitary | 16 | 28.98 | 3.94\% | 5.88\% | 13 | 60.16 | 4.71\% | 5.50\% |
| Equipment | 17 | 30.33 | 1.35\% | 4.94\% | 15 | 66.18 | 0.86\% | 2.21\% |
| Legal/consulting/computing services | 18 | 34.43 | 7.88\% | $5.27 \%$ | 20 | 91.09 | 11.01\% | 7.67\% |
| Transportation manufacturing | 19 | 35.02 | 0.19\% | 2.03\% | 17 | 69.44 | 0.15\% | 1.04\% |
| Chemicals/petroleum | 20 | 35.94 | 0.25\% | 1.11\% | 18 | 84.35 | 0.20\% | 0.70\% |

Notes: Yearly earnings per worker are in thousands of U.S. dollars.

Lopez, 2022), our econometric specification for the relationship between the number of establishments and minimum wages is

$$
\begin{equation*}
\ln e_{i p t}=\alpha+\beta \ln M W_{i t}+\gamma \ln P_{i t}+\eta_{i}+\tau_{p t}+\nu_{i t} \tag{1}
\end{equation*}
$$

where for commuting zone-state $i$ from pair $p$ in year $t, e_{i p t}$ is the number of establishments, $M W_{i t}$ is the minimum wage, $P_{i t}$ is the working-age population, $\eta_{i}$ is a commuting zone-state $i$ fixed effect, and $\tau_{p t}$ denotes pair-year fixed effects (which control for spatial heterogeneity at the local level), and $\nu_{i t}$ is the error term.

From the previous econometric specification, our coefficient of interest is $\beta$, which denotes the elasticity of the number of establishments to the minimum wage. Using the multi-way fixed-effect estimator of Correia (2016), which allows us to easily control for commuting zone-state fixed effects and pair-year fixed effects, Table 2 presents our results from the estimation of (1) for each of our 20 industries and overall. As in DLR, standard errors are two-way clustered at the state and bordersegment levels using the procedure of Cameron, Gelbach, and Miller (2011), with a border segment defined as a pair of states sharing a multi-state commuting zone.

Table 2 shows an overall minimum wage elasticity of establishment counts of -0.091 , which is significant at a $10 \%$ level. Moreover, Table 2 shows a negative relationship between minimum wages and establishment counts for 16 out of 20 industries, with the elasticity being statistically significant for six of them. From the numbers in Table 1, the industries with negative elasticities account for $94.7 \%$ of establishments in 1990 , and for $94.4 \%$ in 2016 , whereas those with significant elasticities account for $30.2 \%$ of establishments in 1990 and for $25.7 \%$ in 2016 . The point estimates for the statistically significant elasticities range from -0.137 for retail trade (industry 2 ) to -0.778 for plastics/clay/stone (industry 9). Notice that not only do the lowest-wage industries (restaurants and retail trade) have negative and significant estimated elasticities, mid-wage industries such as the primary sector (agriculture, forestry, fishing and mining), paper and printing, and metals as well.

Table 2 shows that the population control is positive and significant overall, so that a larger population is associated with more establishments. The population coefficient is also positive in 19 out of 20 industries, and is significant in 13 of them. To account for cyclical changes in the number of establishments, Table A-1 in the Appendix re-estimates specification (1) for each of the 20 industries, but adds as control the log of establishment counts in all the other industries. ${ }^{9}$ Although the minimum wage elasticities become slightly smaller in size, all of them retain their sign from Table 2 and only one coefficient loses its statistical significance (the restaurant industry point estimate declines in size

[^4]Table 2: Pair-approach estimation of minimum wage responses of establishment counts in the U.S., 1990-2016

| $\underline{\text { Industry } \rightarrow}$ | Twenty industries (sorted by 1990 earnings per worker) |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Overall | 1 | 2 | 3 | 4 | 5 | 6 |
| $\ln$ (minimum wage) | $\begin{gathered} -0.091^{*} \\ (0.048) \end{gathered}$ | $\begin{gathered} -0.208^{*} \\ (0.119) \end{gathered}$ | $\begin{gathered} -0.137^{* *} \\ (0.053) \end{gathered}$ | $\begin{aligned} & -0.061 \\ & (0.046) \end{aligned}$ | $\begin{gathered} -0.036 \\ (0.325) \end{gathered}$ | $\begin{gathered} 0.381 \\ (0.298) \end{gathered}$ | $\begin{gathered} 0.093 \\ (0.366) \end{gathered}$ |
| $\ln$ (population) | $\begin{gathered} 0.866^{* * *} \\ (0.083) \end{gathered}$ | $\begin{gathered} 1.063^{* * *} \\ (0.118) \end{gathered}$ | $\begin{gathered} 0.641^{* * *} \\ (0.092) \end{gathered}$ | $\begin{gathered} 0.789^{* * *} \\ (0.118) \end{gathered}$ | $\begin{gathered} 0.682 \\ (0.410) \end{gathered}$ | $\begin{gathered} 0.076 \\ (0.403) \end{gathered}$ | $\begin{aligned} & 1.799^{* *} \\ & (0.785) \end{aligned}$ |
| Observations | 8,134 | 8,134 | 8,134 | 8,134 | 5,740 | 7,196 | 6,164 |
| $\underline{\text { Industry }} \rightarrow$ | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
| $\ln$ (minimum wage) | $\begin{aligned} & -0.077 \\ & (0.154) \end{aligned}$ | $\begin{gathered} -0.202 \\ (0.151) \end{gathered}$ | $\begin{gathered} -0.778^{*} \\ (0.426) \end{gathered}$ | $\begin{gathered} -0.372^{* *} \\ (0.157) \end{gathered}$ | $\begin{aligned} & -0.105 \\ & (0.102) \end{aligned}$ | $\begin{gathered} -0.250^{* *} \\ (0.122) \end{gathered}$ | $\begin{aligned} & -0.048 \\ & (0.093) \end{aligned}$ |
| $\ln$ (population) | $\begin{gathered} 0.806^{* *} \\ (0.319) \end{gathered}$ | $\begin{gathered} 1.065^{* * *} \\ (0.141) \end{gathered}$ | $\begin{aligned} & -1.120 \\ & (1.022) \end{aligned}$ | $\begin{gathered} 0.916^{* *} \\ (0.440) \end{gathered}$ | $\begin{gathered} 0.853^{* * *} \\ (0.192) \end{gathered}$ | $\begin{gathered} 0.653^{* * *} \\ (0.193) \end{gathered}$ | $\begin{gathered} 0.753^{* * *} \\ (0.131) \end{gathered}$ |
| Observations | 6,456 | 8,056 | 7,212 | 8,004 | 8,128 | 7,732 | 8,094 |
| $\underline{\text { Industry } \rightarrow}$ | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| $\ln$ (minimum wage) | $\begin{aligned} & -0.077 \\ & (0.070) \end{aligned}$ | $\begin{aligned} & -0.645^{*} \\ & (0.368) \end{aligned}$ | $\begin{gathered} 0.033 \\ (0.082) \end{gathered}$ | $\begin{aligned} & -0.066 \\ & (0.217) \end{aligned}$ | $\begin{gathered} -0.110 \\ (0.120) \end{gathered}$ | $\begin{aligned} & -0.271 \\ & (0.328) \end{aligned}$ | $\begin{gathered} 0.441 \\ (0.282) \end{gathered}$ |
| $\ln$ (population) | $\begin{gathered} 0.843^{* * *} \\ (0.114) \end{gathered}$ | $\begin{gathered} 0.375 \\ (0.363) \end{gathered}$ | $\begin{gathered} 0.665^{* * *} \\ (0.158) \end{gathered}$ | $\begin{gathered} 0.272 \\ (0.286) \end{gathered}$ | $\begin{gathered} 1.121^{* * *} \\ (0.256) \end{gathered}$ | $\begin{gathered} 0.147 \\ (0.441) \end{gathered}$ | $\begin{gathered} 0.349 \\ (0.318) \end{gathered}$ |
| Observations | 8,134 | 6,382 | 8,116 | 7,208 | 8,094 | 6,344 | 5,346 |

Notes: This table reports $\hat{\beta}$ and $\hat{\gamma}$ from the estimation of equation (1) for 20 industries and overall using yearly data from 1990 to 2016. All regressions include commuting zone-state fixed effects and pair-year fixed effects. Industries are sorted according to the 1990 earnings ranking of Table 1. Standard errors (in parentheses) are two-way clustered at the state and border segment levels. The coefficients are statistically significant at the $* 10 \%, * * 5 \%$, or $* * * 1 \%$ level.
from -0.208 to -0.183 , with its $p$-value increasing from 0.088 to 0.11$).{ }^{10}$

### 2.3 Long-Term Effects of Minimum Wages

To assess the long-term effects of minimum wages on U.S. establishment counts, we follow DLR and estimate a distributed-lag version of (1) that includes two years of leads and four years of lags (see also Jha, Neumark, and Rodriguez-Lopez, 2022). The distributed-lag specification is

$$
\begin{equation*}
\ln e_{i p t}=\alpha+\sum_{k=-2}^{3} \beta_{-k} \Delta \ln M W_{i, t-k}+\beta_{-4} \ln M W_{i, t-4}+\gamma \ln P_{i t}+\eta_{i}+\tau_{p t}+\nu_{i t}, \tag{2}
\end{equation*}
$$

[^5]

Figure 1: Time path of minimum wage effects on the number of U.S. establishments with $90 \%$ confidence intervals
where $\Delta$ is a one-year difference operator. From (2), the seven $\beta$ parameters give the cumulative minimum wage elasticity of establishment counts, starting with $\beta_{2}$, which represents the lead effect two years before the minimum wage change, and up to $\beta_{-4}$, which denotes the cumulative elasticity four years after the minimum wage change. We estimate specification (2) for the 20 industries and overall, presenting all the results in Table A-2 in the Appendix.

For the overall regression, Figure 1 shows the estimates of the $\beta$ parameters along with $90 \%$ confidence intervals. We assume that the minimum wage change occurs at time $s$, and hence the plot starts at $s-2$ with $\hat{\beta}_{2}$, and continues through $s+4$ with $\hat{\beta}_{-4}$. The plot shows statistically significant medium- and long-term negative effects of minimum wages on U.S. establishment counts, with a clear change in the slope occurring around time $s$. The cumulative elasticity becomes significant at a $10 \%$ level at $s+2$ with a point estimate of -0.121 , and reaches -0.224 after four years of the minimum wage change. Notice that the four-year elasticity is about 2.5 times larger than the -0.091 contemporaneous elasticity of the previous section. Thus, there is evidence of persistent negative effects of minimum wages on the number of U.S. establishments.

For individual industries, Table A-2 in the Appendix shows that 16 out of 20 industries have negative four-year estimated elasticities, with five of them being statistically significant. Of those that are significant, the four-year estimated elasticity is -0.662 for restaurants, -0.298 for retail trade, -0.161 for services, -1.402 for plastics/clay/stone, and -0.792 for the primary sector. To sum up, our long-term results show that a $10 \%$ increase in the minimum wage is associated with a
$2.24 \%$ reduction in the number of U.S. establishments after four years, but industries are affected differently, with the three lowest-wage industries having reductions of $6.62 \%$ (restaurants), $2.98 \%$ (retail trade), and $1.61 \%$ (services).

## 3 The Model

This section presents a model with a monopsonistic labor market, heterogeneous firms, and endogenous firm variety. The model shows that a binding minimum wage reduces the mass of firms, which then reduces welfare because workers love employer variety. Here we present the relevant parts of the model, and leave the most technical details for section B in the Appendix.

### 3.1 Household Preferences and Production

The economy produces a single final good that is chosen as the numéraire. The final good is traded in a perfectly competitive market, and is produced by a finite mass, $M$, of heterogeneous firms. Firms produce the final good using labor, which is procured from a unit measure of households participating in a monopsonistic labor market.

As in Berger, Herkenhoff, and Mongey (2022), the utility function of the representative household is

$$
\begin{equation*}
\mathbb{U} \equiv C-\frac{N^{1+\frac{1}{\psi}}}{1+\frac{1}{\psi}}, \tag{3}
\end{equation*}
$$

where $C$ is the consumption of the final good, $N$ is the labor-supply index, and $\psi$ is the Frisch elasticity of labor supply. The labor-supply index is defined as

$$
\begin{equation*}
N=\left(\int_{\omega \in \Omega} l(\omega)^{\frac{1+\theta}{\theta}} d \omega\right)^{\frac{\theta}{1+\theta}} \tag{4}
\end{equation*}
$$

where $l(\omega)$ is the amount of labor supplied to firm $\omega, \Omega$ is a set of measure $M$ of firms/employers offering jobs, and $\theta>\psi$. The parameter $\theta>0$ is the elasticity of substitution across jobs from different firms, and accounts for workers' cost of mobility: the lower the value of $\theta$, the higher the mobility costs, and thus the greater the monopsony power of firms.

The above specification captures the love-of-variety for employers. To see this clearly, suppose there are $M$ identical firms, so that $l(\omega)=l$ is the same across firms and $N=M^{\frac{\theta}{1+\theta}} l$. For a constant amount of supplied labor, $L=M l$, note that the labor-supply index can be written as $N=\frac{L}{M^{1 /(1+\theta)}}$. Hence, the disutility from supplying the same amount of labor is lower the larger $M$ is.

Given the utility function in (3) and wages $w(\omega)$, for $\omega \in \Omega$, the representative household maximizes its utility by choosing, $C, N$, and allocating labor, $l(\omega)$, across firms. As shown in the

Appendix, this maximization exercise yields the firm-level labor supply function

$$
\begin{equation*}
l(\omega)=\frac{w(\omega)^{\theta}}{W^{\theta-\psi}} \tag{5}
\end{equation*}
$$

for $\omega \in \Omega$, where $W$ is an index of the wages available to the representative household, which is defined as

$$
\begin{equation*}
W=\left(\int_{\omega \in \Omega} w(\omega)^{1+\theta} d \omega\right)^{\frac{1}{1+\theta}} \tag{6}
\end{equation*}
$$

Firms take $W$ as given, and hence, the function in (5) features a constant wage-elasticity of labor supply, $\theta .{ }^{11}$ The firm-level labor supply is increasing in $w(\omega)$, and thus, the firm has monopsony power in the labor market.

The maximization problem also yields $N=W^{\psi}$ and hence, our assumption that $\theta>\psi$ simply means that the elasticity of the labor-supply index (also known as the Frisch elasticity) is smaller than the elasticity of firm-level labor supply. The wage bill of firms, which is given by $\int_{\omega \in \Omega} w(\omega) l(\omega) d \omega=W N=W^{1+\psi}$, equals the consumption of the household, $C$. Therefore, the welfare of the representative household in (3) can be rewritten as

$$
\begin{equation*}
\mathbb{U}=W N-\frac{N^{1+\frac{1}{\psi}}}{1+\frac{1}{\psi}}=\frac{W^{1+\psi}}{1+\psi}, \tag{7}
\end{equation*}
$$

Thus, welfare is increasing in the wage index, $W$.
As in Melitz (2003), after incurring an entry cost of $f_{E}$ in terms of the final good, each firm draws its productivity $\varphi$ from a distribution $G(\varphi)$. The firm produces for the market if and only if it can cover a fixed cost of operation, $f$, also in terms of the final good. ${ }^{12}$ After meeting the fixed cost, the production function for a firm with productivity $\varphi$ is $y(\varphi)=\varphi l$. Whereas the goods market is perfectly competitive, the labor market is monopsonistically competitive. Given (5) and using $\varphi$ instead of $\omega$ to identify each firm, the profit maximization problem of a firm with productivity $\varphi$ yields as solution

$$
\begin{equation*}
l(\varphi)=\left(\frac{\theta}{1+\theta}\right)^{\theta} \frac{\varphi^{\theta}}{W^{\theta-\psi}} \quad \text { and } \quad w(\varphi)=\left(\frac{\theta}{1+\theta}\right) \varphi . \tag{8}
\end{equation*}
$$

The solution shows that employment and wages are increasing in $\varphi$ : higher productivity firms employ more workers and pay higher wages. Note also that the solution for $w(\varphi)$ shows that a worker is paid a fraction $\frac{\theta}{1+\theta}$ of the value of the worker's marginal product, $\varphi$ (i.e., the proportional markdown

[^6]on wages, $\frac{1}{1+\theta}$, is the same for every firm). It follows that the gross profit function of a firm with productivity $\varphi, \pi(\varphi)=\varphi l(\varphi)-w(\varphi) l(\varphi)$, is given by
\[

$$
\begin{equation*}
\pi(\varphi)=\left[\frac{\theta^{\theta}}{(1+\theta)^{1+\theta}}\right] \frac{\varphi^{1+\theta}}{W^{\theta-\psi}} . \tag{9}
\end{equation*}
$$

\]

### 3.2 Decentralized Equilibrium and the Social Planner's Problem

As in Melitz (2003), there is a cutoff level of productivity, $\hat{\varphi}$, such that firms with productivity below $\hat{\varphi}$ cannot cover their fixed cost of operation and hence do not survive. The zero-cutoff-profit condition is $\pi(\hat{\varphi})=f$, which from (9) implies that $W^{\theta-\psi}=\left[\frac{\theta^{\theta}}{(1+\theta)^{1+\theta}}\right] \frac{\hat{\varphi}^{1+\theta}}{f}$, so that we can rewrite firm-level employment in (8) as $l(\varphi)=\frac{(1+\theta) f \varphi^{\theta}}{\hat{\varphi}^{1+\theta}}$ and the gross profit function in (9) as $\pi(\varphi)=\left(\frac{\varphi}{\varphi}\right)^{1+\theta} f$. Firms enter up to the point that the expected value of entry, $\int_{\hat{\varphi}}^{\infty}[\pi(\varphi)-f] g(\varphi) d \varphi$, is equal to the entry $\operatorname{cost}, f_{E}$; therefore, the free entry condition is given by

$$
\begin{equation*}
\int_{\hat{\varphi}}^{\infty}\left[\left(\frac{\varphi}{\hat{\varphi}}\right)^{1+\theta}-1\right] f g(\varphi) d \varphi=f_{E} \tag{10}
\end{equation*}
$$

Once we solve for $\hat{\varphi}$ from (10), we obtain the equilibrium $W$ from the zero-cutoff-profit condition, and thus, using (7) we obtain that welfare is $\mathbb{U}=\frac{1}{1+\psi}\left\{\left[\frac{\theta^{\theta}}{(1+\theta)^{1+\theta}}\right] \frac{\hat{\varphi}^{1+\theta}}{f}\right\}^{\frac{1+\psi}{\theta-\psi}}$.

Letting $M_{E}$ be the mass of entrants, the mass of producing firms, $M$, is simply the fraction of entrants that survive: $M=[1-G(\hat{\varphi})] M_{E}$. The equilibrium $M$ is determined from the definition of $W$ in (6), which can be rewritten as

$$
\begin{equation*}
W=\left[M \int_{\hat{\varphi}}^{\infty} w(\varphi)^{1+\theta} g(\varphi \mid \varphi \geq \hat{\varphi}) d \varphi\right]^{\frac{1}{1+\theta}} . \tag{11}
\end{equation*}
$$

Finally, total employment is obtained by aggregating firm-level employment across all producing firms, $L=M \int_{\hat{\varphi}}^{\infty} l(\varphi) g(\varphi \mid \varphi \geq \hat{\varphi}) d \varphi$, which can be rewritten as

$$
\begin{equation*}
L=\frac{(1+\theta) f M}{\hat{\varphi}^{1+\theta}} \int_{\hat{\varphi}}^{\infty} \varphi^{\theta} g(\varphi \mid \varphi \geq \hat{\varphi}) d \varphi . \tag{12}
\end{equation*}
$$

In the following, we refer to the decentralized equilibrium values as $\hat{\varphi}_{D}, l_{D}(\varphi), \mathbb{U}_{D}, M_{D}$, and $L_{D}$, where subscript $D$ denotes 'dencentralized'.

A social planner chooses $\hat{\varphi}, l(\varphi)$, and the mass of entrants, $M_{E}$, so as to maximize (3) subject to (4) and final-good consumption $(C)$ being equal to total final-good production minus final-good requirements to cover firms' entry and fixed costs. Section B. 3 in the Appendix shows the details of this standard maximization problem. Letting $\hat{\varphi}_{P}, l_{P}(\varphi), \mathbb{U}_{P}, M_{P}$, and $L_{P}$ denote the solution values from the planner's problem, the Appendix shows that $\hat{\varphi}_{P}=\hat{\varphi}_{D}, l_{P}(\varphi)=l_{D}(\varphi)$ for every $\varphi$,

$$
\frac{M_{P}}{M_{D}}=\frac{L_{P}}{L_{D}}=\left(\frac{1+\theta}{\theta}\right)^{\frac{(1+\theta) \psi}{\theta-\psi}}>1 \quad \text { and } \quad \frac{\mathbb{U}_{P}}{\mathbb{U}_{D}}=\frac{\theta-\psi}{(1+\theta)}\left(\frac{1+\theta}{\theta}\right)^{\frac{\theta(1+\psi)}{\theta-\psi}}>1 .
$$

Thus, the decentralized equilibrium has the same productivity cutoff and the same firm level employment as in the planner's problem, but the planner chooses a higher level of $M$, which results in a higher $L$ and higher welfare. In other words, the decentralized equilibrium provides a sub-optimal mass of firms.

Intuitively, for a given amount of supplied labor, the representative household's disutility from labor supply is smaller the larger the mass of firms (due to the household's love-of-variety for employers). The planner recognizes this and therefore, the perceived cost of providing an additional firm is lower in the planner's problem than in the decentralized case, so the planner ends up choosing a higher mass of firms. Importantly, the choice of labor across firms is not distorted in the decentralized case - the planner chooses the same allocation of resources across firms as in the decentralized outcome. This is a consequence of the constant elasticity of firm-level labor supply, which implies that all firms mark down wages below the value of the marginal product by the same proportion, resulting in an efficient allocation of resources across firms.

A natural question is whether there is a policy that can correct the distortion and restore optimality in the decentralized equilibrium. In section B. 4 in the Appendix we show that this is indeed the case: a wage subsidy of $\frac{1}{1+\theta}$ financed by a lump-sum tax on households restores optimality, so that the mass of firms, labor supply, and welfare in the decentralized case correspond to the planner's problem solution. ${ }^{13}$

### 3.3 Impact of a Minimum Wage Regulation

Denote a binding minimum wage by $\underline{w}$. Since the lowest productivity firm that survives in a decentralized equilibrium without any policy intervention offers a wage of $w\left(\hat{\varphi}_{D}\right)$, for the minimum wage to be binding it must be the case that $\underline{w}>w\left(\hat{\varphi}_{D}\right)$. Let $\underline{\varphi}$ denote lowest productivity level for which the desired wage offered by the firm, $\left(\frac{\theta}{1+\theta}\right) \underline{\varphi}$, equals $\underline{w}$. Therefore, $\underline{\varphi}=\frac{(1+\theta) \underline{w}}{\theta}$, and firms with $\varphi \geq \underline{\varphi}$ are unconstrained by the minimum wage, with their gross profits given by $\underline{\pi}(\varphi)=\left[\frac{\theta^{\theta}}{(1+\theta)^{1+\theta}}\right] \frac{\varphi^{1+\theta}}{W^{\theta-\psi}}$, where $\underline{W}$ is the wage index.

Let $\underline{\hat{\varphi}}$ denote the cutoff level of productivity in an equilibrium with a binding minimum wage, so that firms with $\varphi \in[\hat{\varphi}, \underline{\varphi})$ are minimum wage constrained. These firms' gross profits are directly proportional to their employed labor, $\underline{\pi}(\varphi)=(\varphi-\underline{w}) l(\varphi)$, and therefore, each of them hires $\frac{w^{\theta}}{\underline{W}^{\theta-\psi}}$,

[^7]which from (5) we know is the amount of labor that workers supply to a firm paying wage $\underline{w}$. The zero-cutoff-profit condition, $\underline{\pi}(\underline{\hat{\varphi}})=f$, is then $(\underline{\hat{\varphi}}-\underline{w}) \frac{w^{\theta}}{\underline{W^{\theta}-\psi}}=f$. Lastly, the free entry condition is $\int_{\hat{\varphi}}^{\infty}[\underline{\pi}(\varphi)-f] g(\varphi) d \varphi=f_{E}$, which can be rewritten as
\[

$$
\begin{equation*}
\int_{\underline{\hat{\varphi}}}^{\underline{\varphi}}\left[\frac{(\varphi-\underline{w}) \underline{w}^{\theta}}{\underline{W}^{\theta-\psi}}-f\right] g(\varphi) d \varphi+\int_{\underline{\varphi}}^{\infty}\left\{\left[\frac{\theta^{\theta}}{(1+\theta)^{1+\theta}}\right] \frac{\varphi^{1+\theta}}{\underline{W}^{\theta-\psi}}-f\right\} g(\varphi) d \varphi=f_{E} . \tag{13}
\end{equation*}
$$

\]

Using the definition of $\underline{\varphi}$, we solve for the equilibrium values of $\underline{\hat{\varphi}}$ and $\underline{W}$ from the zero-cutoff-profit condition and the free entry condition. We then solve for the equilibrium mass of firms ( $\underline{M}$ ), total employment $(\underline{L})$, and welfare ( $\underline{\mathbb{U}}$ ) using similar expressions to those in section 3.2. As well, the average wage, $\underline{\bar{w}}$, can be calculated as the ratio of the total wage bill $\left(\underline{W}^{1+\psi}\right)$ and total employment. The following proposition presents our model's main results.

## Proposition 1. (The effects of a binding minimum wage)

A binding minimum wage wipes out the least productive firms, and reduces the total mass of firms, the wage index, and workers' welfare. If productivity follows a Pareto distribution, then a binding minimum wage also reduces total employment and increases the average wage.

The proof of this proposition is in section B. 5 in the Appendix. Given that the minimum wage equilibrium approaches the decentralized equilibrium when $\underline{w} \rightarrow w\left(\hat{\varphi}_{D}\right)$, the proof simply shows that (i) for every productivity distribution, it holds that $\frac{d \hat{\varphi}}{d \underline{w}}>0, \frac{d M}{d \underline{w}}<0, \frac{d \underline{W}}{d \underline{w}}<0, \frac{d \underline{U}}{d \underline{w}}<0$, and thus $\underline{\hat{\varphi}}>\hat{\varphi}_{D}, \underline{M}<M_{D}, \underline{W}<W_{D}$, and $\underline{\mathbb{U}}<\mathbb{U}_{D}$; and that (ii) if the productivity distribution is Pareto, then it also unambiguously holds that $\frac{d \underline{L}}{d \underline{w}}<0$ and $\frac{d \bar{w}}{d \underline{w}}>0$, so that $\underline{L}<L_{D}$ and $\underline{\bar{w}}>\bar{w}_{D}$, where $\bar{w}_{D}$ is the average wage in the decentralized equilibrium. ${ }^{14}$

Supporting Proposition 1, our main empirical finding from section 2 is that an increase in the minimum wage is associated with reductions in U.S. establishment counts. In the model, a binding minimum wage makes the survival of low-productivity firms harder. This is captured by an increase in the cutoff productivity level, which then leads to a reduction in the mass of firms. The reduction in $\underline{M}$ causes a decline in the wage index, $\underline{W}$, which then translates into a reduction in welfare, $\underline{\mathbb{U}}=\frac{W^{1+\psi}}{1+\psi}$. Welfare declines due to workers' love-of-variety for employers. To see this, it is useful to refer to the definition of the wage index in (11), which depends on the mass of firms and firm-level

[^8]wages. Whereas firm-level wages increase to $\underline{w}$ for constrained firms, which pushes for an increase in $\underline{W}$, the reduction in $\underline{M}$ works in the opposite direction and is the dominant force. ${ }^{15}$

Notice that in spite of Melitz-type reallocation of resources from less productive firms to more productive firms, the minimum wage does not increase welfare. To understand why this is the case, recall from section 3.2 that the allocation of resources in the decentralized equilibrium is efficient ( $\hat{\varphi}_{P}=\hat{\varphi}_{D}$ and $l_{P}(\varphi)=l_{D}(\varphi)$ for every $\varphi$ ). Therefore, any reallocation induced by a binding minimum wage cannot be a source of welfare gain. On the other hand, we also know from section 3.2 that the mass of firms is suboptimal in the decentralized equilibrium. By further reducing the mass of firms, a binding minimum exacerbates the existing distortion. ${ }^{16}$

### 3.4 Welfare Effects of Minimum Wages

Given that the wage bill, $\underline{L} \underline{\bar{w}}$, equals $\underline{W}^{1+\psi}$, from (7) we can rewrite the expression for welfare as $\underline{\mathbb{U}}=\frac{\underline{L} \underline{\bar{w}}}{1+\psi}$. It follows that

$$
\begin{equation*}
\zeta_{\underline{\mathbb{U}}, \underline{w}}=\zeta_{\underline{L}, \underline{w}}+\zeta_{\underline{\bar{w}}, \underline{w}}, \tag{14}
\end{equation*}
$$

where $\zeta_{\underline{\mathbb{U}}, \underline{w}}$ is the minimum wage elasticity of welfare, and $\zeta_{\underline{L}, \underline{w}}$ and $\zeta_{\underline{\bar{w}}, \underline{w}}$ are minimum wage elasticities of total employment and the average wage. Hence, to quantify the welfare implications of our model, we use the data described in section 2.1 to estimate the elasticities on the right-hand side of equation (14).

Similar to Table 2, Tables A-3 and A-4 in the Appendix present the results from the estimation of equation (1), but using employment and earnings per worker instead of the number of establishments. The point estimate for the overall minimum wage elasticity of employment is significant and equal to -0.204 , whereas the point estimate for the overall minimum wage elasticity of earnings per worker is positive but insignificant at just 0.017 . Hence, in accordance with Proposition 1, our empirical results show that an increase in the minimum wage is associated with lower employment and higher earnings per worker in the United States, though the effect on worker earnings is negligible. Based on these values, from (14) we obtain that the estimated minimum wage elasticity of welfare is -0.187 so that, as predicted by Proposition 1, a 10 percent increase in the minimum wage is associated with a 1.87 percent loss in welfare. ${ }^{17}$

[^9]For the two lowest-earnings industries, our estimated minimum wage elasticities of employment are -0.273 for restaurants and -0.119 for retail trade, with both of them being significant, whereas the elasticities of worker earnings are 0.164 for restaurants and 0.039 for retail trade, with only the former being significant. Thus, the minimum wage elasticities of welfare are -0.109 for restaurants and -0.08 for retail trade. Nevertheless, and in contrast to the overall welfare elasticity, industrylevel welfare elasticities do not take into account that workers that lose their job in one industry may find a job in another industry.

## 4 Conclusion

Whereas we presented a simple model with competitive firms and monopsonistic labor markets, its key insights regarding the impact of a binding minimum wage on the mass of firms and employment will go through even if the product market were imperfectly competitive, as long as the number of firms is endogenous. The welfare effects would be different, however, depending on the precise specification of imperfect competition. For example, with standard CES preferences and monopolistic competition, a minimum wage-induced reduction in the mass of firms will reduce welfare through the consumption channel, in addition to the welfare loss discussed in the paper through the employer variety channel.

In our model, the employer variety effect arises due to idiosyncratic preferences of workers for employers offering different job characteristics, with these job characteristics being held constant. However, Clemens (2021) summarizes evidence on how employers may adjust job attributes like effort requirements, schedule flexibility, and training opportunities in response to changes in minimum wages. A potential extension of our framework is to study how these extra margins of adjustment affect the impact of minimum wages on establishment counts, employment, and welfare.
establishment counts ( -0.091 ), which implies that average firm size declines with the minimum wage. On the other hand, our model predicts that average firm size increases with the minimum wage, which is a consequence of our simplifying assumption of a production function with constant returns to scale. In the case with decreasing returns to scale (see footnote 15) it is possible that average firm size declines in response to the minimum wage. This possibility arises because in that case the minimum wage can reduce employment in some constrained firms.

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[^0]:    ${ }^{1}$ DLR study the effects of minimum wages on restaurant employment by exploiting minimum wage variation within county pairs sharing a state border, and find a positive - but small and insignificant-elasticity. Jha, Neumark, and Rodriguez-Lopez (2022) show that DLR's results crucially depend on their definition of local economic area. Using the same cross-border design, but defining local economic areas as multi-state commuting zones, Jha, Neumark, and Rodriguez-Lopez (2022) obtain a negative and significant minimum wage elasticity of restaurant employment of -0.141 when using DLR's QCEW 1990-2006 data, and an elasticity of -0.242 when using the same CBP 1990-2016 data as in this paper. Jha, Neumark, and Rodriguez-Lopez (2022) also show that multi-state commuting zones are better in capturing local economic shocks than cross-border county pairs. Allegretto, Dube, and Reich (2009) also use multi-state commuting zones in their analysis of minimum wages and teen employment, mentioning that: "these areas are not only contiguous; they are also demonstrably linked with each other by an economically meaningful criterion".

[^1]:    ${ }^{2}$ In related work, in Jha and Rodriguez-Lopez (2021) we study the effects of international trade on inequality and welfare when the labor market is monopsonistic and employer variety matters. Dustmann, Lindner, Schönberg, Umkehrer, and vom Berge (2021) study the reallocation effects of minimum wages following the introduction of a nationwide minimum wage in Germany that affected 15 percent of all employees. They find that the minimum wage raised wages and did not lower employment, but induced low-wage workers to move from small, low-paying firms to larger, higher-paying firms at the expense of increased commuting time. The latter finding highlights the importance of idiosyncratic, non-pecuniary factors in workers' preferences for employers.
    ${ }^{3}$ This parallels the result in Dhingra and Morrow (2019) where with CES preferences, monopolistic competition is efficient.

[^2]:    ${ }^{4}$ Although the CBP data can be obtained up to 2019, we do not use 2017-2019 data because the CBP stopped reporting full establishment counts since the 2017 release. In particular, since 2017 the CBP omits establishment counts from county-industry cells with less than three establishments. This is an important limitation for CBP post-2016 data: whereas the 2016 data includes 784,474 county-industry cells with a positive establishment count, the 2017 data only includes 350,097.
    ${ }^{5}$ The District of Columbia, which belongs to the three-state commuting zone DC-VA-MD, is not included in our analysis because it appears in the CBP data starting in 2004. Therefore, we treat the DC-VA-MD area as a two-state commuting zone.
    ${ }^{6}$ Jha, Neumark, and Rodriguez-Lopez (2022) show that the 137 multi-state commuting zones are fairly distributed within the continental U.S., and that they follow similar patterns to the rest of the country for the number of establishments, total employment, employment-to-population ratios, earnings per worker, and average minimum wages.

[^3]:    ${ }^{7}$ Compared to retail trade (the second lowest-earnings industry), earnings in restaurants were $43 \%$ lower in 1990 and $36 \%$ lower in 2016.
    ${ }^{8}$ The minimum wage data is available at this link.

[^4]:    ${ }^{9}$ The Appendix is available at http://www.socsci.uci.edu/~jantonio/Papers/minwage_variety_app.pdf.

[^5]:    ${ }^{10}$ Using establishment counts in the rest of the industries as control leads to an attenuation bias of the minimum wage effect, as minimum wages are negatively related to the number of establishments in most industries. That is, even though the regressor is intended to account for cyclical effects on establishment counts, it is a "bad control" or overcontrol.

[^6]:    ${ }^{11}$ Jha and Rodriguez-Lopez (2021) and Egger, Kreickemeier, Moser, and Wrona (2021) also derive a constant elasticity labor supply function by using a random utility framework where workers have idiosyncratic preferences for employers. Close to the endogenous-labor-supply feature of our model, Bhaskar and To (1999) study the implications of minimum wages in a setting where firms' monopsony power emerges due to workers' commuting costs, so that firms must pay higher wages to attract workers from farther away.
    ${ }^{12} \mathrm{We}$ model entry and fixed costs in terms of the final good so that it is the same for all firms. Modeling it in terms of labor will make it different for firms because each firm pays a different wage in equilibrium.

[^7]:    ${ }^{13}$ Cahuc and Laroque (2014) study optimal policies in a monopsony model where workers are heterogeneous in productivity and in working opportunity costs-heterogeneous opportunity costs generate an upward-sloping labor supply curve, giving rise to monopsony power (as in Bhaskar and To, 1999). Similar to our findings, the monopsony distortion leads to suboptimal employment, which is corrected by a wage subsidy. The possibility of suboptimal employment also arises in the search model of Flinn (2006) if the bargaining power of workers is less than the elasticity of the matching function with respect to searchers. A minimum wage could potentially correct this distortion and increase employment.

[^8]:    ${ }^{14}$ Since Chaney (2008), the Pareto distribution has been used extensively in applications of the Melitz model, as it brings substantial tractability gains. This is also true for our case, where it allows us to obtain closed-form solutions for $d \underline{L} / d \underline{w}$ and $d \underline{w} / d \underline{w}$. Although the second part of Proposition 1 cannot be proved for a general productivity distribution, we verified numerically that it holds for a lognormal distribution, $g(\varphi)=\frac{1}{\varphi \sqrt{2 \pi \rho}} \exp \left(-(\ln \varphi-\mu)^{2} / 2 \rho\right)$, with parameter values $\mu=-0.02$ and $\rho=0.35$. These values are from Combes, Duranton, Gobillon, Puga, and Roux (2012), who find that firm-level productivity of French firms is better approximated by a mix $95 \% \operatorname{lognormal}$ and $5 \%$ Pareto, and that restricting the distribution to be $100 \%$ lognormal yields our assumed values.

[^9]:    ${ }^{15}$ Note that firm-level wages for unconstrained firms do not change $(w(\varphi)=\theta \varphi /(1+\theta)$ for $\varphi \geq \varphi)$. If we assume instead a firm-level production function with decreasing returns to scale, $y(\varphi)=\varphi l^{\lambda}$, for $\lambda<1$, the equilibrium firmlevel wage for unconstrained firms is given by $w(\varphi)=\left\{[\lambda \theta /(1+\theta)] \underline{W}^{(\theta-\psi)(1-\lambda)} \varphi\right\}^{1 /[1+\theta(1-\lambda)]}$, which is increasing in $\underline{W}$. The result $d \underline{W} / d \underline{w}<0$ still holds with $\lambda<1$, and therefore, a binding minimum wage reduces unconstrained firms' wages.
    ${ }^{16}$ Berger, Herkenhoff, and Mongey (2022) show that a binding minimum wage in their oligopsony model can alleviate the distortion induced by firms' markdowns on wages, but in contrast to our model, they abstract from the welfare effects of employer variety because they consider a fixed number of firms.
    ${ }^{17}$ Note that the estimated elasticity of employment $(-0.204)$ is larger in magnitude than the estimated elasticity of

